



Observations of Secondary Wave Manifestation Arising from Migrating Diurnal Tide-Quasi Two-Day Wave Interaction

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Nonlinear Wave-Wave Interactions

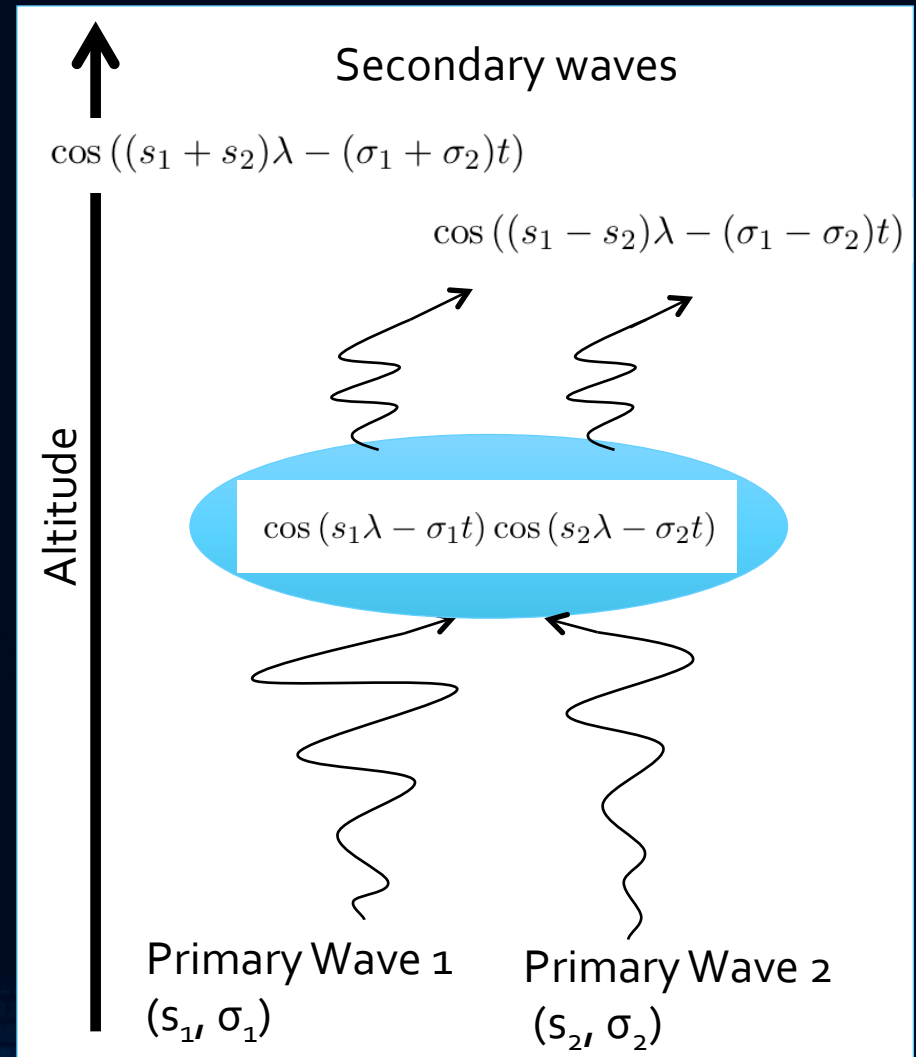
Theory of Nonlinear Interactions (Teitelbaum, 1991)

Sources of Tides/PWs

Solar Driven Processes in the Lower/Upper Atmosphere

Lunar gravitational

Nonlinear wave-wave Interactions



Previous Work on Nonlinear Interactions



Ground-Based Studies

- Numerous studies showing evidence of primary wave and secondary wave periodicities at the same location

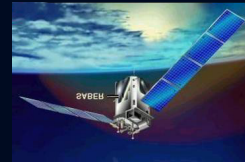


Limitations

- Ground-based studies cannot provide global information

Satellite-Based Studies

- Recent evidence of secondary waves on a global scale



Limitations

- Certain wave-wave interactions are difficult to observe (QTDW-DW₁) due to aliasing

Modeling-Based Studies

- Modeling studies using general circulation models (GCMs) support that secondary waves can be generated in the atmosphere



Limitations

- GCMs are complex
- Lack of observational basis

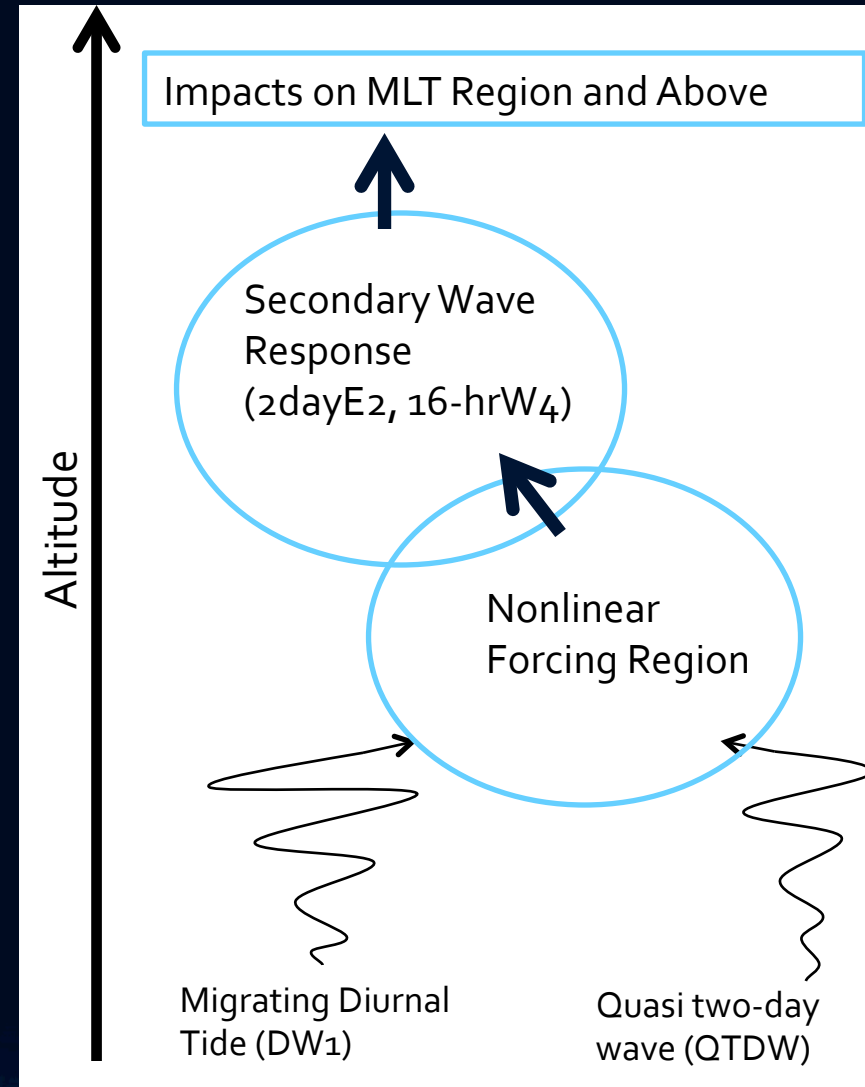


Science Questions

1. Where in the atmosphere is DW1 and QTDW interacting to force secondary waves and where do significant secondary wave responses occur?
2. How does the nonlinear forcing region affect the structure and propagation of the resulting secondary waves?

Methodology

Estimate the primary waves and secondary waves from satellite observations (EOS Aura-MLS and TIMED-SABER)

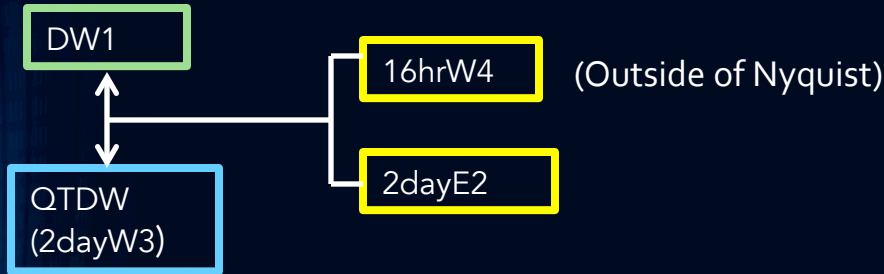




Secondary Wave Response

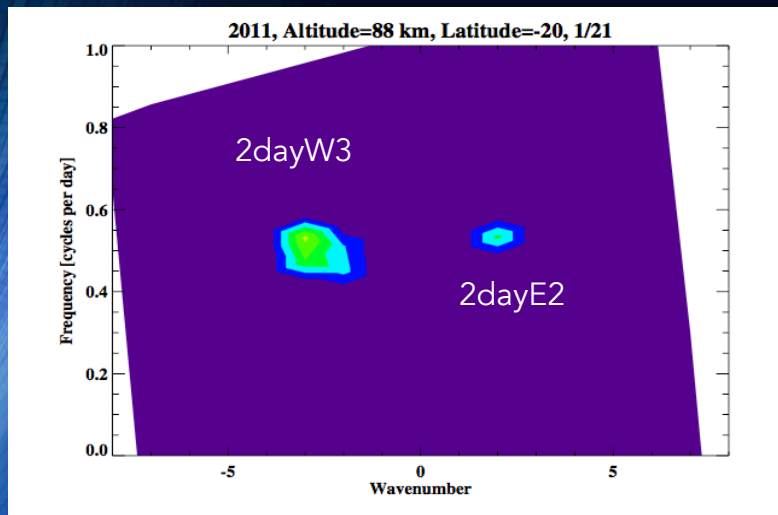
Primary Waves

Secondary Waves

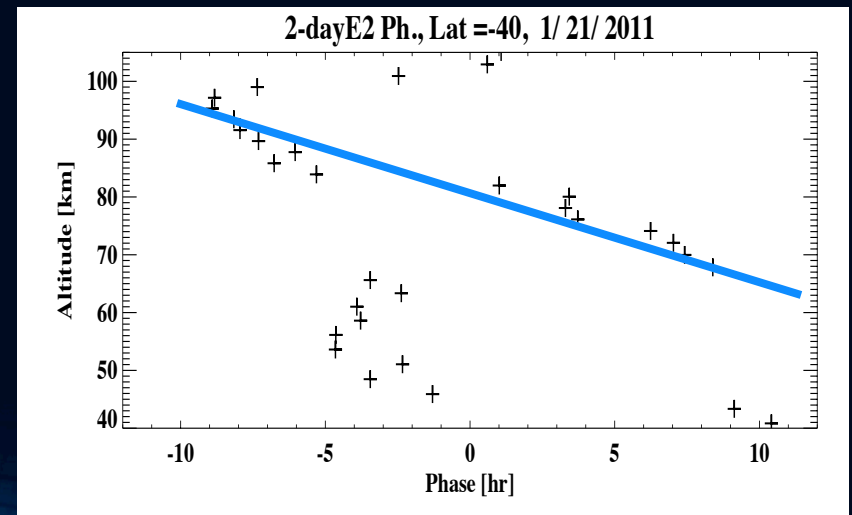
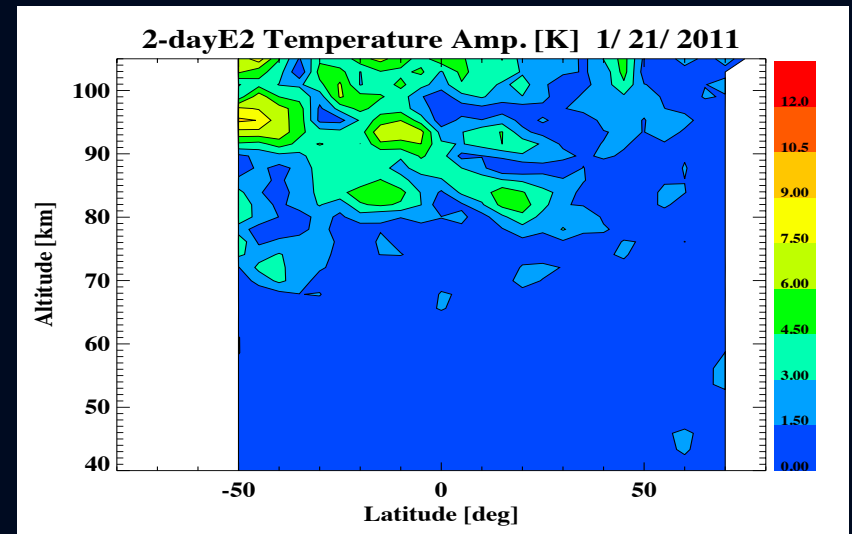


- FFSM (Salby, 1982) method completely separates the QTDW and 2-dayE2 from each other
- 2-dayE2 signal represents 2-dayE2/16hrW4 secondary wave activity

Frequency-Wavenumber Spectrum (Jan 2006)



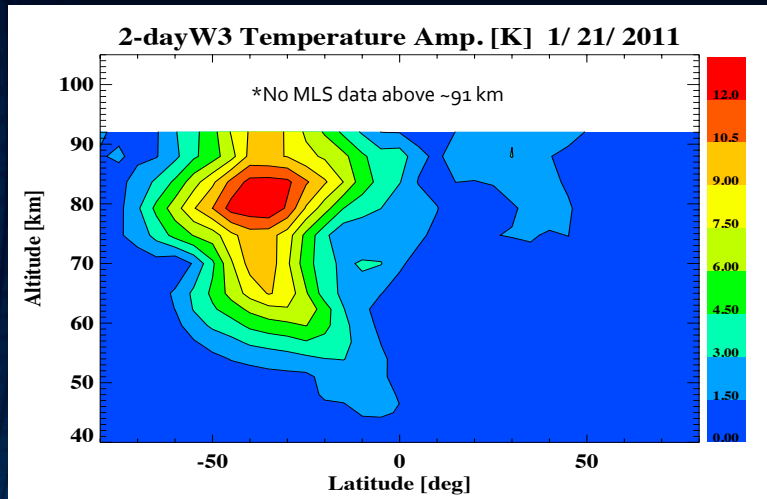
Secondary Wave from SABER



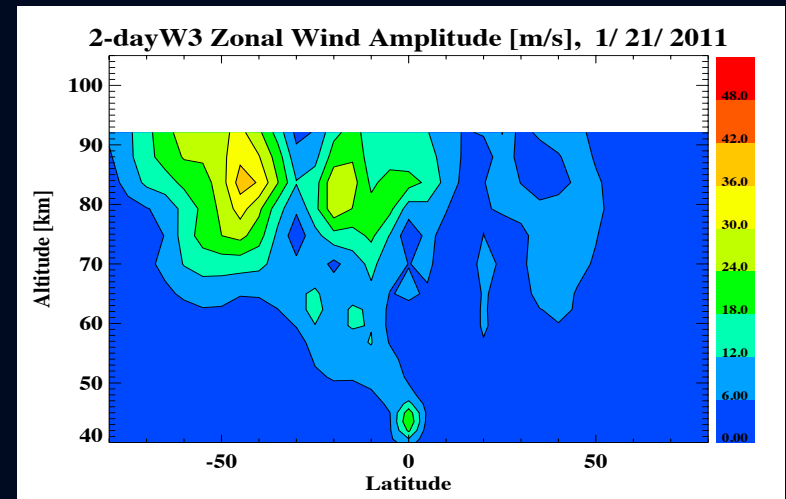


QTDW Temperatures, Winds

QTDW Temperature from Salby Method



Derived QTDW Winds



Compute QTDW u' and v' using momentum balance

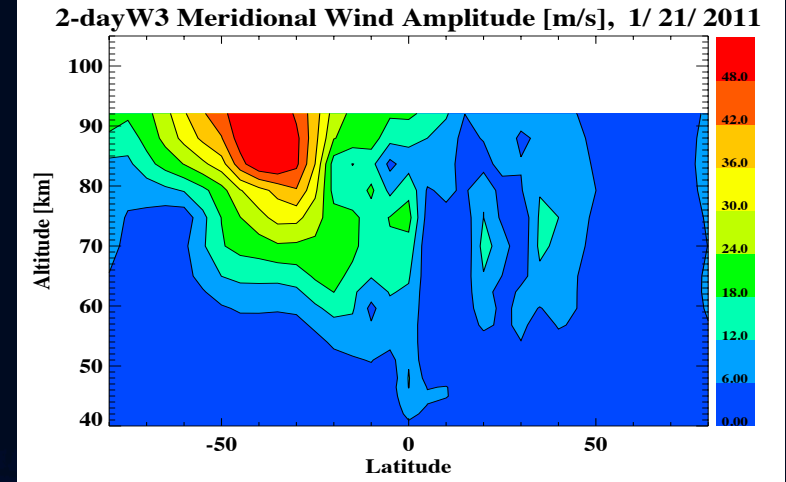


$$\frac{\partial u'}{\partial t} + \frac{\bar{u}}{a \cos \phi} \frac{\partial u'}{\partial \lambda} - \tilde{f} v' = -\frac{1}{a \cos \phi} \frac{\partial \Phi'}{\partial \lambda}$$

$$\frac{\partial v'}{\partial t} + \frac{\bar{u}}{a \cos \phi} \frac{\partial v'}{\partial \lambda} + \tilde{f} u' = -\frac{1}{a} \frac{\partial \Phi'}{\partial \phi}$$

Derived gradient background zonal wind

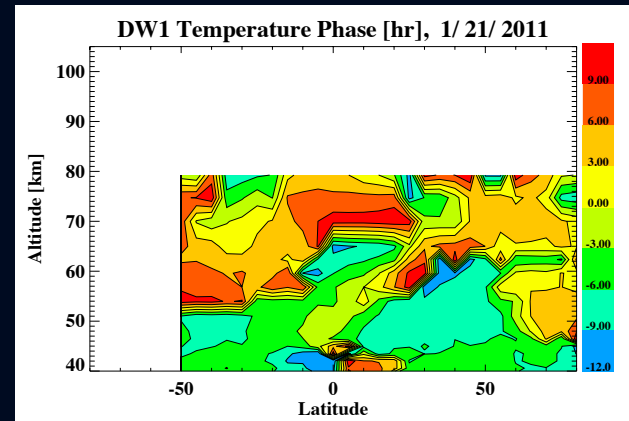
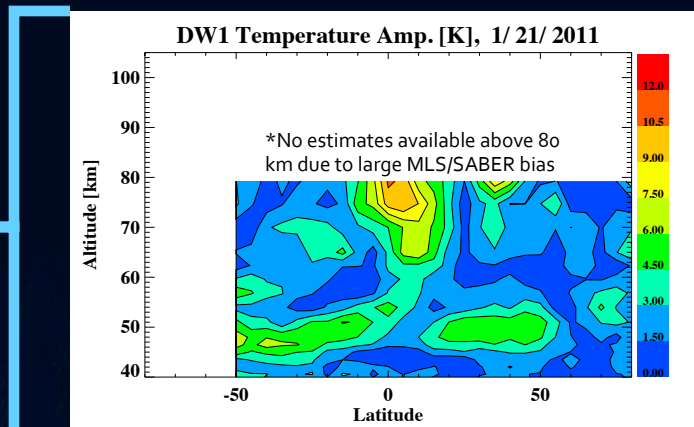
QTDW geopotential height from MLS observations



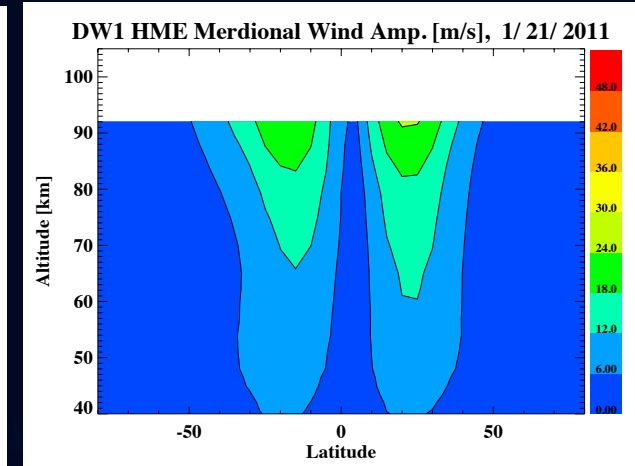
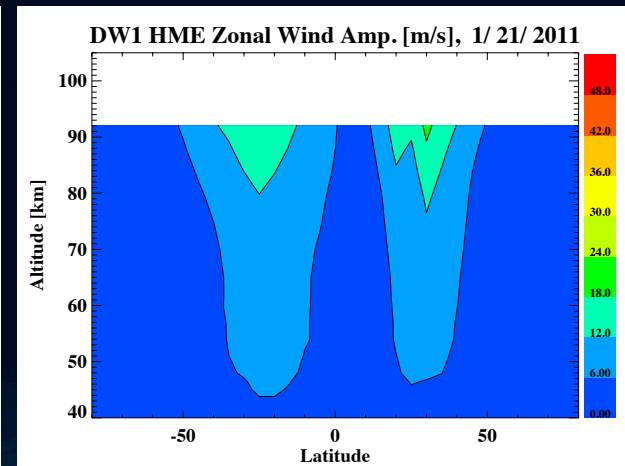
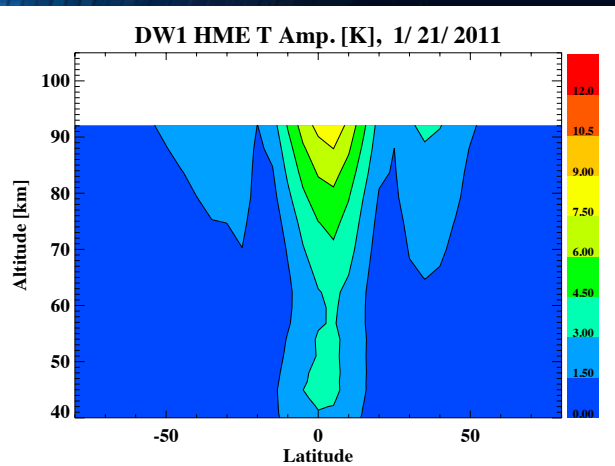


DW1 Temperature, Winds

Short-term temperature estimates of DW1 from combined MLS/SABER data
(Nguyen and Palo, 2013)



Fit to Global Scale Wave Model (GSWM) Hough Mode Extensions to derive horizontal winds





Nonlinear Forcing Term

Dynamics of the atmosphere are governed by conservation of momentum, energy, mass and ideal gas law

Conservation of momentum (zonal, meridional) and energy

$$\frac{\partial u}{\partial t} + \left\{ \frac{u}{a \cos \phi} \frac{\partial}{\partial \lambda} + \frac{v}{a} \frac{\partial}{\partial \phi} + w \frac{\partial}{\partial z} \right\} u - \frac{uv \tan \phi}{a} + \frac{uw}{a} = F_{Cor,x} + F_{Pressgrad,x} + F_{fric,x} + F_{other,x}$$

$$\frac{\partial v}{\partial t} + \left\{ \frac{u}{a \cos \phi} \frac{\partial}{\partial \lambda} + \frac{v}{a} \frac{\partial}{\partial \phi} + w \frac{\partial}{\partial z} \right\} v + \frac{u^2 \tan \phi}{a} + \frac{vw}{a} = F_{Cor,y} + F_{Pressgrad,y} + F_{fric,y} + F_{other,y}$$

$$\rho c_v \left[\frac{\partial T}{\partial t} + \left\{ \frac{u}{a \cos \phi} \frac{\partial}{\partial \lambda} + \frac{v}{a} \frac{\partial}{\partial \phi} + w \frac{\partial}{\partial z} \right\} T \right] = Work + Heat$$

Advection

Dependent Field Variables

u=zonal wind vel.

w=vertical wind vel.

v=meridional wind vel.

T=Temperature

Assume u, v, w, T are composed of 2 primary waves

$$f = f'_1 + f'_2 = A_1 \cos(s_1 \lambda - \sigma_1 t + \theta_1) + A_2 \cos(s_2 \lambda - \sigma_2 t + \theta_2)$$

Products of primary waves through nonlinear terms

Zonal momentum forcing

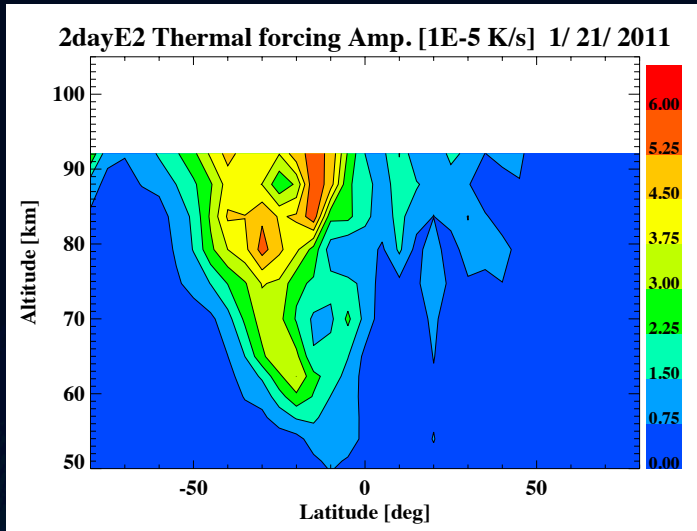
Meridional momentum forcing

Thermal forcing

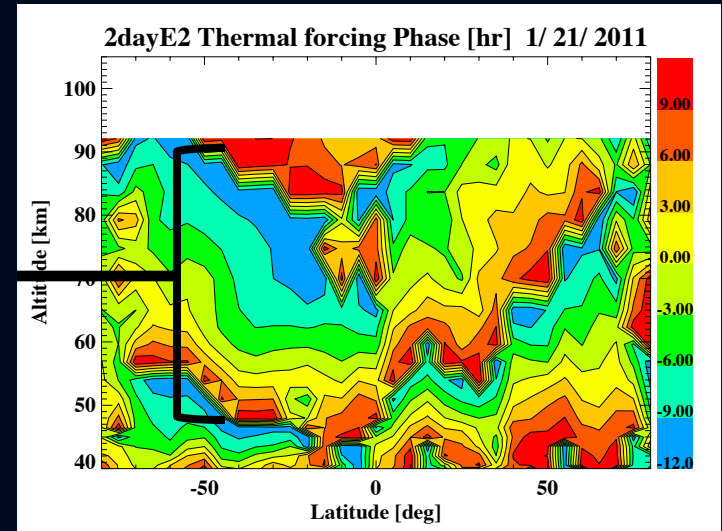


Thermal Forcing of Secondary Waves

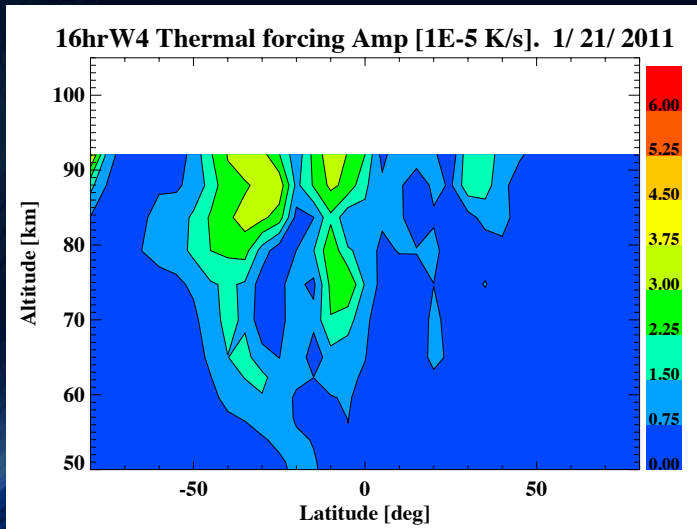
2-dayE2
Thermal
Forcing



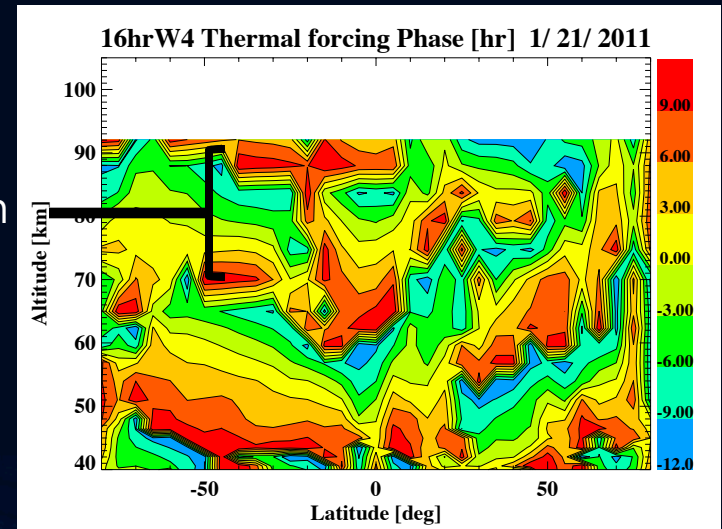
40km



16hrW4
Thermal
Forcing



20km





Conclusions/Future

Summary

- Investigates the forcing and manifestation of secondary waves arising from DW1-QTDW interaction from satellite observations

Future

- Global Scale Wave Model (GSWM) will be utilized to investigate the relationship between nonlinear forcing region and the secondary wave response
- Determine potential impact on the MLT and IT systems

Acknowledgements

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GSWM Secondary Wave Response

