



# New Methods for Physics-Based Neutral Density

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***Integrity ★ Service ★ Excellence***



# Project Goals & Motivation



## Goals:

- Blend data and physics-based I-T model to improve accuracy both where and when data is not available
- Identify the obstacles currently hindering physics-based I-T data assimilation techniques and design new ones

## Motivation:

- Empirical or climatological I-T models offer limited predictive capabilities
- Physics-based models offer better predictive ability, but significant advances to Data Assimilation techniques are needed first



# Data Assimilation

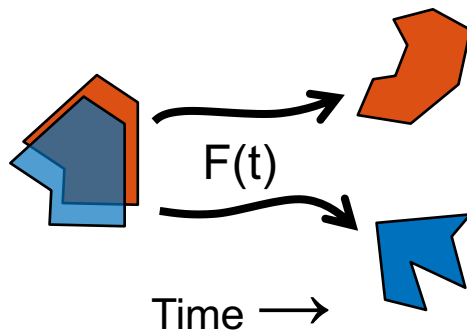
## Different Approaches for Different Systems



### Features of the Ionosphere-Thermosphere (I-T) system:

- Highly driven
- Sparsely observed

#### Chaotic System (e.g. tropospheric weather)



#### Strongly Driven System (e.g. Ionosphere-Thermosphere)

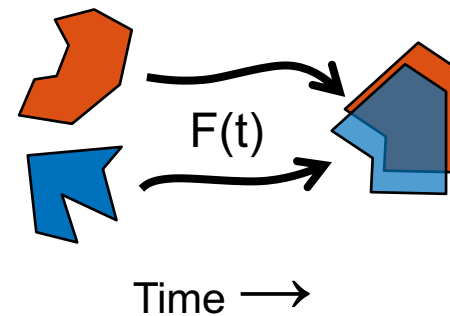


Image credit: S. Codrescu

See the method by [S. Codrescu et al. \[2018, Space Weather\]](#)



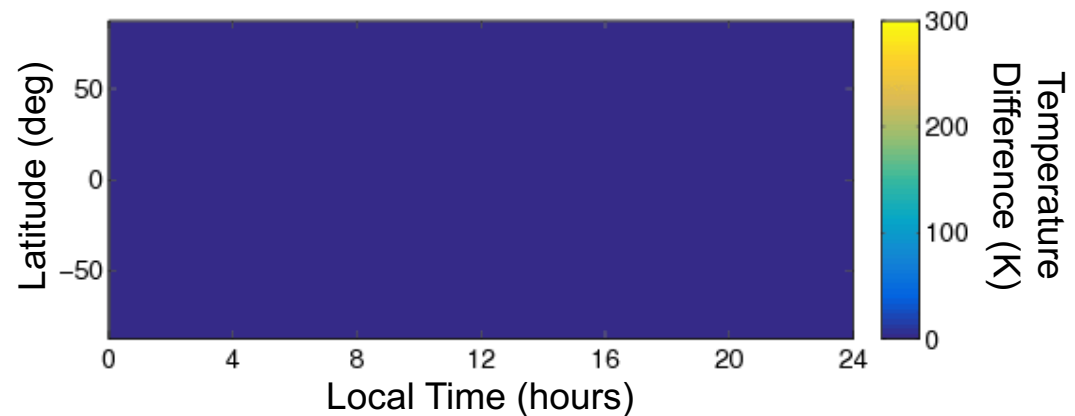
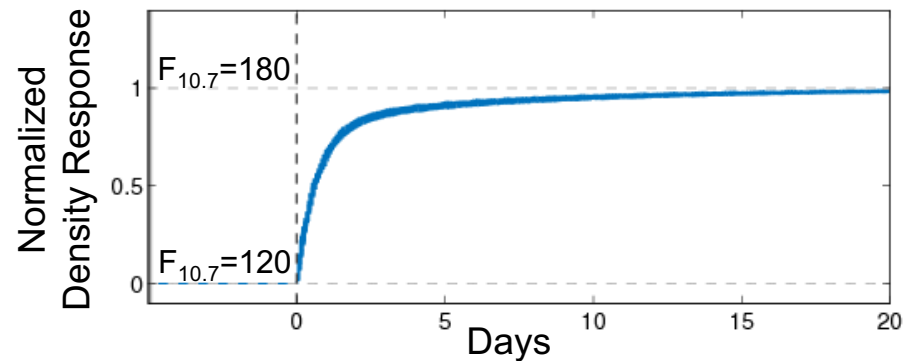
# I-T Response Characteristics

One example



## Response of the I-T to a step increase in solar irradiance:

- $F_{10.7}$  increases from 120 to 180 at  $t=0$
- Neutral density response as observed by a circular, polar satellite orbiting at 400 km altitude
- Density is normalized between two steady-state simulations ( $F_{10.7}=120$  and 180)
- The increase in temperature across the globe is shown below





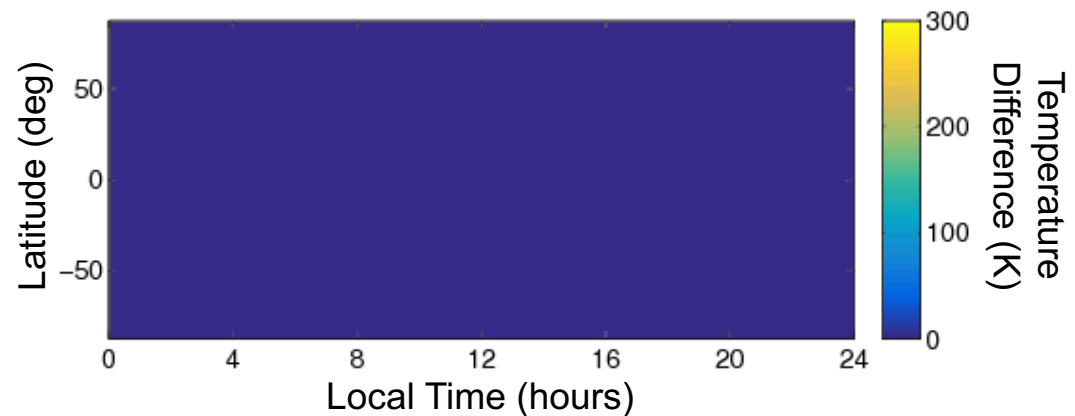
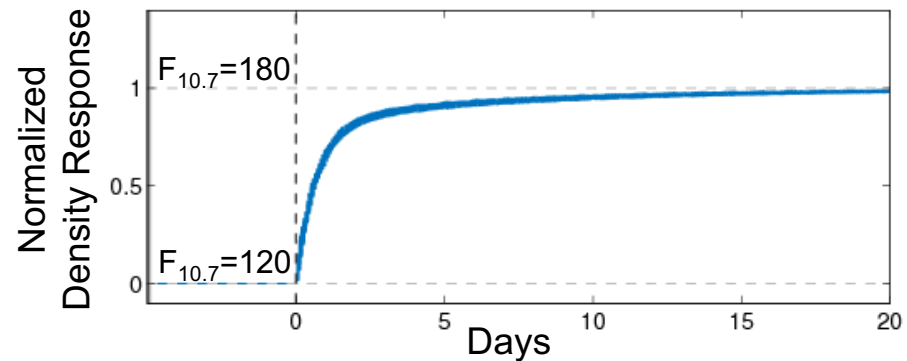
# I-T Response Characteristics

One example



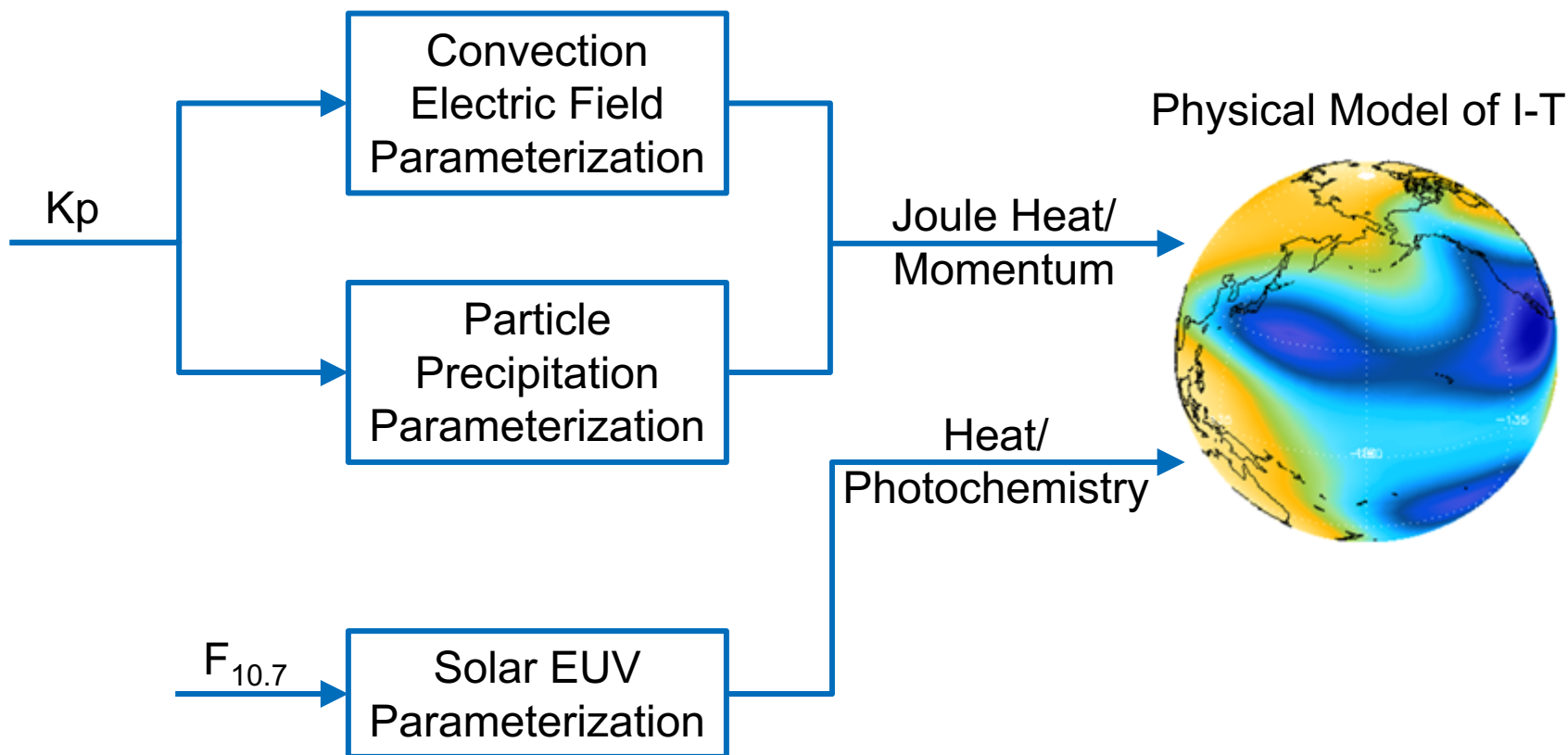
## Response of the I-T to a step increase in solar irradiance:

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# Drivers of an I-T Model





# Data Assimilation

## Obstacles



1. **Driven system:** initial conditions less important than conditions of the solar wind and solar flux
2. **Sluggish response:** thermosphere takes some time to respond to drivers
3. **Unknown drivers:** solar flux (EUV) and solar wind/magnetosphere/ionosphere coupling are not always well observed



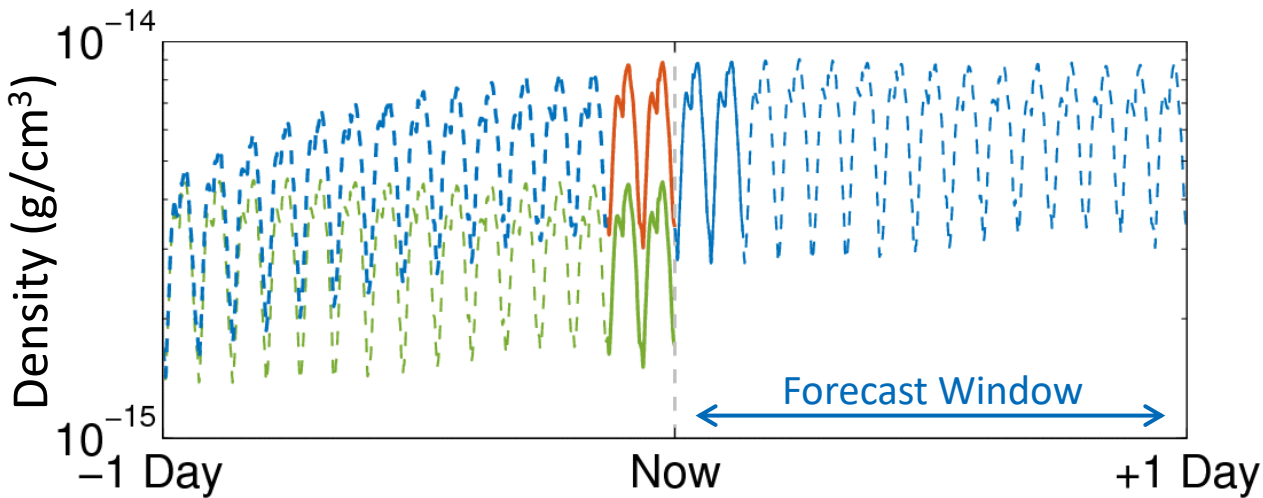
# Data Assimilation

## New Approach



### New approach to data assimilation:

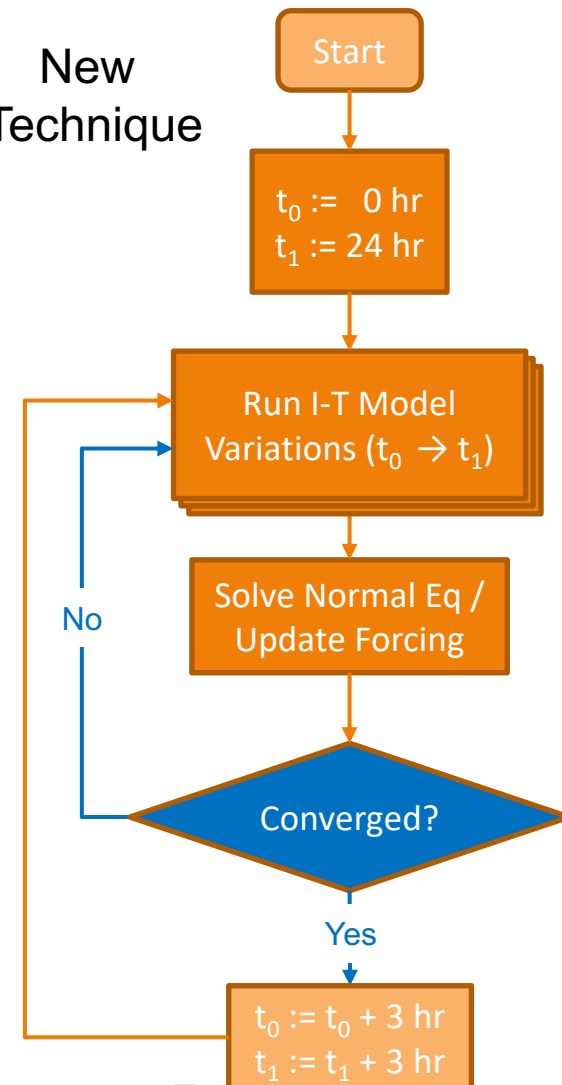
- Calculate what the driver *should* be for I-T model output to match observations
- Apply new estimated driver retrospectively to allow model to equilibrate



**Observations**  
**Initial guess from I-T Model**  
**I-T Model after data assimilation**

More details here: [Sutton \[2018, doi:10.1002/2017SW001785\]](https://doi.org/10.1002/2017SW001785)

### New Technique







# Physics-Based I-T Model

## TIE-GCM



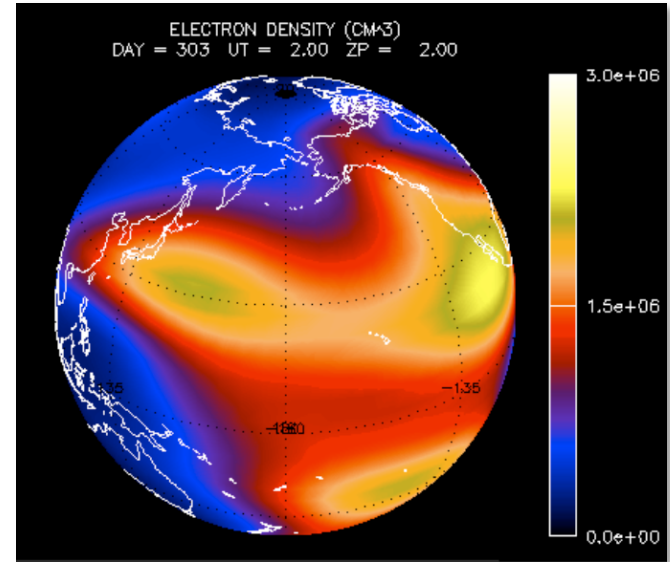
Solves the 3D neutral equations for:

- Energy
- Momentum
- Continuity
- Comp./chem. (O<sub>2</sub>, O, N<sub>2</sub>, +minor species)

and the ionospheric equations for:

- O<sup>+</sup> production/transport/chemistry
- O<sub>2</sub><sup>+</sup>, NO<sup>+</sup>, N<sub>2</sub><sup>+</sup>, N<sup>+</sup>, e<sup>-</sup> photochemical equilibrium
- Electric potential
- Ion/elect. Heating

<http://www.hao.ucar.edu/modeling/tgcm/tie.php>



$$\frac{\partial T'}{\partial t} = \frac{ge^z}{\rho_0 c_p} \frac{\partial}{\partial z} \left( \frac{K_T}{H} \frac{\partial T'}{\partial z} \right) - aT' - \mathbf{V} \cdot \nabla T' - w \left[ S + \frac{\partial T'}{\partial z} + \frac{RT'}{c_p m} \right] + Q'/c_p$$

$$\frac{\partial u}{\partial t} = \frac{ge^z}{P_0} \frac{\partial}{\partial z} \left( \frac{\mu}{H} \frac{\partial u}{\partial z} \right) + \left[ f + \frac{u}{r} \tan \phi - \lambda_{xy} \right] v - \lambda_{xx} u - \mathbf{V} \cdot \nabla u - w \frac{\partial u}{\partial z} - \frac{1}{r \cos \phi} \frac{\partial \Phi'}{\partial \lambda} + (F_\lambda + \lambda_{xy} v_l + \lambda_{xx} u_l)$$

$$\frac{\partial v}{\partial t} = \frac{ge^z}{\rho_0} \frac{\partial}{\partial z} \left( \frac{\mu}{H} \frac{\partial v}{\partial z} \right) - \left[ f + \frac{u}{r} \tan \phi - \lambda_{yx} \right] u - \lambda_{yy} v - \mathbf{V} \cdot \nabla v - w \frac{\partial v}{\partial z} - \frac{1}{r} \frac{\partial \Phi'}{\partial \phi} + (F_\phi + \lambda_{yy} v_l - \lambda_{yx} u_l)$$

$$\frac{\partial \Phi'}{\partial z} = R(T_0 + T')/m \quad \frac{1}{r \cos \phi} \frac{\partial}{\partial \phi} (v \cos \phi) + \frac{1}{r \cos \phi} \frac{\partial u}{\partial \lambda} + e^z \frac{\partial}{\partial z} (e^{-z} w) = 0$$

Thermosphere

Ionosphere

$$\frac{3}{2} N_e k_B \frac{\partial T_e}{\partial t} = -N_e k_B T_e \nabla \cdot \mathbf{u}_e - \frac{3}{2} N_e k_B u_e \cdot \nabla T_e - \nabla \cdot \mathbf{q}_e - \sum Q_e - \sum L_e$$

$$\sin^2 I \frac{\partial}{\partial H \partial Z} \left( \frac{2 K^0}{7 H} \frac{\partial G}{\partial Z} \right) - \left( \frac{L_{on} + L_{oi}}{T_e^{5/2}} \right) G = -L_{on} T_n - L_{oi} T_i - Q_e$$

$$\frac{\partial n}{\partial t} - Q + Ln = -\nabla \cdot n \mathbf{V}$$

$$\mathbf{V} = \mathbf{V}_\beta + \mathbf{V}_\perp$$

$$\mathbf{V}_\beta = \left\{ \mathbf{b} \cdot \frac{1}{\nu} \left[ \mathbf{g} - \frac{1}{\rho_i} \nabla (P_i + P_e) \right] + \mathbf{b} \cdot \mathbf{u} \right\} \mathbf{b}$$

$$\mathbf{V}_\perp = \frac{1}{|B|} \mathbf{E} \times \mathbf{b}$$

$$\nabla \cdot \sigma \cdot \nabla \Phi = \nabla \cdot \sigma \cdot (\mathbf{V}_n \times \mathbf{B})/c$$



# TIE-GCM vs. IRIDEA

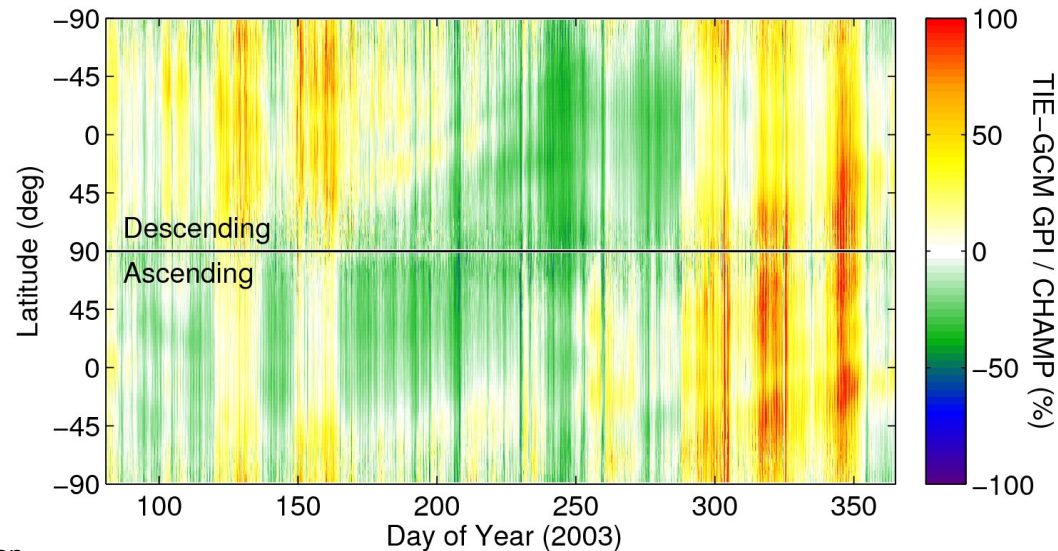
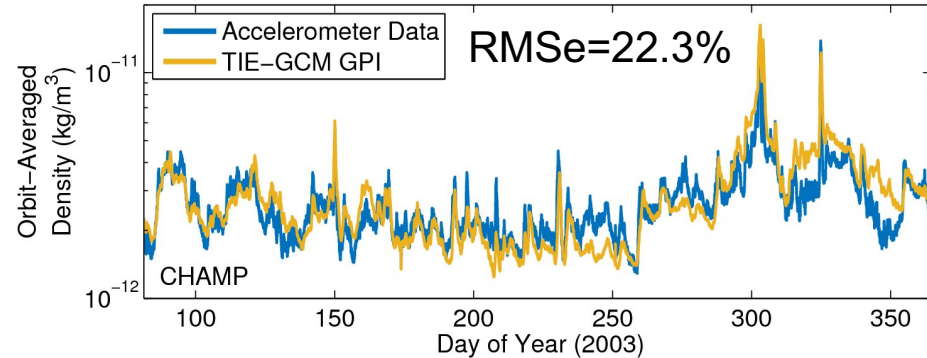
Day 80-365, 2003



## Without Data Assimilation

### Validate new approach, IRIDEA, with real-world scenario

- Simulate the **I-T without data assimilation**
- Simulate the **I-T with IRIDEA data assimilation**
  - Ingest CHAMP/STAR accelerometer observations at ~400 km
  - Estimate corrections to both solar flux and geomagnetic activity drivers
- Compare output of I-T model with observations of **neutral density from CHAMP**



IRIDEA: Iterative Re-Initialization, Driver Estimation, and Assimilation



# TIE-GCM vs. IRIDEA

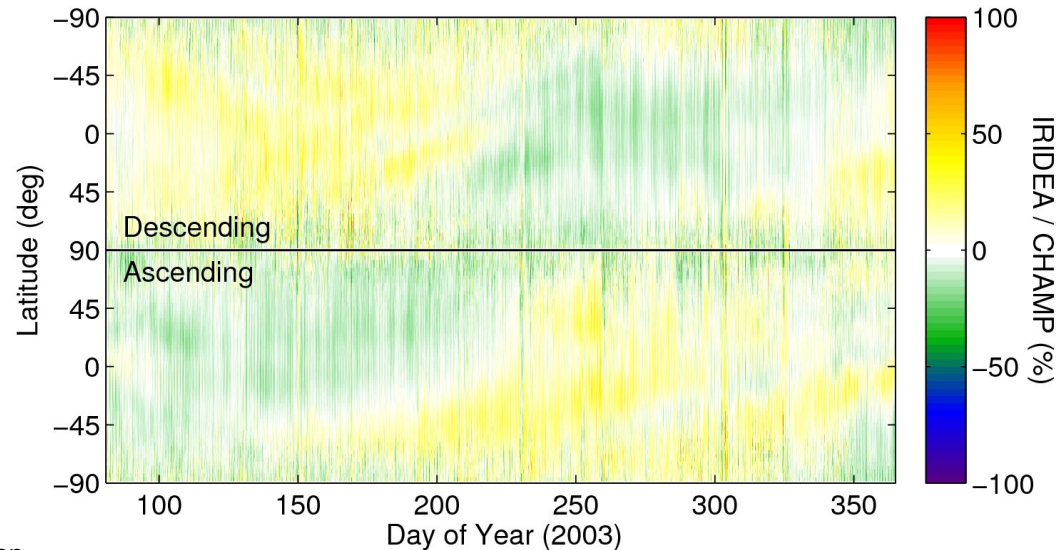
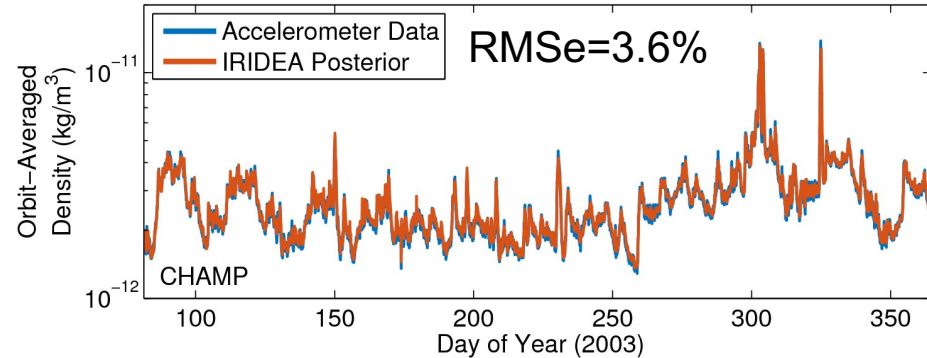
Day 80-365, 2003



## With IRIDEA Data Assimilation

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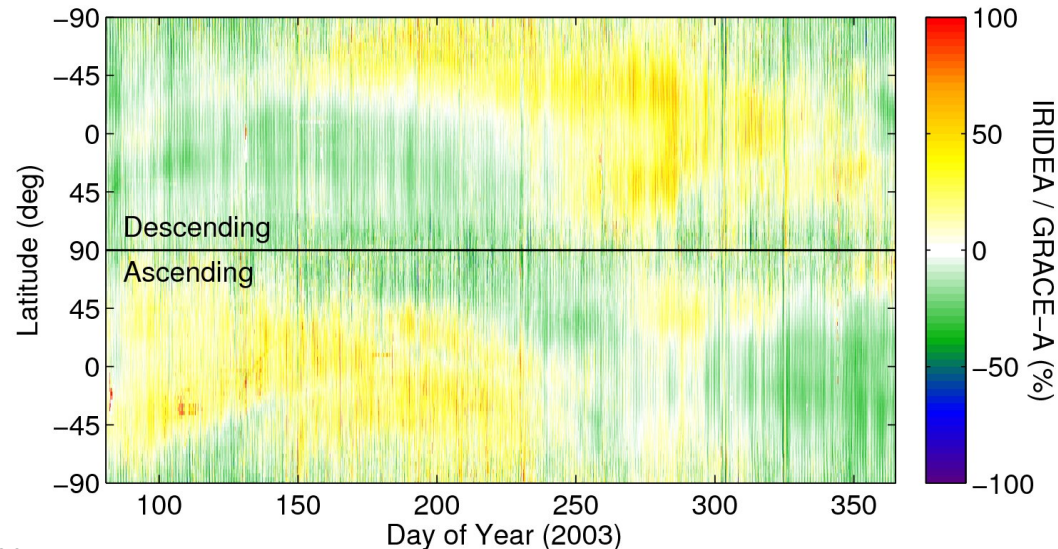
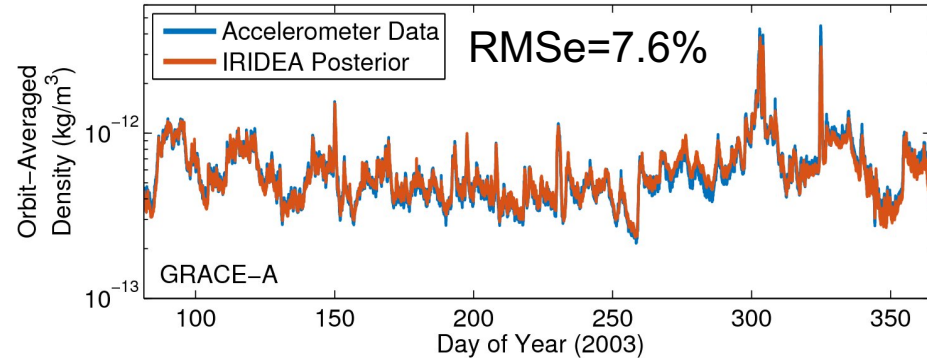
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## With IRIDEA Data Assimilation

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  - Ingest CHAMP/STAR accelerometer observations at ~400 km
  - Estimate corrections to both solar flux and geomagnetic activity drivers
- Compare output of I-T model with observations of **neutral density from GRACE** at ~500 km and separated in local time from CHAMP



IRIDEA: Iterative Re-Initialization, Driver Estimation, and Assimilation





# Observed vs. Estimated Drivers



## The estimated $F_{10.7}$ time series resembles the actual

- Solar rotational modulation is evident
- But, the spikes are probably not representative of EUV variations

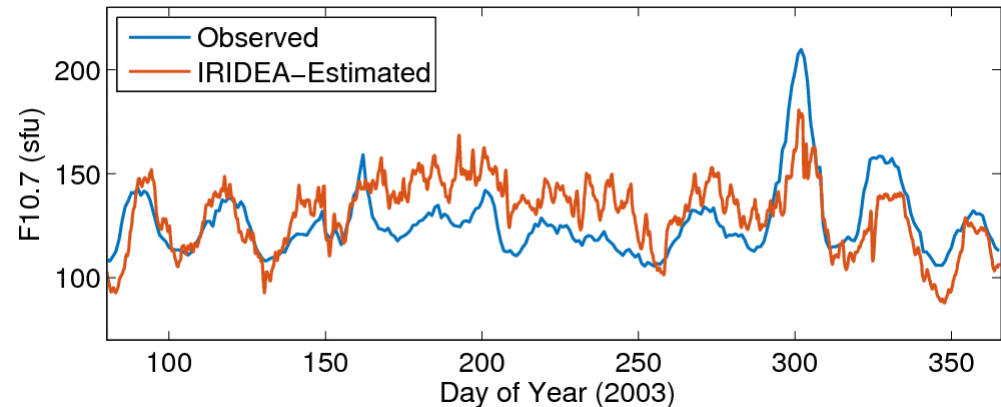
## The estimated Kp time series *somewhat* resembles the actual

- Better correlation when a daily running-maximum filter is applied
- Does TIE-GCM have a problem cooling down **or** is correlation of the estimated drivers causing this?

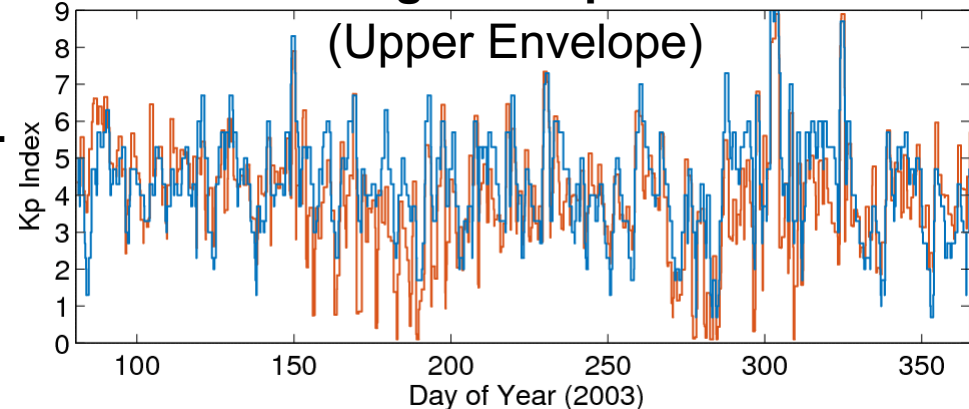
## How do we better disentangle solar vs. geomagnetic influences?

- Improve data coverage?
- Incorporate data types with better information content?
- Incorporate actual drivers into the mix?

## Solar Flux



## Geomagnetic Kp Index





# Summary



**A new data assimilation technique has been developed for I-T physics-based models:**

- Accounts for the driven I-T system with response time-scales of approximately 1 day
- Able to accurately specify neutral densities in both quiet and disturbed times for the first time

## Questions:

- How do we best incorporate actual drivers (e.g., EUV vs. F10.7)?
- How do we best incorporate forecasts of drivers?
- How do we best disentangle solar irradiance vs. geomagnetic driving?
- What measurements would be more ideal for driving this type of a technique?
- Are there analogs throughout Geospace?

### Results Recently Published in:

**Space Weather**  
RESEARCH ARTICLE

**A new method of physics-based data assimilation  
for the quiet and disturbed thermosphere**

10.1002/2017SW001785



This work was sponsored by the Air Force Office of Scientific Research. Travel was paid for by the NASA LWS Institute on Neutral Density Nowcasting.



# Backup Slides





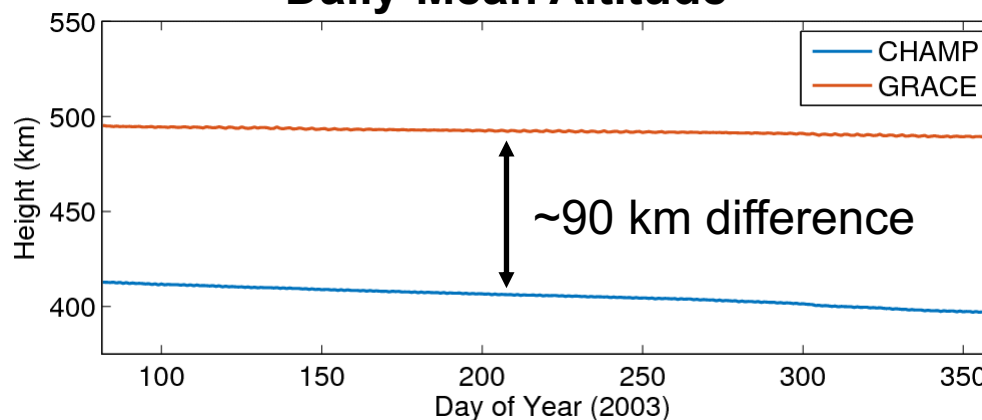
# Data Sets



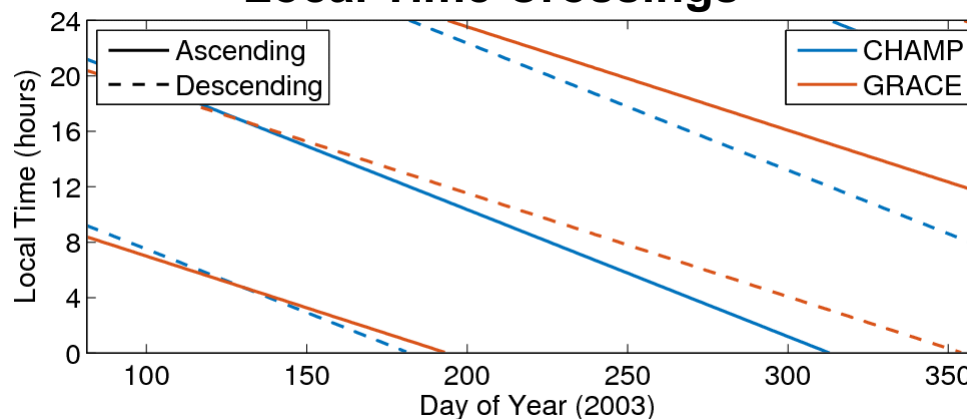
## Assimilation and Validation Data Sets:

- **Ingested data:** neutral densities measured onboard CHAMP satellite
- **Independent Validation Data:** neutral densities measured onboard GRACE-A satellite
- GRACE-A is ~90 km higher than CHAMP during the interval
- Local times align early in the interval, diverging near the end of the interval with a difference of ~4 hours
- Both Satellite orbits are circular and near-polar

## Daily-Mean Altitude



## Local Time Crossings







# Model Performance Metrics

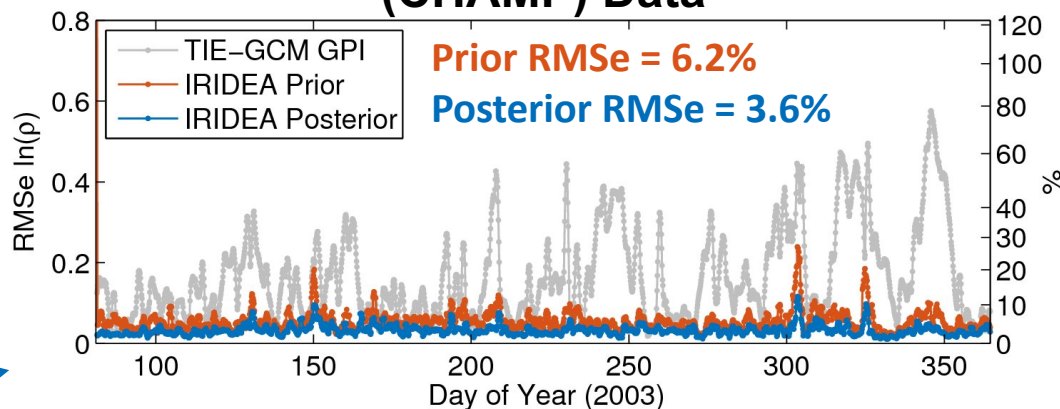


Day 80-365, 2003

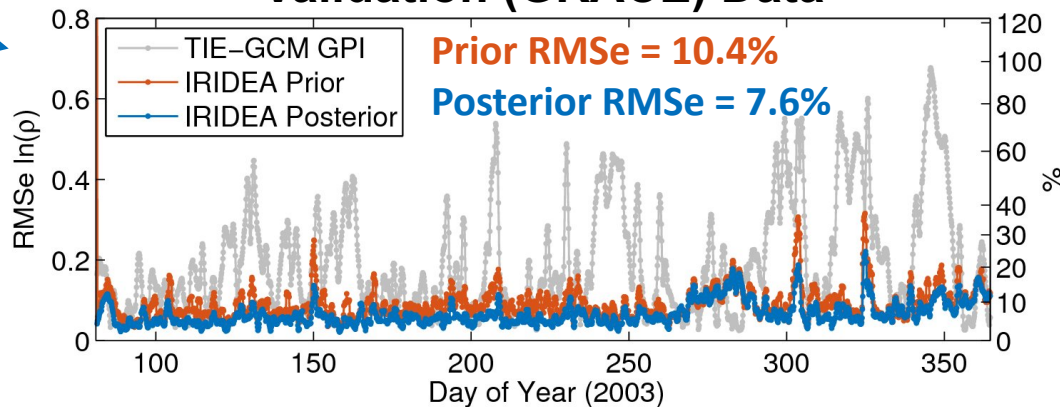
## Validate new approach, IRIDEA, with real-world scenario

- Root Mean Squared error (RMSe) of model simulations with respect to:
  - Ingested data
  - Independent validation data

### Comparison with the Ingested (CHAMP) Data



### Comparison with the Independent Validation (GRACE) Data





# Model Performance Metrics



2003

	TIE-GCM GPI	IRIDEA		JB-08	MSIS
		Prior	Posterior		
<b>CHAMP</b>					
$\mu(m/o)$	1.02	1.01	1.01	0.99	1.09
$\sigma(m/o)$	22.2%	6.1%	3.3%	13.1%	17.4%
RMSe	22.3%	6.2%	3.6%	13.1%	20.2%
<b>GRACE-A</b>					
$\mu(m/o)$	1.03	1.00	1.01	0.99	1.13
$\sigma(m/o)$	27.0%	10.3%	7.6%	17.2%	22.4%
RMSe	27.3%	10.4%	7.6%	17.2%	26.6%

Ingested Data

Independent Validation Data

$$\text{RMSe} = \sqrt{\frac{1}{N} \sum_{n=1}^N \left( \ln \frac{\rho_{m,i}}{\rho_{o,i}} \right)^2}$$

$$\mu(m/o) = \exp \left( \frac{1}{N} \sum_{n=1}^N \ln \frac{\rho_{m,i}}{\rho_{o,i}} \right)$$

$$\text{RMSe}^2 = \ln(\mu(m/o))^2 + \sigma(m/o)^2$$

$$\sigma(m/o) = \sqrt{\frac{1}{N} \sum_{n=1}^N \left( \ln \frac{\rho_{m,i}}{\rho_{o,i}} - \ln \mu(m/o) \right)^2}$$



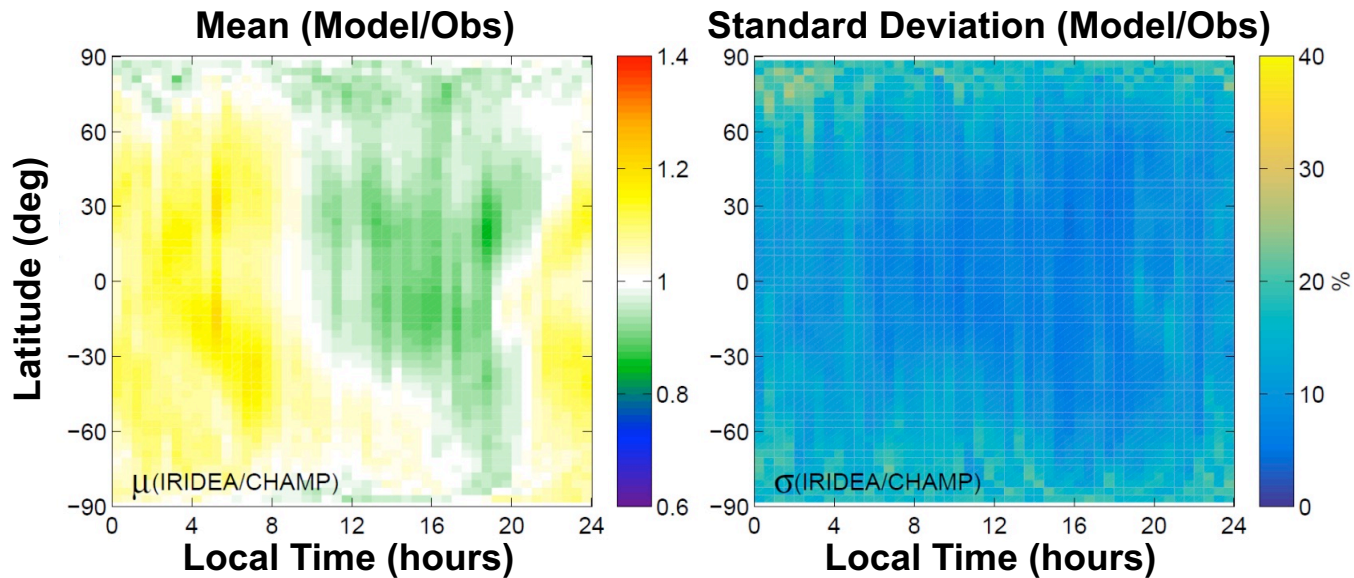
# Going Forward...

## Location-Dependent Errors



Orbit-averaged model output is greatly improved, but how do we minimize the remaining location-dependent errors?

### Binned IRIDEA-to-CHAMP Residuals



**Need to assess contributions from:**

- Lower atmosphere waves and tides
- Lower boundary considerations: TIE-GCM vs. TIME-GCM vs. WACCM-X
- Viscous and ion drag (and many other model parameters)