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Air-density-dependent model for analysis of air heating associated					
with streamers, leaders, and transient luminous events					
Transient Luminous Events and TGFs					
Lightning Effects on the Upper Atmosphere					
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Comparison with Data

Scaling with Altitude

Model Formulation

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- 2 Model of Streamer-to-Spark Transition
- Comparison with Experimental Results
- 4 Streamer-to-Spark Transition between 0 and 70 km Altitudes





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- 5 Conclusions



Observations of Upward Discharges









Figure: (a) A black and white image of a 2-min time exposure of a blue jet [Wescott et al., 2001]. (b) Processed image obtained by averaging of sequence of video fields from observations reported in Pasko et al. [2002].

 Streamer structure of jets was first suggested by Petrov and Petrova [1999]



[Pasko et al., 2002]



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Mechanisms of Conductivity Increase [Naidis, 1999]

Thermal Mechanism

- O Heated gas expands
- Gas number density is lowered
- Q Ratio E/N increases
- Ionization rate grows
- Onductivity increases

Kinetic Mechanism

- Active particles (radicals and excited molecules) accumulate
- Detachment, electron impact ionization of radicals and associative ionization accelerate
- Balance between rates of generation and loss of electrons changes
- Onductivity increases

Depending on the regime, one mechanism dominates.

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Model of Streamer-to-Spark Transition: 1-D Gas Dynamics Model

- 1-D axisymmetric model
- Vibrational-translational relaxation processes
- Fast heating of air in the streamer channel

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \vec{v}) = 0$$

$$\frac{\partial}{\partial t} (\rho \vec{v}) + \nabla \cdot (\rho \vec{v} \vec{v}) = -\nabla p$$

$$\frac{\partial \varepsilon}{\partial t} + \nabla \cdot \{(\varepsilon + p) \vec{v}\} = \eta_{\rm T} Q_{\rm e} + Q_{\rm i} + Q_{\rm VT}$$

$$\frac{\partial \varepsilon_{\rm v}}{\partial t} + \nabla \cdot (\varepsilon_{\rm v} \vec{v}) = \eta_{\rm V} Q_{\rm e} - Q_{\rm VT}$$

= Q_e , Q_i , and Q_{VT} depend on n_0 , $n_{O_2^+}$, $n_{O_4^+}$, $n_{O_2^+N_2}$, n_{O^-} , $n_{O_2^-}$, $n_{O_3^-}$, and n_e derived from the kinetics model

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Model of Streamer-to-Spark Transition: 0-D Chemical Kinetics Scheme

- 15 components:
 - = Neutral particles: N₂, O₂, O, N, NO, N₂($A^{3}\Sigma_{u}^{+}$), N₂($B^{3}\Pi_{g}$), N₂($C^{3}\Pi_{u}$), N₂($a'^{1}\Sigma_{u}^{-}$), O₂($a^{1}\Delta_{g}$)
 - Positive ions: O_2^+ , O_4^+ , $O_2^+N_2$
 - Negative ions: \tilde{O}^- , O_2^- , \tilde{O}_3^-
 - Electrons: e
- Effects of gains in electron energy in collisions with vibrationally excited nitrogen molecules on the rate constants of ionization and dissociative attachment processes [e.g., Benilov and Naidis, 2003]
- Self-quenching of $N_2(A^3\Sigma_u^+)$
- Associative ionization of $N_2(A^3\Sigma_u^{\scriptscriptstyle +})$ and $N_2(a'^1\Sigma_u^{\scriptscriptstyle -})$
- General balance equation:

$$\frac{dn_{\rm e}}{dt} = \left(F_{\rm ion} + F_{\rm step} + F_{\rm d} - F_{\rm a_2} - F_{\rm a_3} - F_{\rm rec}\right) n_{\rm e}$$



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Comparison with Experimental Results



Figure: (left) Experimental and model streamer-to-spark transition times for various applied voltages. The solid lines represent the transition times under normal pressure ($p=10^5$ Pa) and reduced pressure ($p=0.75 \times 10^5$ Pa). (right) Same model and experimental data as in left panel but using reduced values of the applied field (EN_0/N) and of the transition times ($\tau_{\rm br} N/N_0$).



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Streamer-to-Spark Transition at 0 and 70 km Altitudes



Figure: Streamer-to-spark transition time at 0 km (left) and 70 km (right) altitudes.



Streamer-to-Spark Transition at 0 and 70 km Altitudes



Figure: Distribution of the reduced gas density on the radial coordinate for $EN_0/N =$ 19 kV/cm at 0 km at t=0, 0.3, 0.6, and 0.9 μ s (left), and at 70 km at t=10, 20, 30, and 40 ms (right).



Streamer-to-Spark Transition at 0 km Altitude



The major cause of spark formation:

- Heated gas expansion
- Accumulation of oxygen atoms and other active species [Naidis, 1999]
- Increase with time in the electron detachment rate
- Existence of two- and three-body processes

Figure: Streamer-to-spark dynamics at sea level for $EN_0/N = 19 \text{ kV/cm}$.





Streamer-to-Spark Transition at 70 km Altitude



Figure: Streamer-to-spark dynamics at 70 km for $EN_0/N = 19 \text{ kV/cm}$.

The major cause of spark formation:

- Gas expansion negligible
- Accumulation of oxygen atoms and other active species [Naidis, 1999]
- Increase with time in the electron detachment rate
- Disappearance of threebody processes



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Scaling with Air Density



Figure: Scaling of the breakdown times as a function of the neutral density for various applied electric fields and altitudes (0, 30, 50, and 70 km).

 $au_{
m br} \propto 1/{\it N}^{-1.11}$

- **a** faster than the timescale of Joule heating ($\propto N^{-2}$)
- slower than that of the vibrational–translational relaxation ($\propto N^{-1}$)



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- Principal Contributions
- Acknowledgements

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Principal	Contributions				

The principal results and contributions, which follow from the studies presented in this work, can be summarized as follows:

- A 1-D axisymmetric air density dependent model of streamer-to-spark transition is introduced.
- O The streamer-to-spark transition model results are successfully compared to experimental data obtained by Černák et al. [1995] and Larsson et al. [1998] at ground and near ground pressures.
- For a broad range of air densities (between altitudes 0 and 70 km) studied the streamer-to-spark transition time is demonstrated to scale with neutral density approximately as: $\tau_{\rm br} \propto 1/N$ therefore exhibiting a significant acceleration of the heating at low air densities in comparison with $1/N^2$ scaling predicted on the basis of simple similarity laws for Joule heating.



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THANK YOU FOR YOUR ATTENTION QUESTIONS?

This work is available online at: http://web.me.com/riousset/



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