



Analyzing Dynamical Interactions in the IT System via LCS Technique



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Motivation:

- ◆ Previous work showed that LCSs are found in the ionosphere-thermosphere (IT) flows [1,2] and respond to geomagnetic activity.
- ◆ Ionosphere and thermosphere are coupled through energy and momentum interaction.
- ◆ Preliminary study showed that the comparison of thermospheric LCSs and ionospheric LCSs according to empirical models can show the evidence of energy interaction in the IT system [3].
- ◆ Objective: analyze the energy interaction in IT system by comparing the shape of thermosphere LCSs and ionospheric LCSs.

Introduction:

◆ Lagrangian Coherent Structures (LCSs)

- Describe regions of maximal separation (or convergence) [4], and are independent of the observer [5].
- Can act as material barriers to bound the transport.
- Are used to understand thermospheric and ionospheric material transport [1,2].

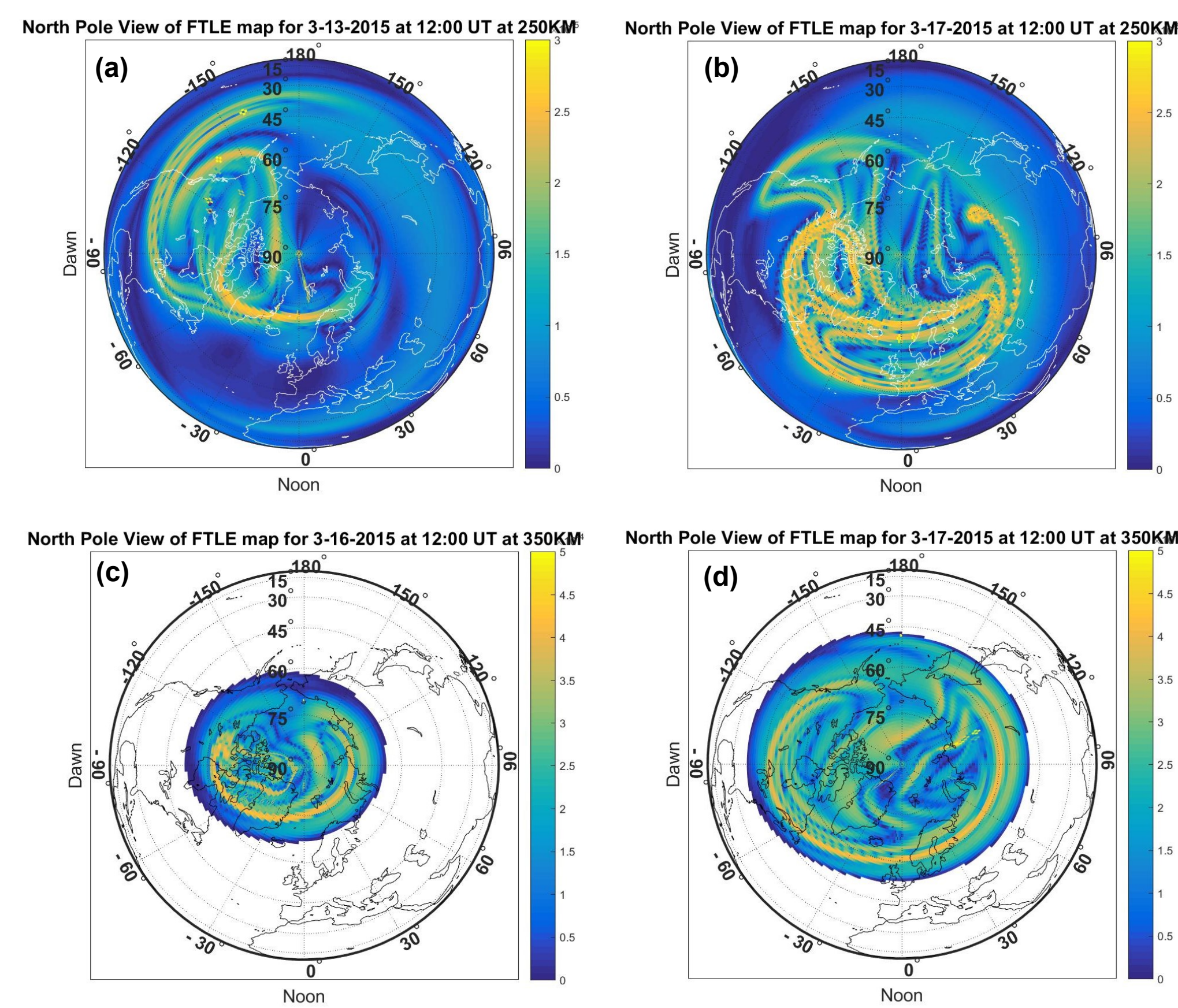


Fig. 1 (a) North pole view of FTLE map for neutral winds velocity field at 250 km during geomagnetic quiet period with $t_0 = 12:00$ UT on 13 March 2015 with integration time of 2 days. (b) during geomagnetic active period with $t_0 = 12:00$ UT on 17 March 2015. (c) North pole view of FTLE map for plasma drifts at 350 km during geomagnetic quiet period with $t_0 = 12:00$ UT on 16 March 2015 with integration time of 3 hours. (d) during geomagnetic active period with $t_0 = 12:00$ UT on 17 March 2015.

⇒ Are defined by the locally maximum finite time Lyapunov exponent.

◆ Finite Time Lyapunov Exponent (FTLE)

- A scalar field measuring the degree of stretching of a fluid particle at a certain point, after a given interval of time τ .

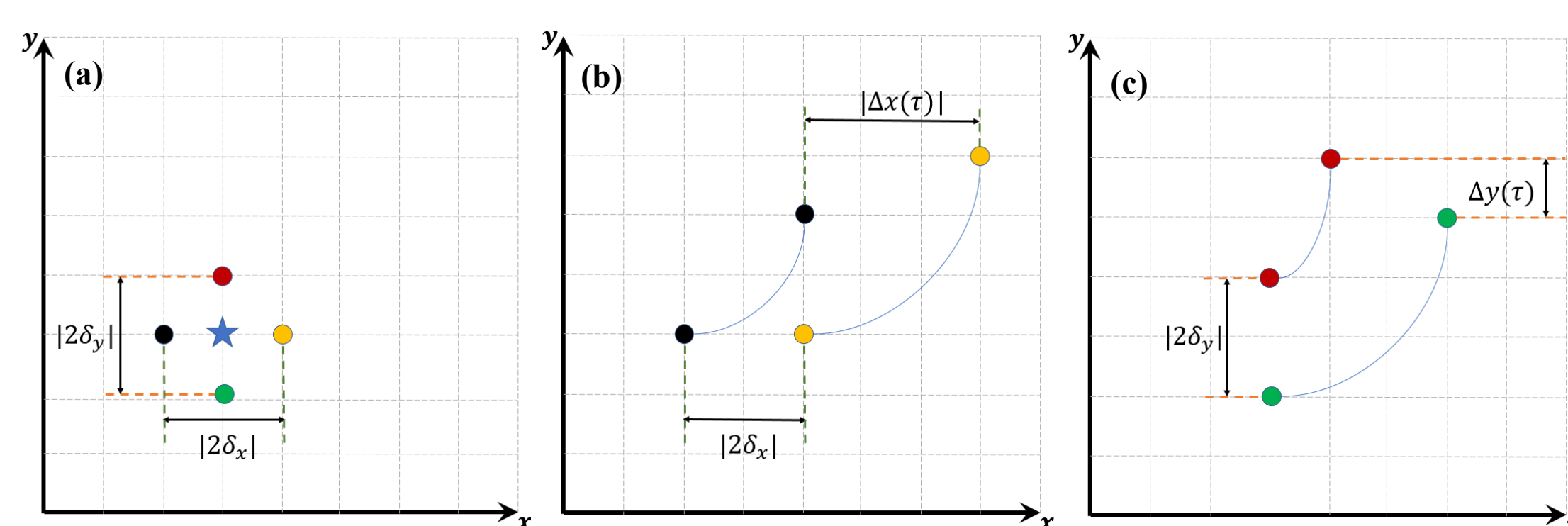


Fig.2 Method for computing FTLE for a grid point in a 2D domain.

$$J = \begin{bmatrix} \frac{\Delta x(\tau)}{2\delta_x} & \frac{\Delta x(\tau)}{2\delta_y} \\ \frac{\Delta y(\tau)}{2\delta_x} & \frac{\Delta y(\tau)}{2\delta_y} \end{bmatrix} \quad \sigma(J) = \frac{1}{|\tau|} \log \left(\sqrt{\lambda_{max}(J^T J)} \right)$$

Method:

◆ Ionosphere-Thermosphere Algorithm for Lagrangian Coherent Structures (ITALCS).

- Given time varying flow fields, ITALCS computes FTLE and tracer positions, more details in [2].
- We will test IT-flows modeled by Thermosphere Ionosphere Electroynamics General Circulation Model (TIEGCM).

◆ Thermosphere Ionosphere Electroynamics General Circulation Model (TIEGCM):

- A three-dimensional (3D) global physical model.
- Self-consistently solves dynamic equations in IT system.
- Applies fourth order finite differencing method.
- Models neutral wind fields and plasma drifts.

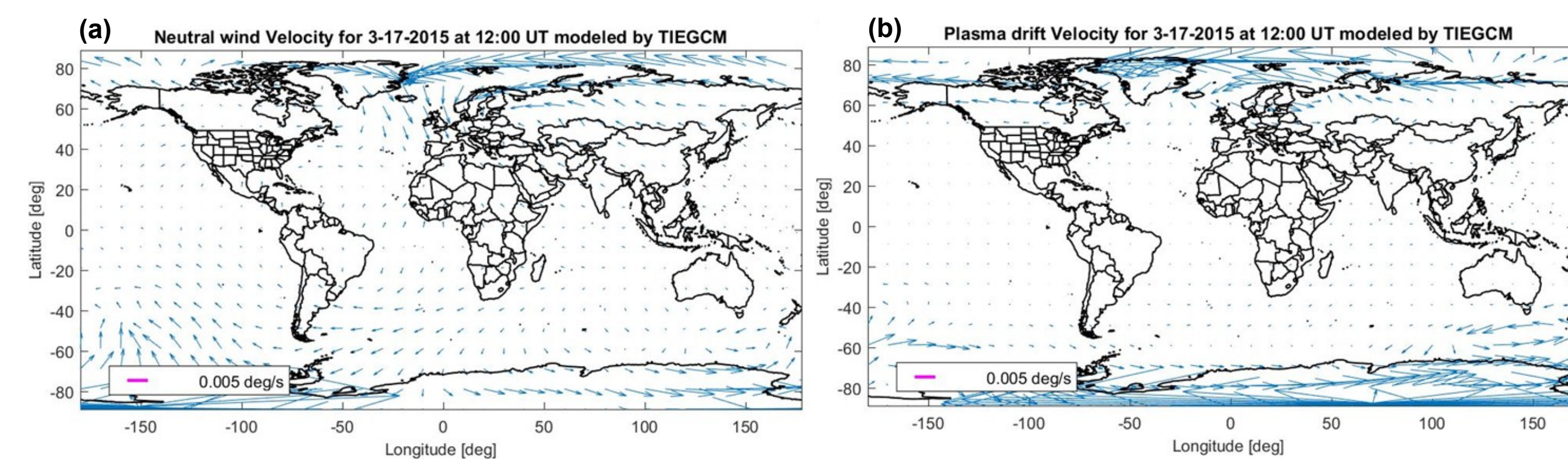


Fig.3 Velocity fields modeled by TIEGCM at 12:00 UT 17 March 2015, (a) neutral winds, and (b) plasma drifts.

- ◆ Charged-neutral collision frequency is a function of energy [6].
- ◆ Geomagnetic activity influences the energy input of IT system.
- ◆ LCSs of modeled IT flows are compared during geomagnetic quiet period and active period.

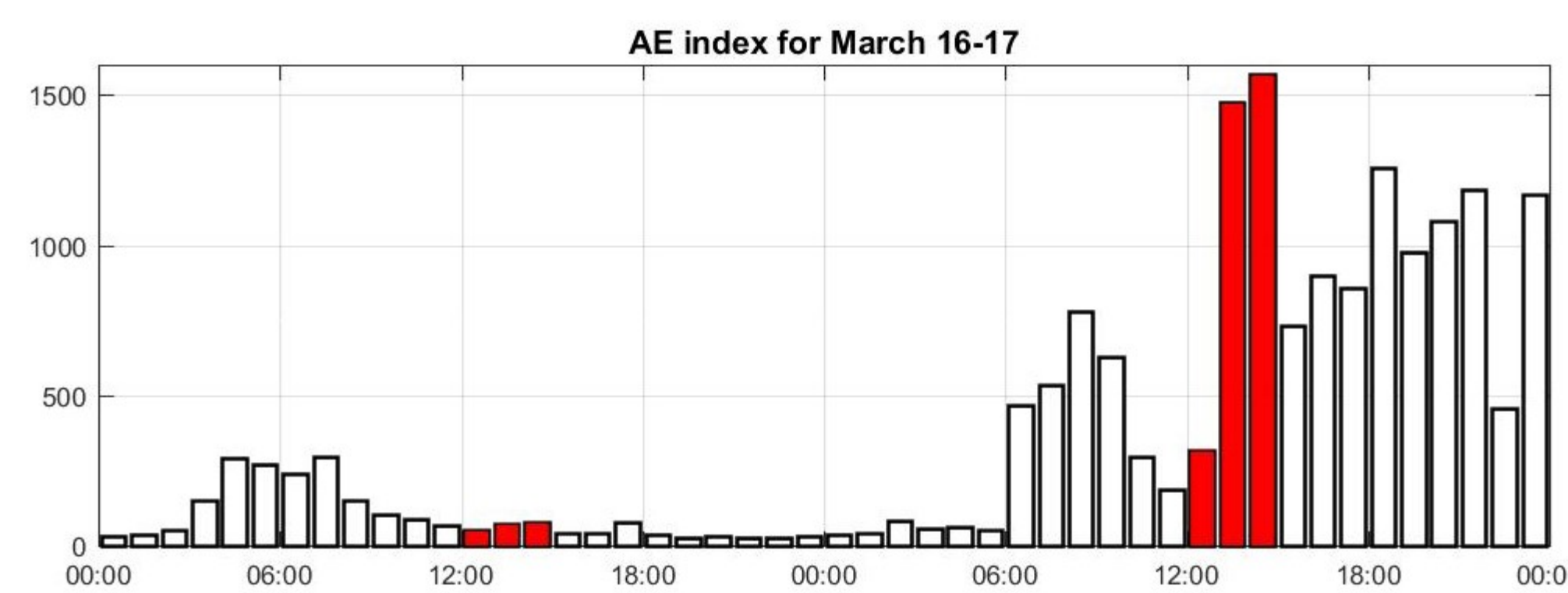


Fig.4 AE index from 16–17 March 2015. The periods labeled in red are used to study the effect of geomagnetic activity.

◆ Parameters:

Integration time: $\tau = 3$ hours.
Altitude: 350km.
Grid space: 2.5 degree.

Geomagnetic quiet period:
 $t_0 = 12:00$ UT 16 March 2015.
Geomagnetic active period:
 $t_0 = 12:00$ UT 17 March 2015.

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References :

- [1] Wang, N., U. Ramirez, F. Flores, and S. Datta-Barua (2017), Lagrangian coherent structures in the thermosphere: Predictive transport barriers, *Geophys. Res. Lett.*, **44**, doi:10.1002/2017GL072568.
- [2] Wang, N., S. Datta-Barua, A. T. Chartier, U. Ramirez, and C. N. Mitchell (2018), Horseshoes in the high-latitude ionosphere, *JGR Space Physics*, doi: https://doi.org/10.1029/2017JA025077.
- [3] Wang, N., U. Ramirez, and S. Datta-Barua, "Dynamic Interactions in the IT System via Lagrangian Coherent Structures Analysis", poster session presented at American Geophysical Union (AGU) Fall Meeting, New Orleans, LA, Dec. 2017.
- [4] Haller, G. (2015), Lagrangian coherent structures, *Annual Review of Fluid Mechanics*, **47**, 137–162, doi:10.1146/annurev-fluid-010313-141322.
- [5] Haller, G. (2005), An objective definition of a vortex, *Journal of Fluid Mechanics*, **525**, 1–26, doi:10.1017/S0022112004002526.
- [6] Datta-Barua, S., G. S. Bust, G. Crowley, and N. Curtis (2009), Neutral wind estimation from 4-D ionospheric electron density images, *J. Geophys. Res.*, **114**, A06317, doi:10.1029/2008JA014004.

Results:

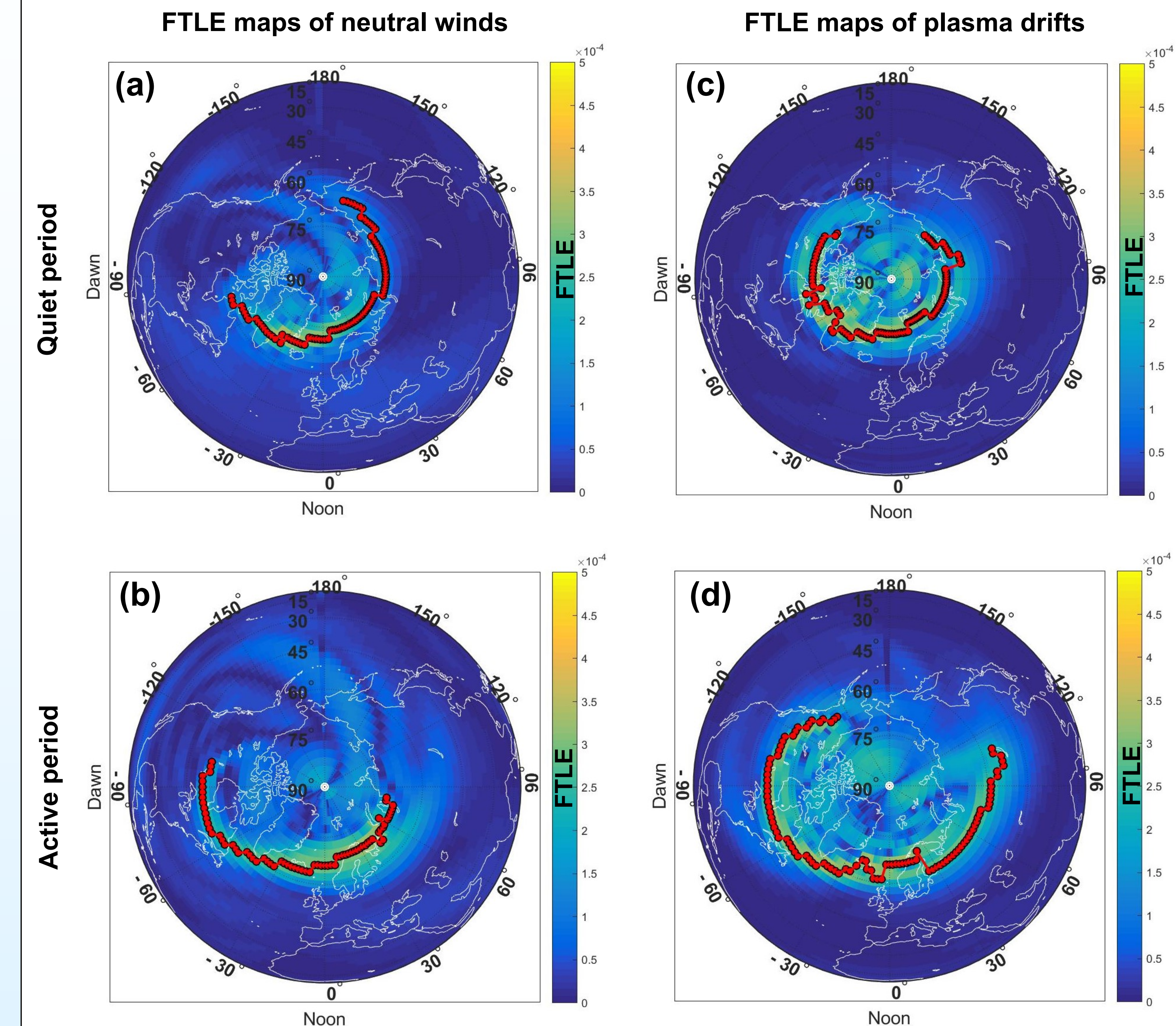


Fig.5 FTLE map for neutral wind field viewed from geographic north pole at 350 km during (a) geomagnetic quiet period with $t_0 = 12:00$ UT, 16 March 2015, and (b) during geomagnetic active period with $t_0 = 12:00$ UT, 17 March 2015, at 350km. FTLE map for plasma drift viewed from geographic north pole at 350 km during (c) geomagnetic quiet period with $t_0 = 12:00$ UT, 16 March 2015, at 350km, and (d) during geomagnetic active period with $t_0 = 12:00$ UT, 17 March 2015, at 350km. The red dots indicate the locally maximum FTLEs.

Table 1 Comparison of rotation angle between thermospheric LCS and ionospheric LCS during geomagnetic quiet period and storm period

	T-LCSs West boundary	T-LCSs East boundary	T-LCSs Middle point	I-LCSs West boundary	I-LCSs East boundary	I-LCSs Middle point	α_{I-T}
Quiet period	77.5 W	165 E	43.75 E	130 W	142.5 E	6.25 E	-37.5
Storm period	102.5 W	80 E	11.25 W	142.5 W	110 E	16.25 W	-5

Summary

- Both modeled thermospheric LCSs (T-LCSs) and ionospheric LCSs (I-LCSs) are horseshoe-like with the "U"-shaped LCSs opening to the night side, and respond to the geomagnetic activity.
- The T-LCSs and I-LCSs are more aligned during the geomagnetically stormy period.
- During the geomagnetic active period, the collision frequency between neutral particles and charged particles is increased. The alignment of T-LCSs and I-LCSs during active period shows the evidence of dynamical interactions in the IT system.

Future work:

- Compare the FTLE maps with the temperature maps during both geomagnetic quiet period and storm period.
- Analyze backward LCSs in the IT flows to explore the energy input during geomagnetic active period.