

Ionospheric Specification and Forecast by Ensemble Assimilation of FORMOSAT-7/COSMIC-2 Slant Total Electron Contents to a Coupled Model of the Thermosphere, Ionosphere, and Plasmasphere

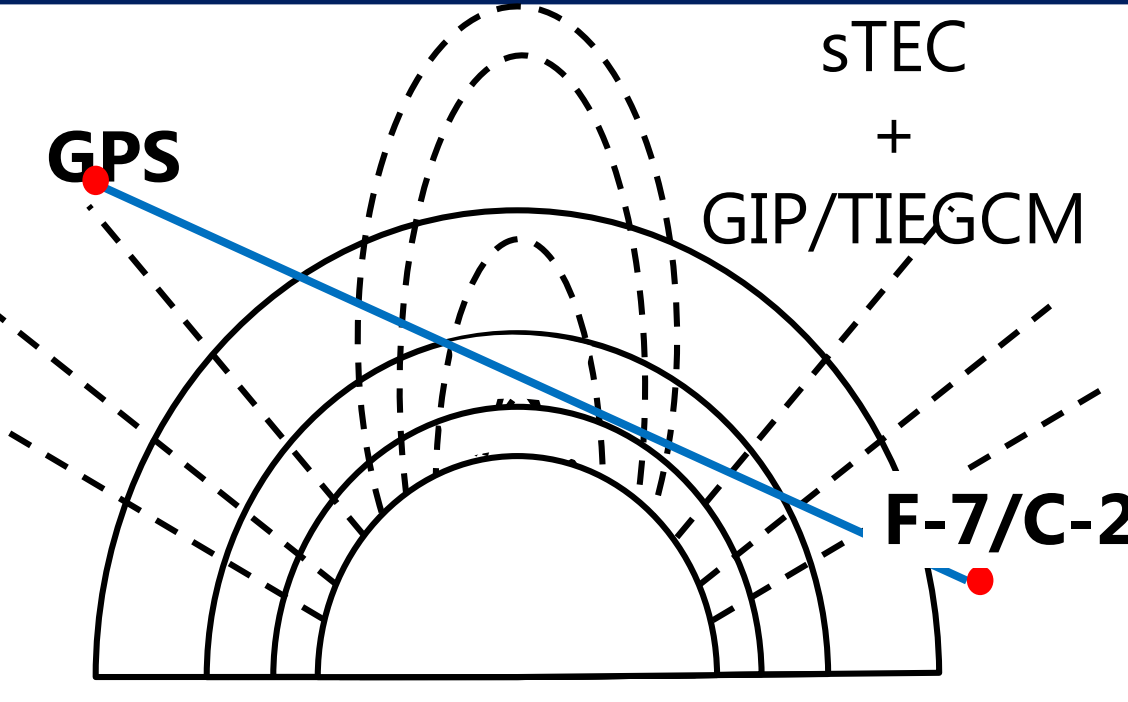
Chih-Ting Hsu^{1,2,3}, Tomoko Matsuo^{2,3}, Xinan Yue⁴, and Jann-Yeng Liu¹

¹Institute of Space Science, National Central University, Taoyuan, Taiwan; ²Cooperative Institute for Research in Environmental Sciences, University of Colorado at Boulder, CO, USA; ³Space Weather Prediction Center, National Oceanic and Atmospheric Administration, Boulder, CO, USA; ⁴Chinese Academy of Sciences, China



Introduction and Background

The Formosa Satellite 7/Constellation Observing System for Meteorology, Ionosphere and Climate 2 (F-7/C-2) radio occultation mission can provide high temporal- and spatial- resolution slant total electron content (sTEC) data globally, with six satellites at low inclination orbits and another six at high inclination orbits, planned to be launched in the future, respectively. It has a great potential to improve ionospheric data assimilation. In this study, synthetic F-7/C-2 sTEC data are assimilated into the Global-Ionosphere-Plasmasphere /Thermosphere-Ionosphere-Electrodynamics General Circulation Model (GIP/TIEGCM) [Pedatella et al., 2011] by using the Grid-point Statistical Interpolation Ensemble Kalman Filter (GSI EnKF) [Whitaker and Hamill, 2001]. Observing System Simulation Experiments (OSSEs) of F-7/C-2 sTEC data are carried out with different localization scale lengths to assess the impact of covariance localization on data assimilation analysis.



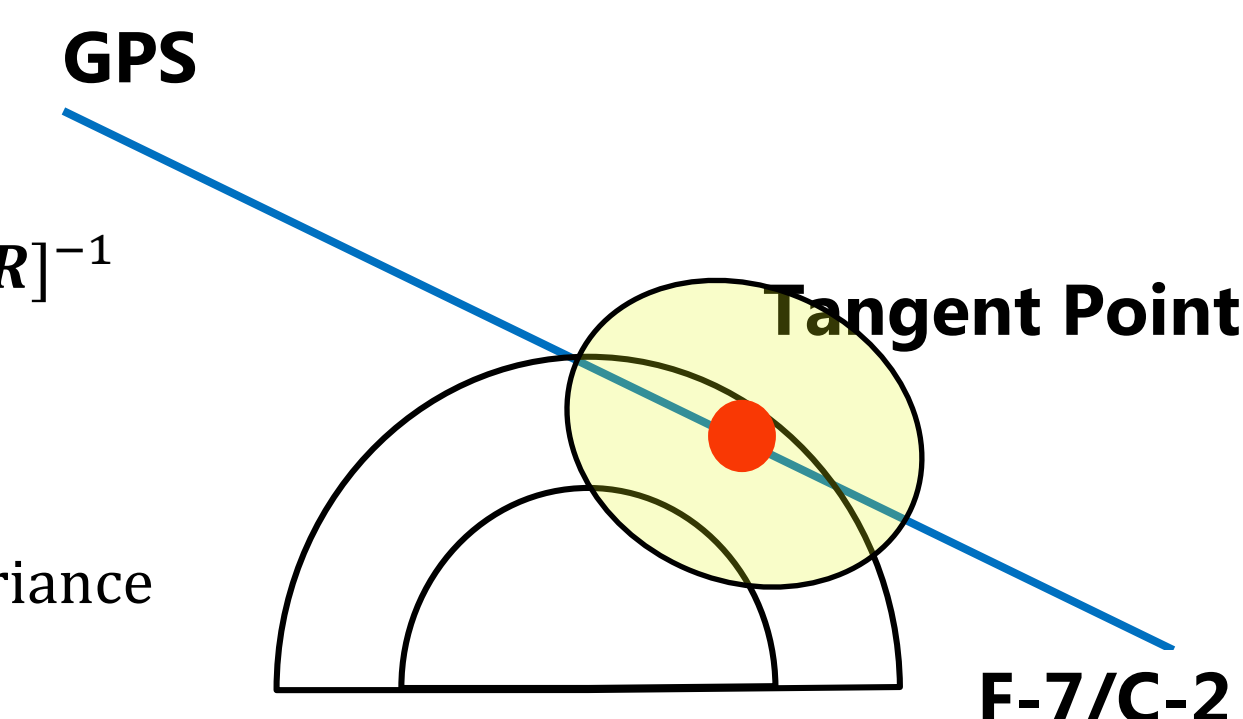
Experiment Setup

83-member GIP/TIEGCM ensemble simulations are initialized by perturbing the model drivers according to a normal distribution. These drivers are solar 10.7cm radio flux (F107), cross-tail potential drop (CP), and auroral hemispheric power (HP).

- Mean value of F107, CP, and HP: $90 \times 10^{-22} \frac{WHz}{m^2}$, 45 kV, and 16 GW respectively.
- Standard deviation of F107, CP, and HP: $5 \times 10^{-22} \frac{WHz}{m^2}$, 10 kV, and 2 GW respectively.
- Synthetic F-7/C-2 sTEC data are sampled from the "truth" simulation with following drivers.
- F107, CP, and HP: $120 \times 10^{-22} \frac{WHz}{m^2}$, 55 kV, and 16 GW respectively.

Parametric Covariance Localization

The ensemble-based covariance needs to be localized around observation locations to minimize the effects of spurious correlations due to sampling errors. The ensemble-based covariance is multiplied by localization matrix element by element.



$$K = [\rho \circ P^f][H(\rho \circ P^f)H^T + R]^{-1}$$

K : Kalman gain
 ρ : localization matrix
 H : forward operator
 P^f : ensemble-based forecast error covariance
 R : observation error covariance

Note that the ensemble-based covariance is here localized around the tangent point even though sTEC is a non-local observation.

Horizontal Localization Function

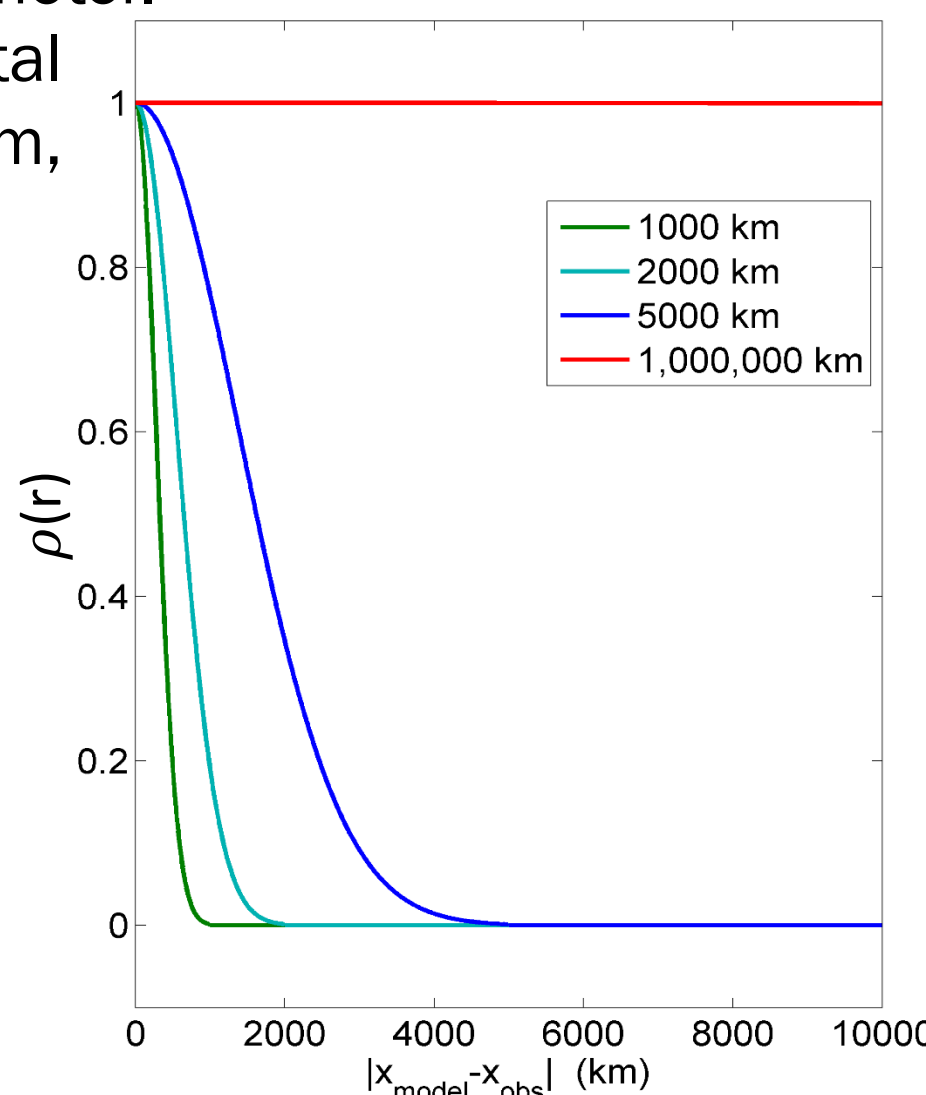
The Gaspari-Cohn [1999] function is used for both horizontal and vertical localization. Horizontal localization parameter L_h is defined in kilometer. In the following experiments, 4 different horizontal localization parameters (1,000,000km, 5,000km, 2,000km, and 1,000km) are applied.

$$r = \frac{|x_{model} - x_{obs}|}{L_h}$$

$$\text{For } r \leq 1 \quad \rho(r) = e^{-\left(\frac{r}{0.388}\right)^2}$$

$$\text{For } r > 1 \quad \rho(r) = 0$$

L_h : horizontal localization parameter
 x_{obs} : location of tangent point
 x_{model} : location of model grid



Vertical Localization Function

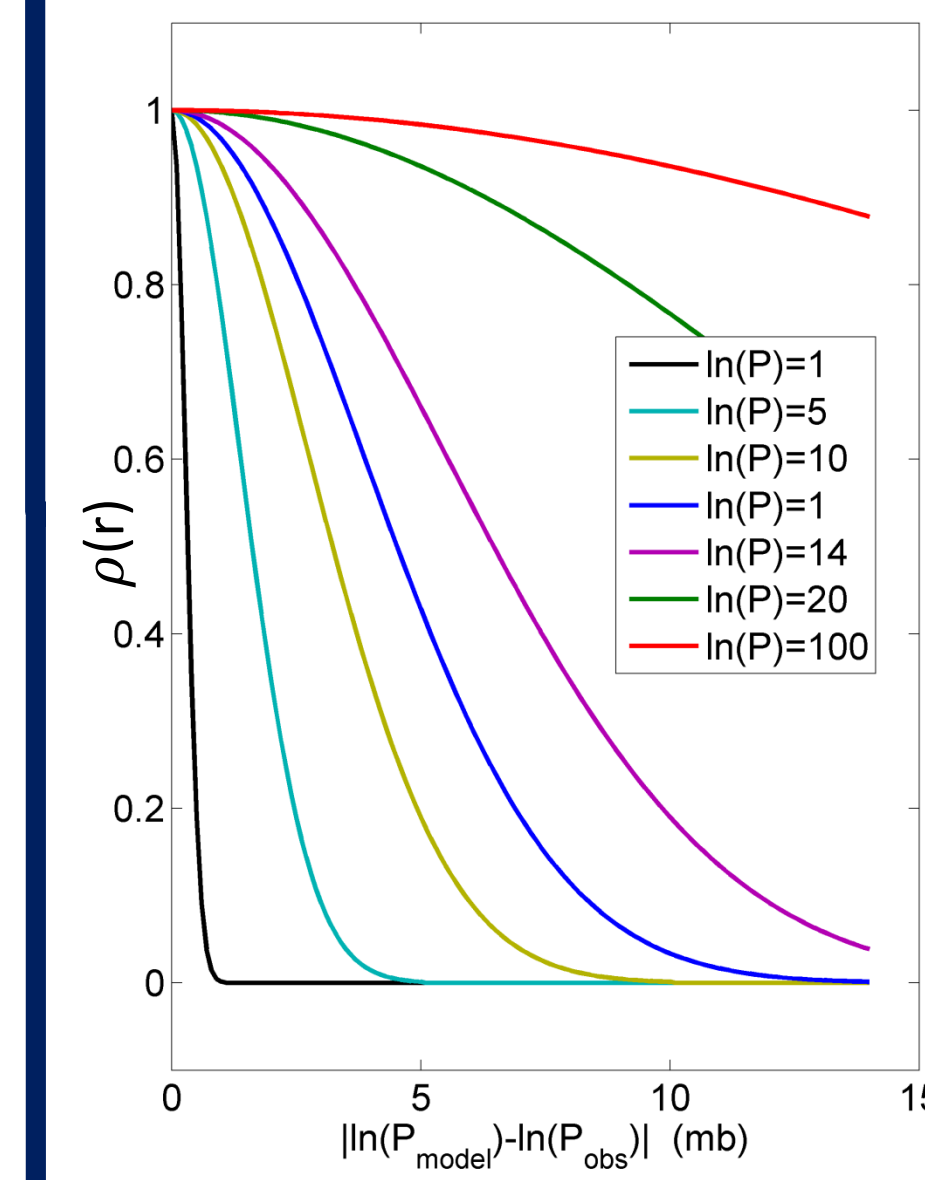
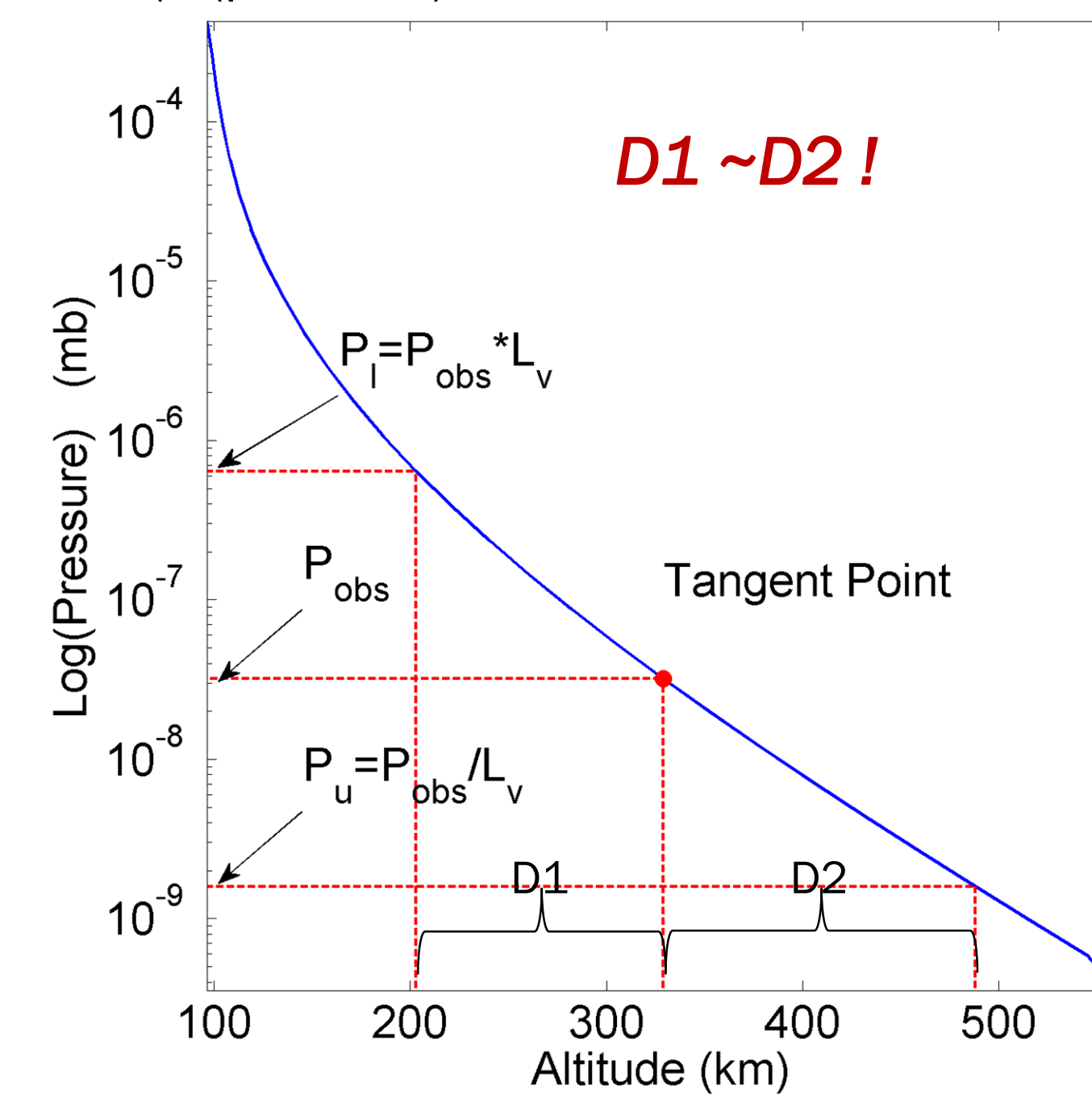
Vertical localization parameter L_v is defined in nature log of pressure. In the following experiments, 7 vertical localization parameters (ln(pressure) = 1, 5, 10, 14, 20, 50, and 100) are applied.

$$r = \frac{|\ln(P_{model}) - \ln(P_{obs})|}{L_v}$$

$$\text{For } r \leq 1 \quad \rho(r) = e^{-\left(\frac{r}{0.388}\right)^2}$$

$$\text{For } r > 1 \quad \rho(r) = 0$$

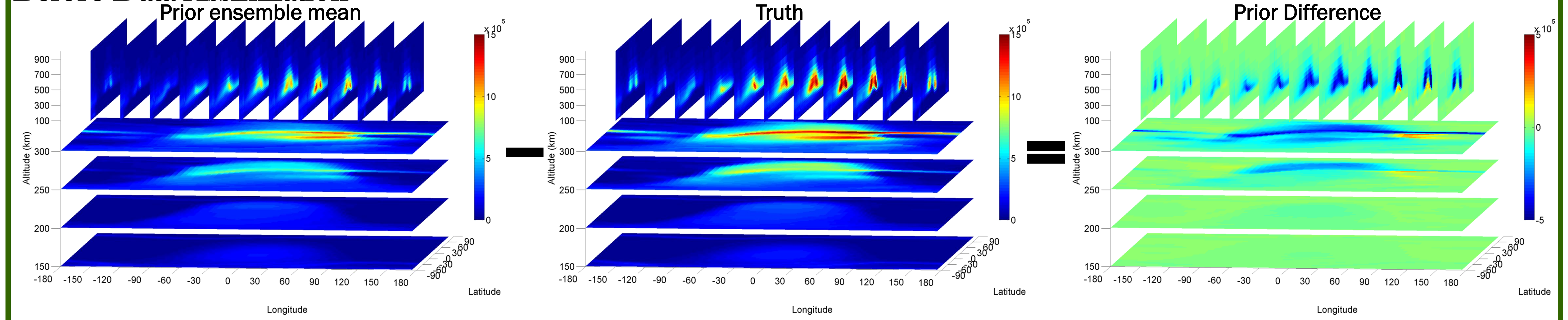
L_v : vertical localization parameter
 P_{obs} : pressure at tangent point
 P_{model} : pressure at model grid



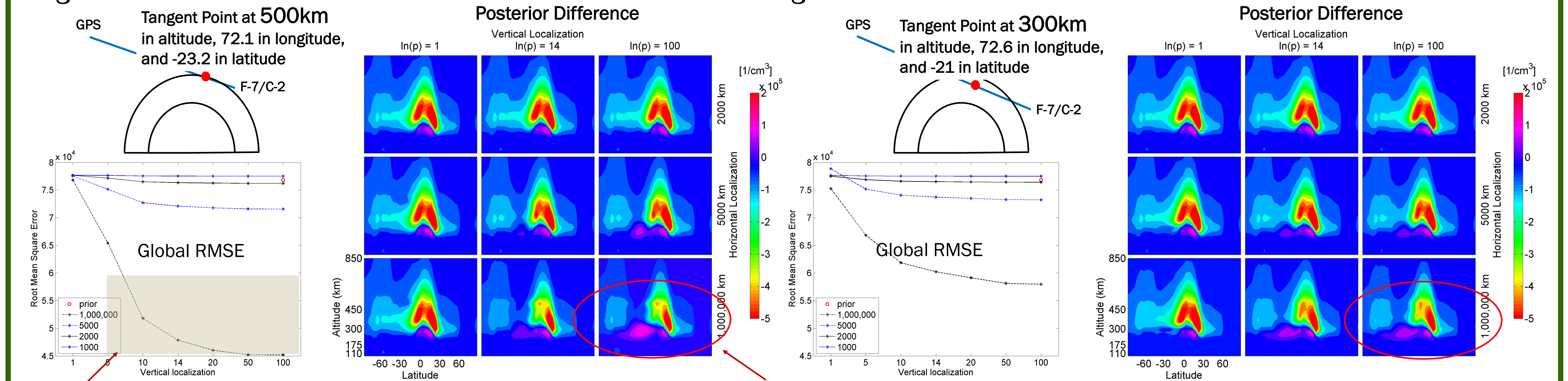
References

- Gaspari, G., and S. E. Cohn, (1999) Construction of correlation functions in two and three dimensions. *Quart. J. Roy. Meteor. Soc.*, **125**, 723-757
- Hsu, C.-T., T. Matsuo, W. Wang, and J.-Y. Liu (2024). Effects of inferring unobserved thermospheric and ionospheric state variables by using an Ensemble Kalman Filter on global ionospheric specification and forecasting. *J. Geophys. Res.*, **129**, e202300257.
- Lei, L., J. L. Anderson, and G. S. Romine (2015). Empirical Localization Functions for ensemble Kalman filter Data Assimilation in regions with and without Precipitation. *Mon. Wea. Rev.*, **143**, 3664-3679
- Pedatella, N. M., J. M. Forbes, A. Mautz, A. D. Richmond, T.-W. Fang, K. M. Larson, and G. Millward (2011). Longitudinal variations in the F-region ionosphere and the topside ionosphere-plasmasphere: Observations and model simulations. *J. Geophys. Res.*, **116**, A12309.
- Whitaker, J. S., and T. M. Hamill (2001). Ensemble Data Assimilation without Perturbed Observations. *Mon. Wea. Rev.*, **130**, 1913-1924.

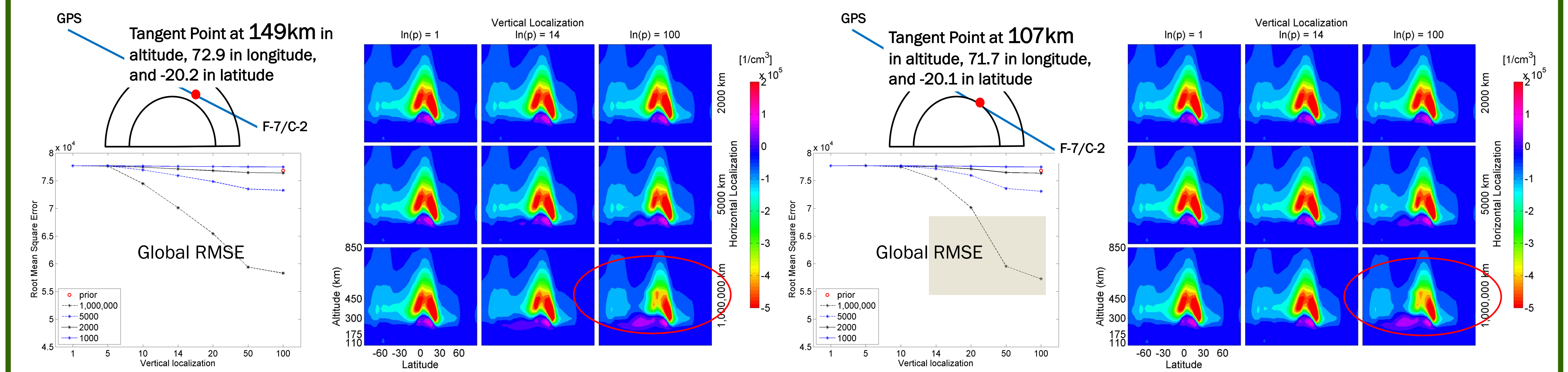
Before Data Assimilation



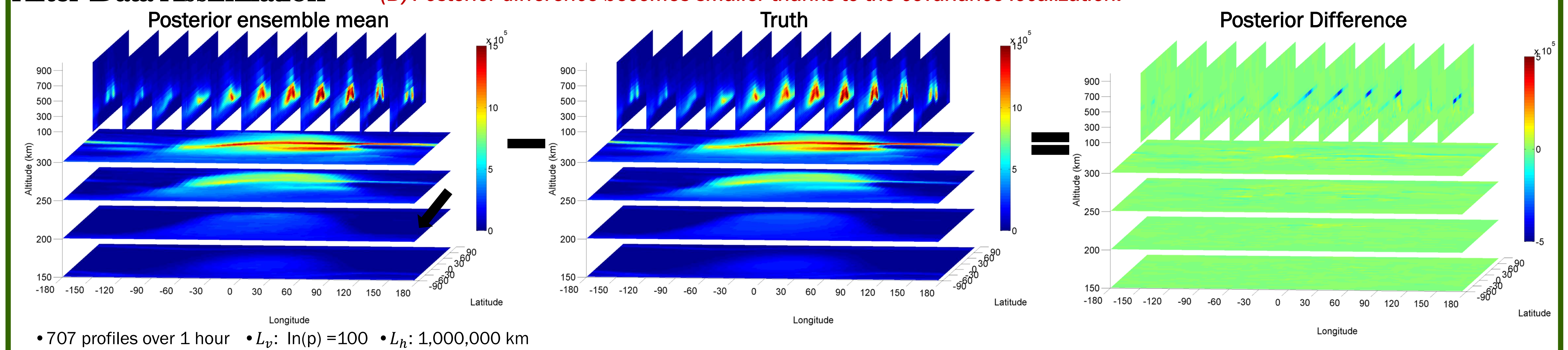
Single Observation OSSEs with Different Localization Length Scales



- (A) The larger the localization length scales are, the smaller global RMSE!
 (B) E-/F-region error becomes larger/smaller!
 (C) Effective localization length scales depend on tangent point's heights!



After Data Assimilation (D) Posterior difference becomes smaller thanks to the covariance localization!



Summary

- ◆ 112 OSSEs for the F-7/C-2 observing system are conducted to assess the impact of covariance localizations on data assimilation analysis.
- **Conclusion A:** Large horizontal and vertical localization length scales yield the smallest error globally.
- **Conclusion B:** Large horizontal and vertical localization cases lead to large/small errors in the E-region/F-region.
- **Conclusion C:** For lower altitude tangent point sTEC observations, it is better to use larger vertical localization length scales (in terms of ln(pressure)).
- ◆ 707 F-7 profiles (~700,000 sTEC data) are assimilated with $L_v = 100$ and $L_h = 1,000,000$ km.
- **Conclusion D:** The covariance localization helped reduce the electron density analysis errors.

Future Work

- ◆ Apply an altitude-dependent horizontal and vertical localization by estimating the empirical localization function [Lei et al., 2015].
- ◆ Conduct assimilation-forecast cycling experiments to examine the impact of estimating both thermospheric and ionospheric states on ionospheric forecasting [Hsu et al., 2014]