

Impact of FORMOSAT-7/COSMIC-2 GNSS RO observations on midlatitude and low-latitude ionosphere specification

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Boulder



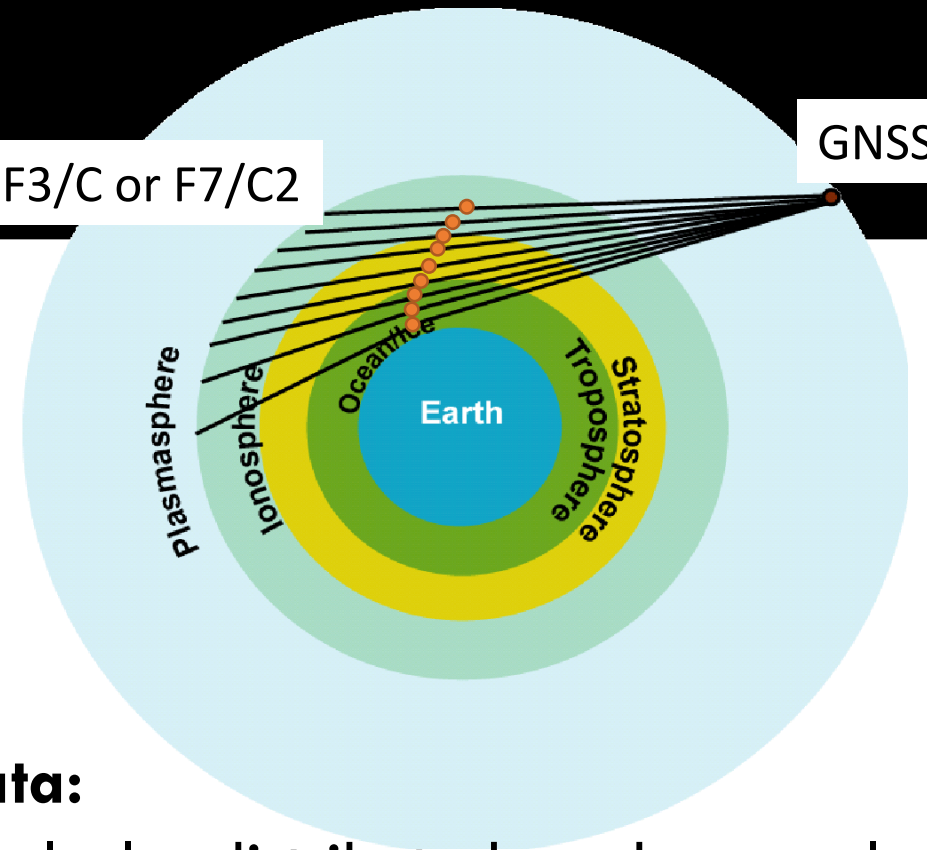
Data Assimilation of RO sTEC

$$s\text{TEC} = \int n_e dl = -\frac{f^2}{40.3 \times 10^6} \int (n - 1) dl = -\frac{f^2 S}{40.3}$$

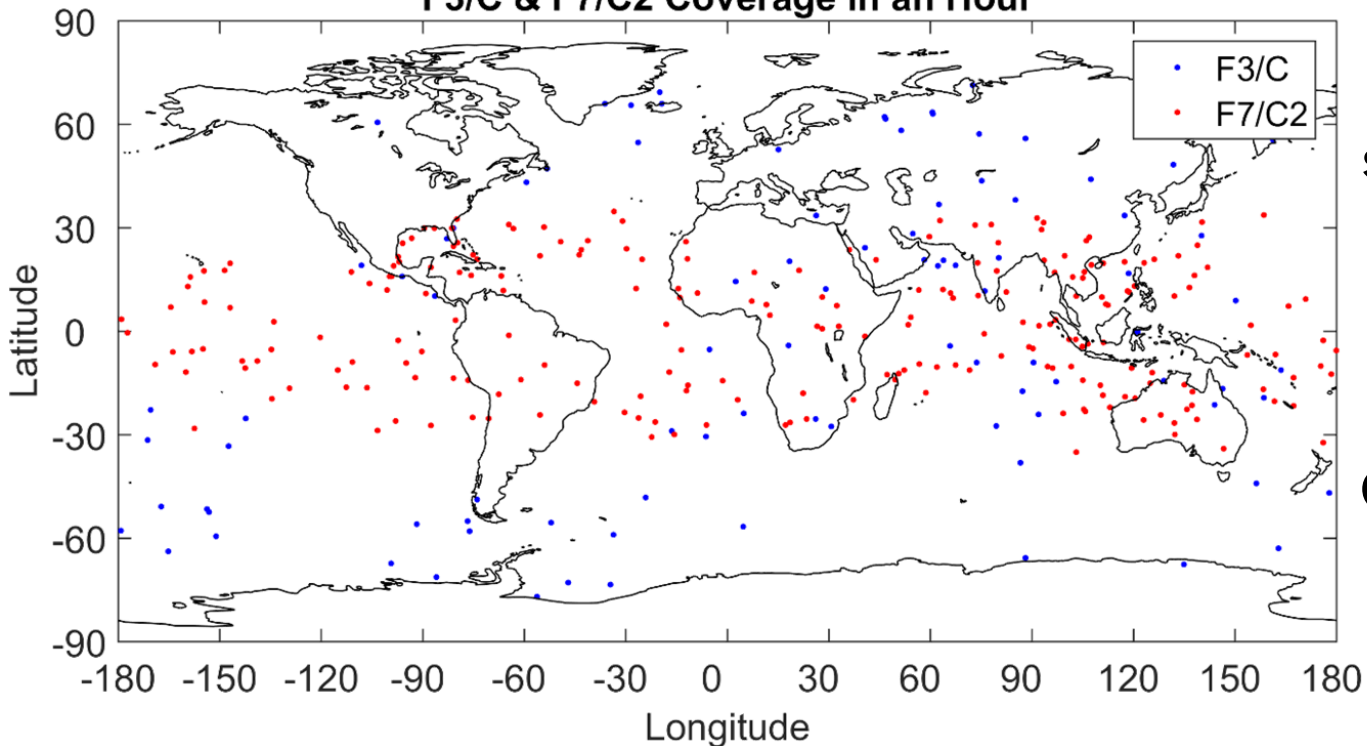
$$s\text{TEC} = \frac{(S_1 - S_2) f_1^2 f_2^2}{40.3(f_1^2 - f_2^2)}$$

F3/C or F7/C2

GNSS



F3/C & F7/C2 Coverage in an Hour



(Lin 2018, personal communication, 23 March)

sTEC data:

Irregularly distributed and sparsely sampled in space and time. Large day-to-day variability.

GIP/TIE-GCM model:

Global and complete in space and time. Small day-to-day variability.

NOAA GSI Ensemble Square Root Filter

Deterministic update by **Ensemble Square Root Filter** (EnSRF, Whitaker & Hamill, 2002) explained using Bayes' rule

$$\bar{\mathbf{X}}^a = \bar{\mathbf{X}}^b + \mathbf{K}(\mathbf{y}^o - \mathbf{H}(\bar{\mathbf{X}}^b))$$

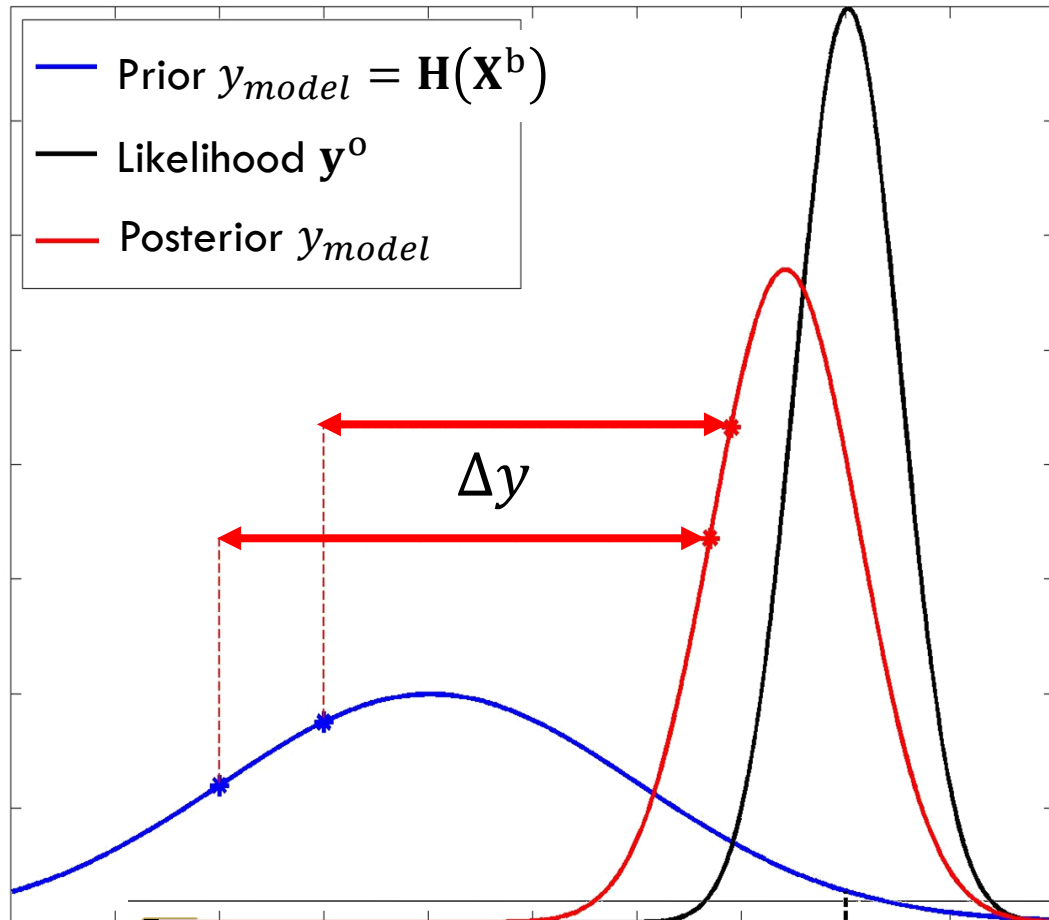
$$\mathbf{X}_n^a - \bar{\mathbf{X}}^a = (\mathbf{X}_n^b - \bar{\mathbf{X}}^b) + \tilde{\mathbf{K}}(-\mathbf{H}(\mathbf{X}_n^b - \bar{\mathbf{X}}^b))$$

$$\mathbf{K} = [\rho^b \circ (\mathbf{P}^b \mathbf{H}^T)] [\rho^b \circ (\mathbf{H} \mathbf{P}^b \mathbf{H}^T + \mathbf{R})]^{-1}$$

$$\tilde{\mathbf{K}}_k = (1 \pm (R / (\mathbf{H} \mathbf{P}^b \mathbf{H}^T + \mathbf{R})))^{-1} \mathbf{K}$$

$$\mathbf{P}^b \mathbf{H}^T \sim \frac{1}{N-1} \sum_{n=1}^N (\mathbf{X}_n^b - \bar{\mathbf{X}}^b) [\mathbf{H}(\mathbf{X}_n^b - \bar{\mathbf{X}}^b)]^T$$

$$\mathbf{H} \mathbf{P}^b \mathbf{H}^T \sim \frac{1}{N-1} \sum_{n=1}^N [\mathbf{H}(\mathbf{X}_n^b - \bar{\mathbf{X}}^b)] [\mathbf{H}(\mathbf{X}_n^b - \bar{\mathbf{X}}^b)]^T$$



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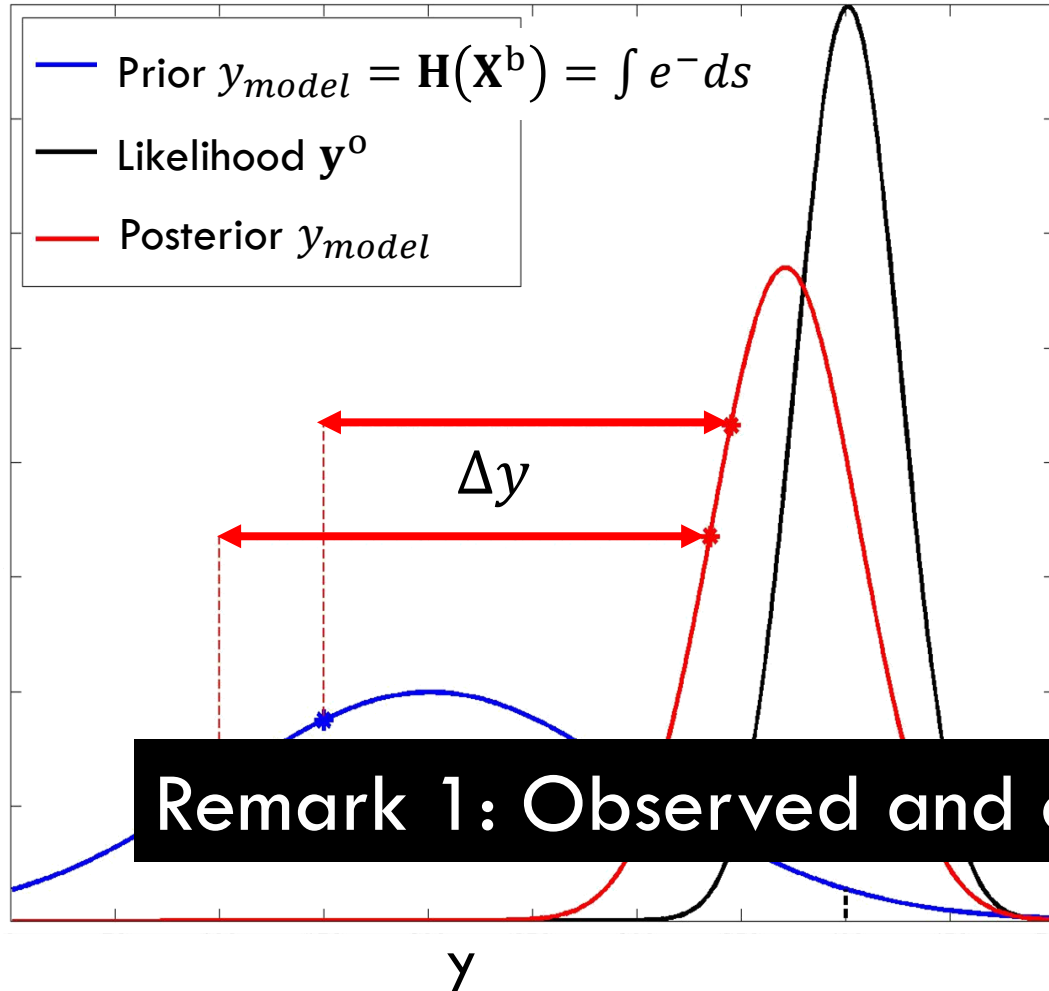
$$\mathbf{X}_n^a - \bar{\mathbf{X}}^a = \underbrace{(\mathbf{X}_n^b - \bar{\mathbf{X}}^b)}_{\text{sTEC}} + \underbrace{\mathbf{H}(\mathbf{X}_n^b - \bar{\mathbf{X}}^b)}_{O^+, e^-, \text{etc.}}$$

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Remark 1: Observed and estimated variables are different.

NOAA GSI Ensemble Square Root Filter

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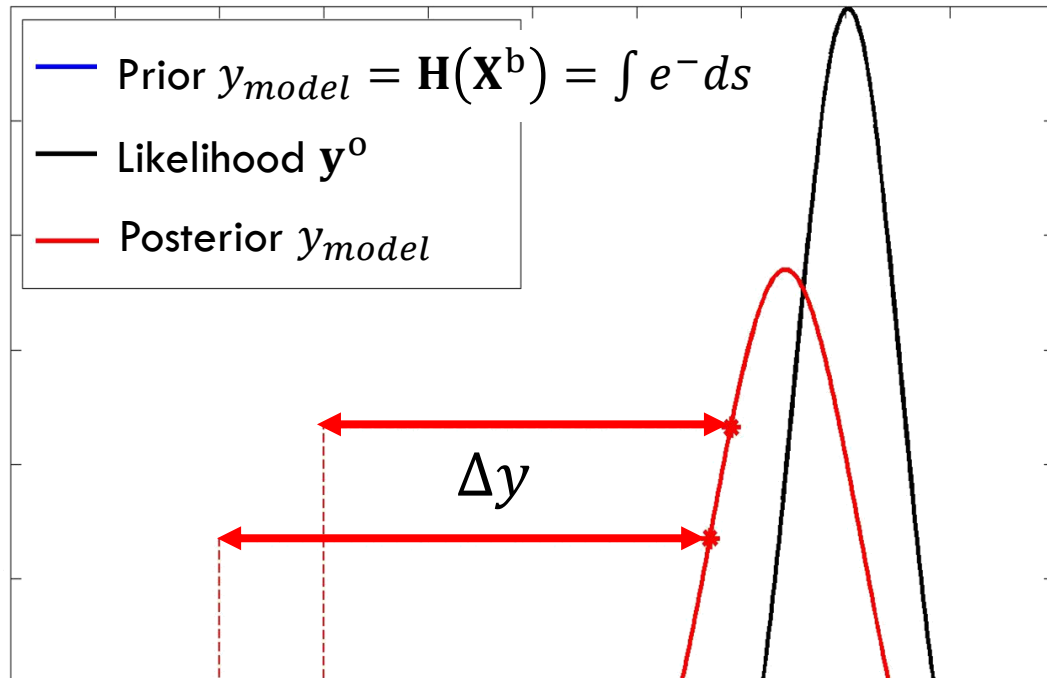
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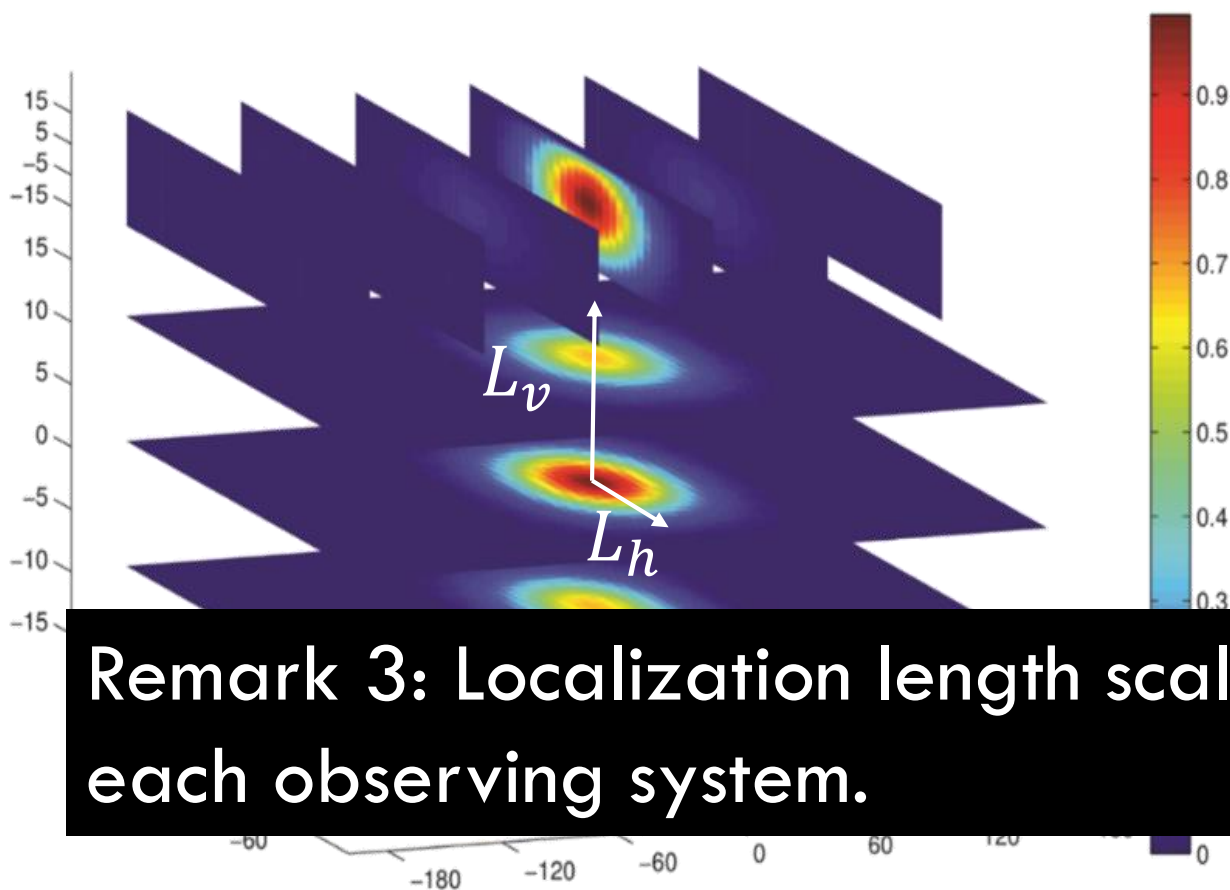
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Remark 2: Key to successful implementation of EnSRF is **covariance inflation/localization** to correct for issues resulting from sampling errors.

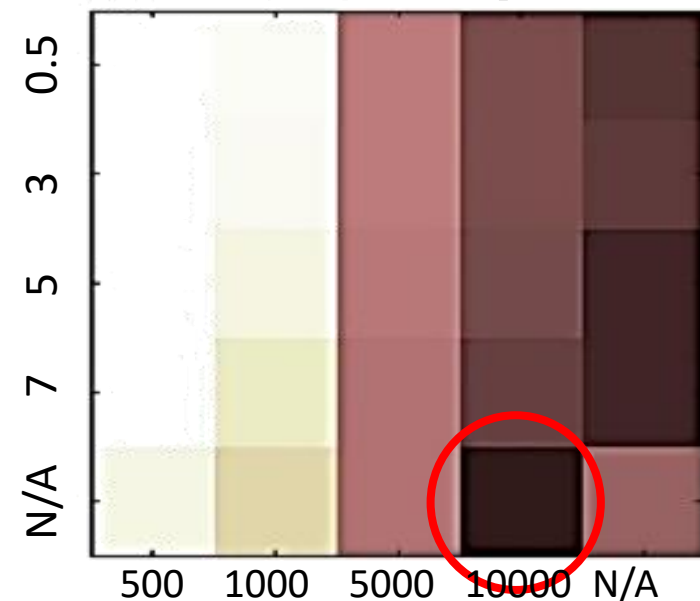
NOAA GSI EnSRF – Covariance Localization

25 experiments with ensemble size 70 (1750 model runs) and different covariance localization length scale for each observing system.

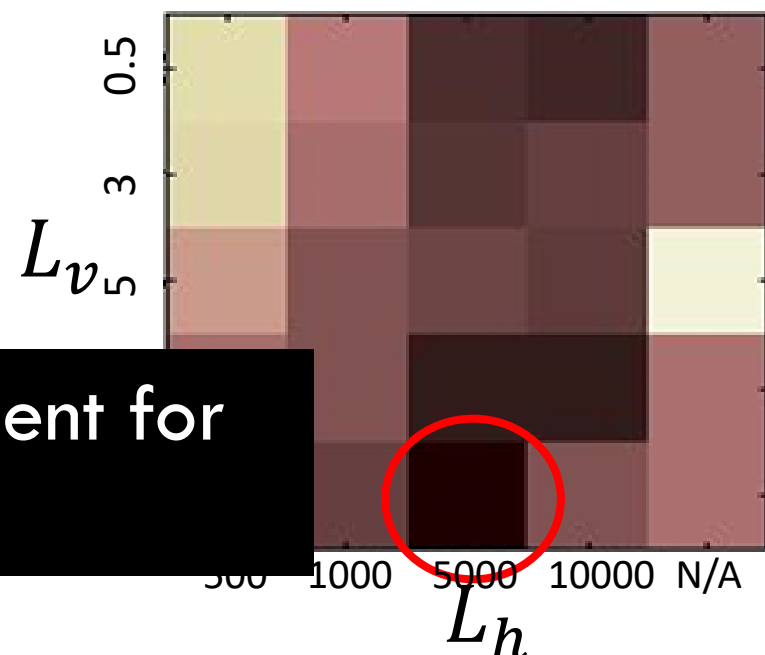


Remark 3: Localization length scales are different for each observing system.

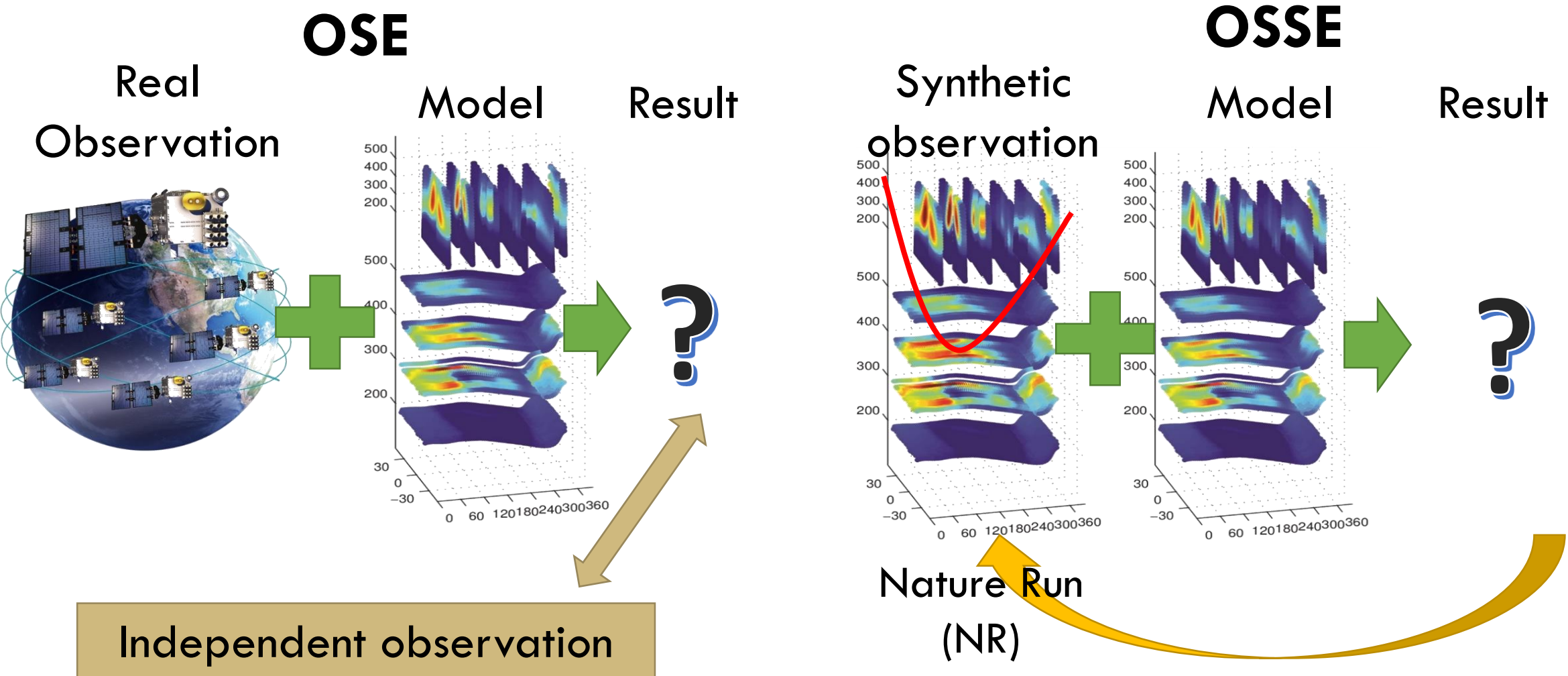
Error of F-3/C Experiment



Error of F-7/C-2 Experiment



Observing System (Simulation) Experiment



Observing System (Simulation) Experiment

OSE

OSSE

Real
Observation

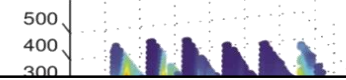
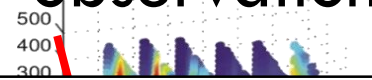
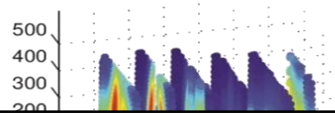
Model

Result

Synthetic
observation

Model

Result



A. Assess the impact of the F-3/C with OSE.

B. Compare the impact of the F-7/C-2 & F-3/C with OSSEs.

➔ Understand the impact of the F-7/C-2 on ionospheric specification.

Independent observation

Nature Run
(NR)

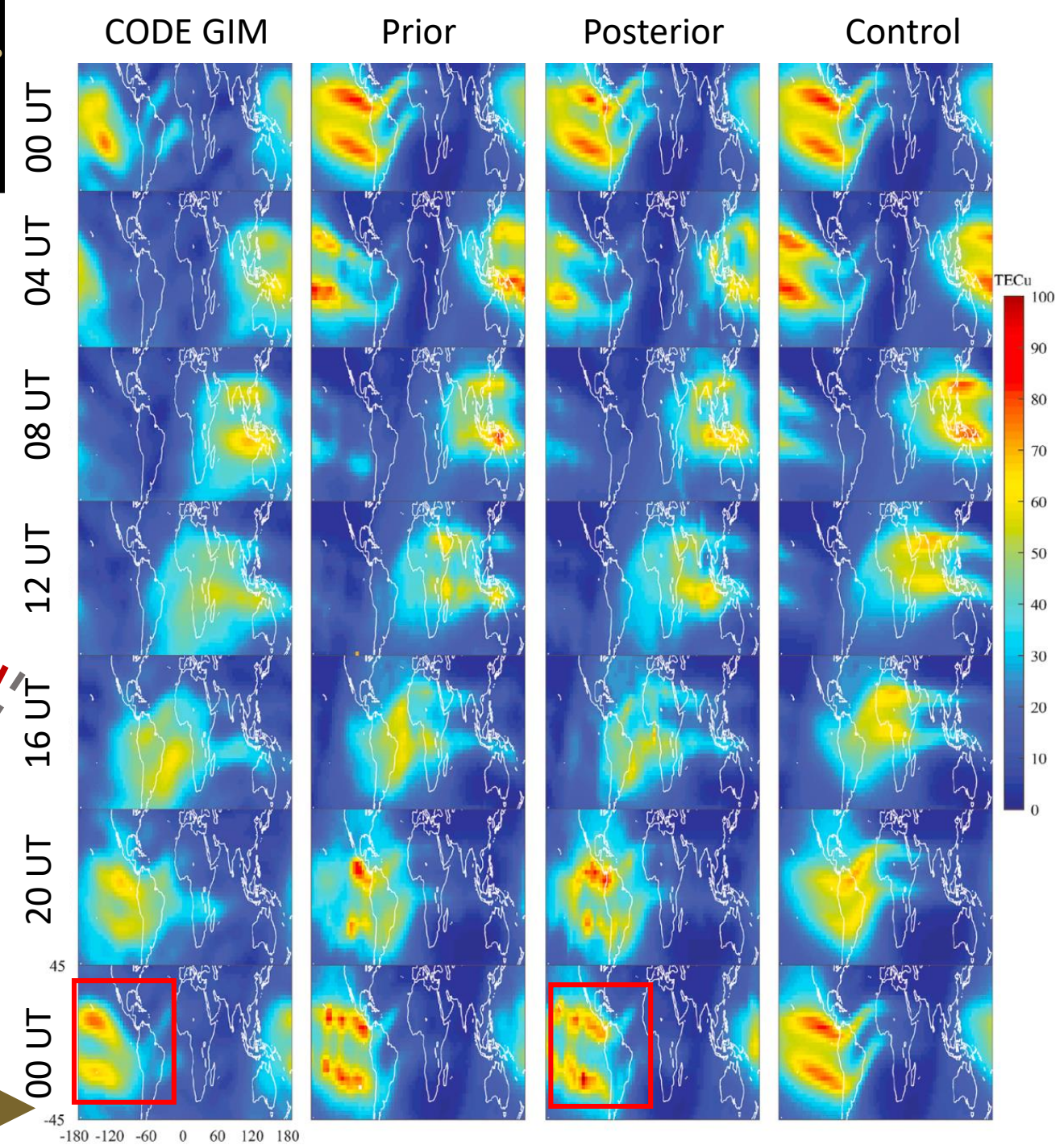
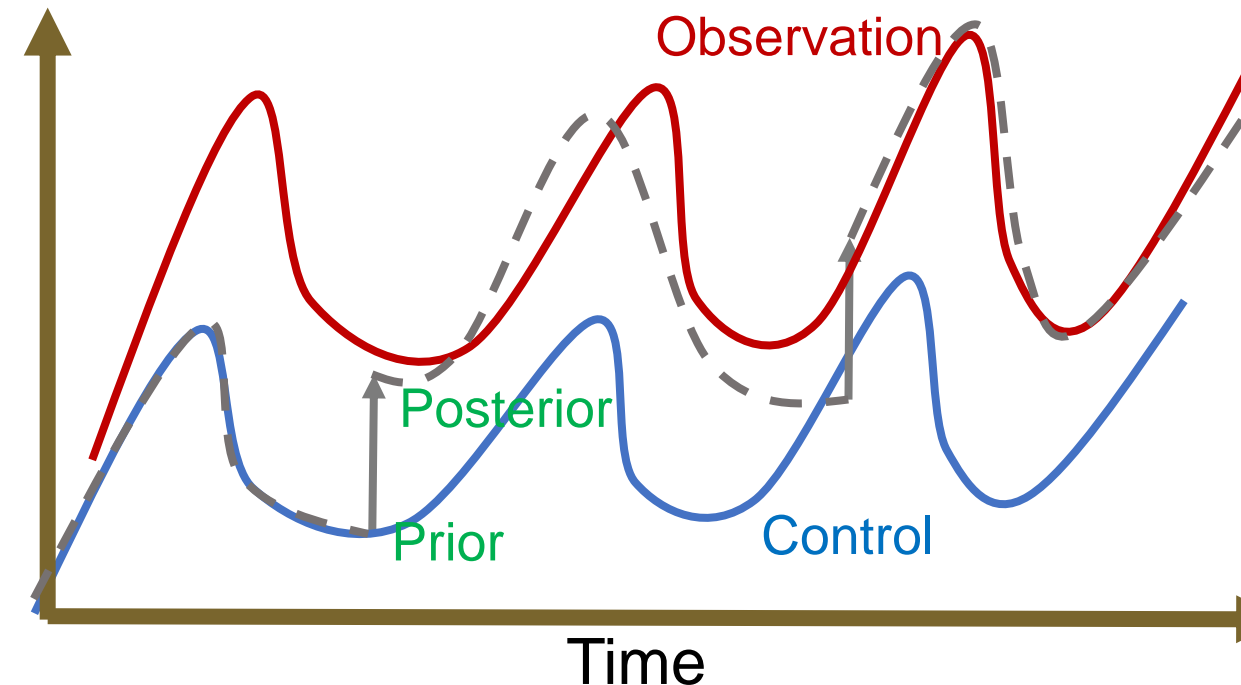


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A. OSE of the FORMOSAT-3/COSMIC

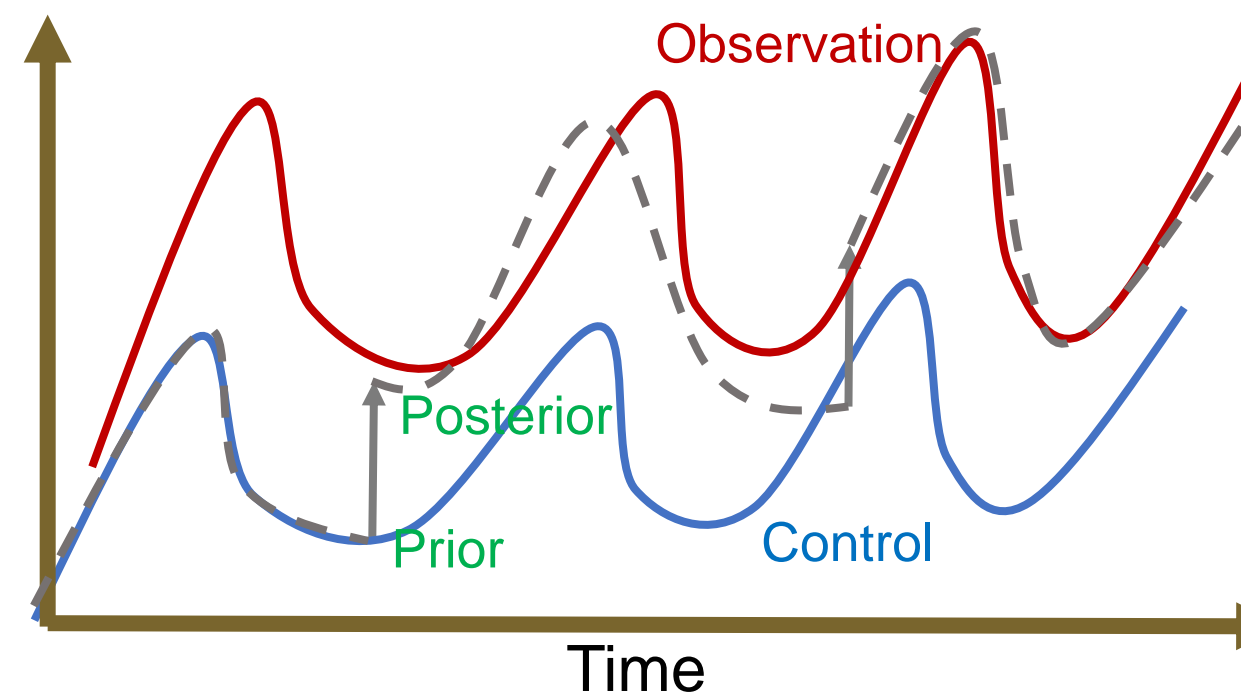
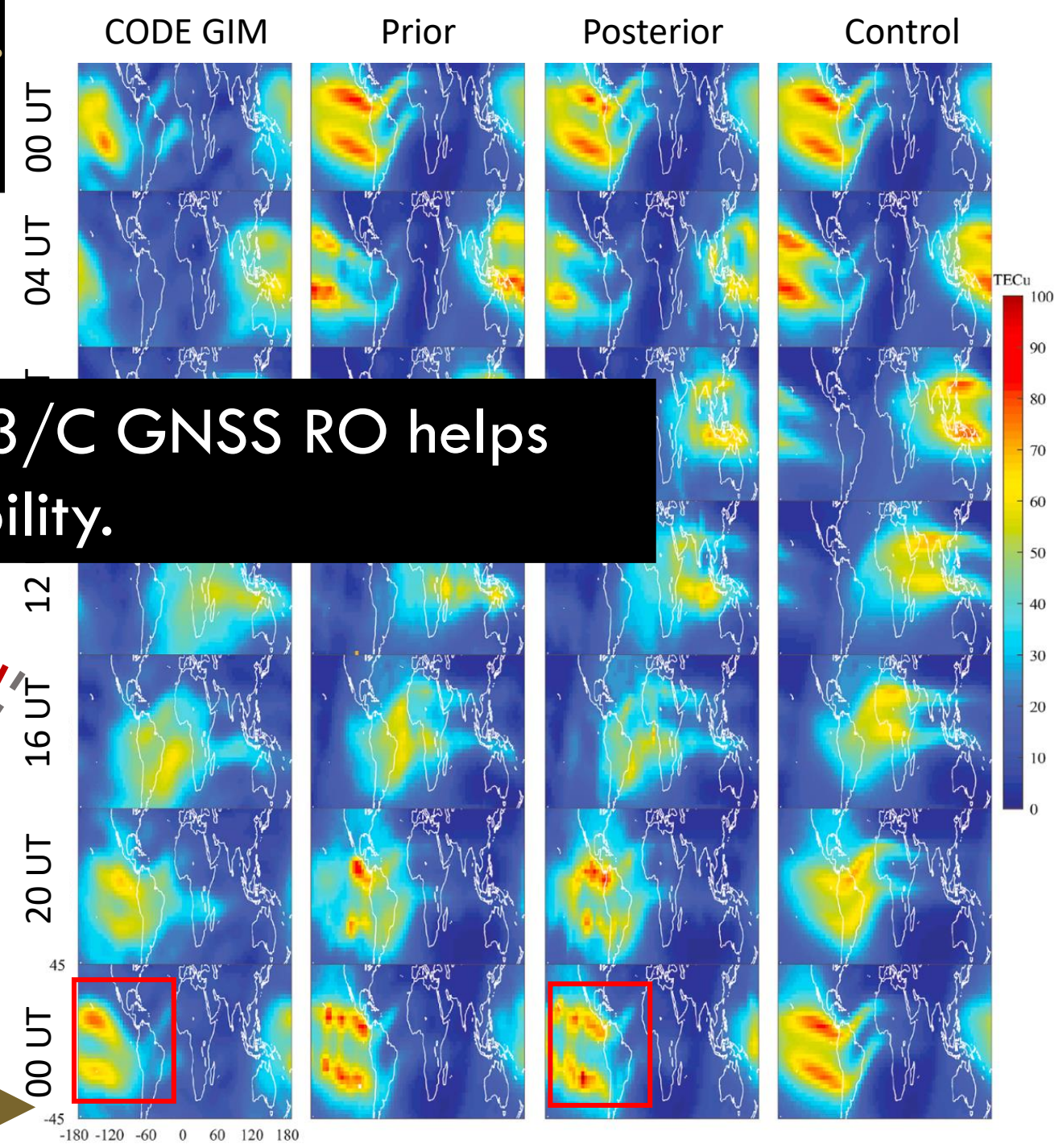
- Observation: F-3/C RO during Jan. 1, 2013
- Validation data: CODE GIM
- Assimilation cycle: 1 hour
- Assimilation period: 24 hours



A. OSE of the FORMOSAT-3/COSMIC

- Observation: F-3/C RO during Jan. 1, 2013
- Validation
- Assimilation
- Assimilation period: 24 hours

Remark 4: Assimilation of F-3/C GNSS RO helps introduce day-to-day variability.

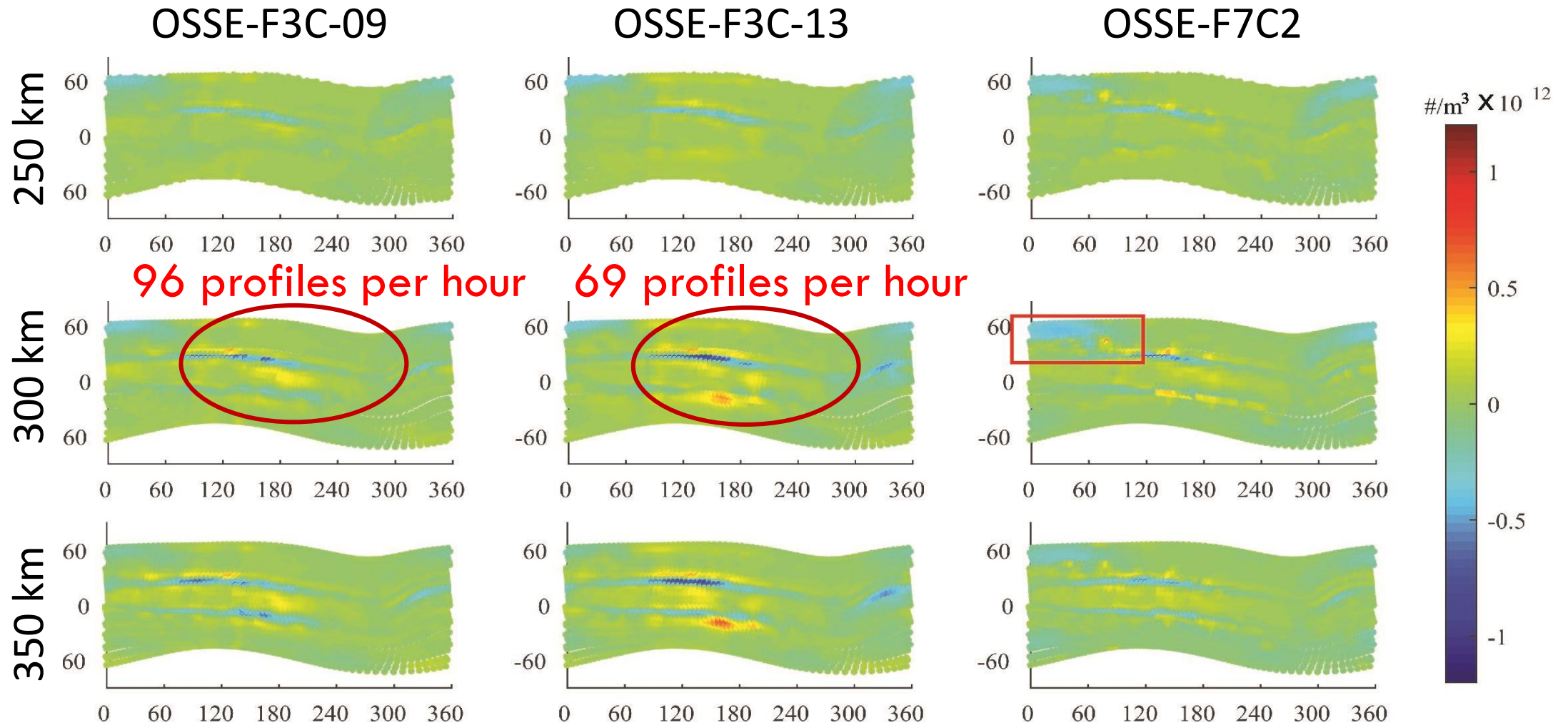


B. OSSEs for FORMOSAT-3/COSMIC & FORMOSAT-7/COSMIC-2

	OSSE-F3C-09	OSSE-F3C-13	OSSE-F7C2
Observing System	F3/C January 1 2009	F3/C January 1 2013	F7/C2
Average Number of sounding per hour	96	69	368
Horizontal Localization	10,000 km	10,000 km	5,000 km
Low & midlatitude RMSE (after 24-hour assimilation)			
High-latitude RMSE			

B. OSSEs for FORMOSAT-3/COSMIC & FORMOSAT-7/COSMIC-2

$$e_{\text{posterior}}^- - e_{NR}^-$$



B. OSSEs for FORMOSAT-3/COSMIC & FORMOSAT-7/COSMIC-2

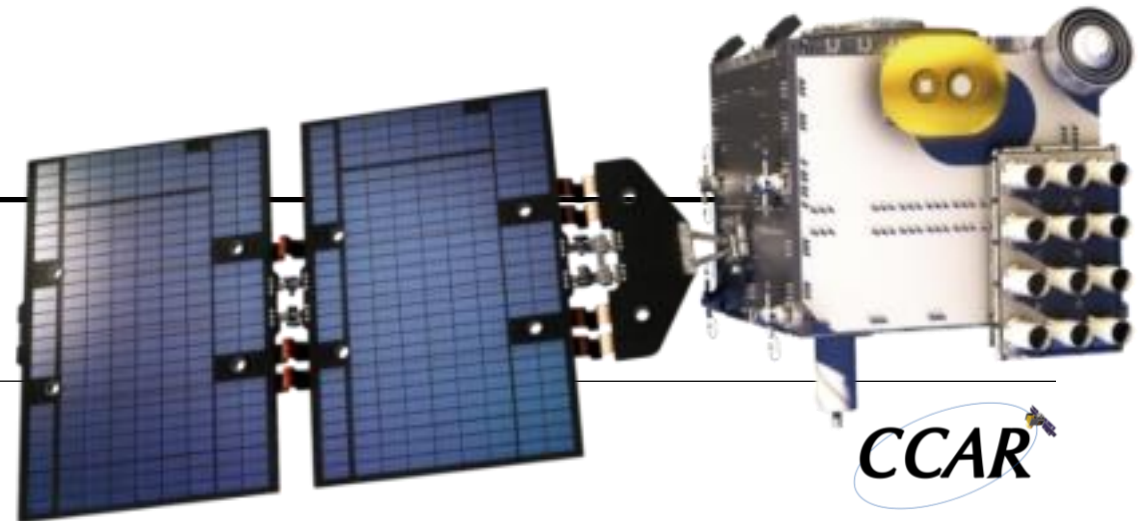
	OSSE-F3C-09	OSSE-F3C-13	OSSE-F7C2
Observing system	F3/C January 1 2009	F3/C January 1 2013	F7/C2
Average number of sounding per hour	96	69	368
Horizontal localization	10,000 km	10,000 km	5,000 km
Low & midlatitude RMSE ratio (after 24-hour assimilation)	0.39	0.51	0.33
High-latitude RMSE ratio	0.52	0.63	0.74

B. OSSEs for FORMOSAT-3/COSMIC & FORMOSAT-7/COSMIC-2

	OSSE-F3C-09	OSSE-F3C-13	OSSE-F7C2
Observing system	F3/C January 1 2009	F3/C January 1 2013	F7/C2
Average number of OSSEs per hour	<p>Remark 5: In comparison to the F-3/C, the F-7/C-2 has higher impact on ionospheric specification in mid- and low-latitude region.</p>		
Horizontal coverage			
Low & mid-latitude coverage (after 24-hour recovery)	<p>Remark 6: Comparative OSSEs of the F-3/C (09 vs 13) shows importance of sufficient amount of RO coverage.</p>		
High-latitude coverage			

More Information on FORMOSAT-7/COSMIC-2

Orbit	Altitude 520~ 550 km, 24 degree inclination
Period	About 97 minutes
Constellation	6 SC to low-inclination-angle orbit
GNSS RO Payload	TGRS
Scientific Payload	IVM and RF Beacon Instrument
Launch Vehicle	Falcon Heavy
Launch Schedule	June 24, 2019
Mission Life	5 years



More Information on FORMOSAT-7/COSMIC-2

2019/1/28-30

2019/04

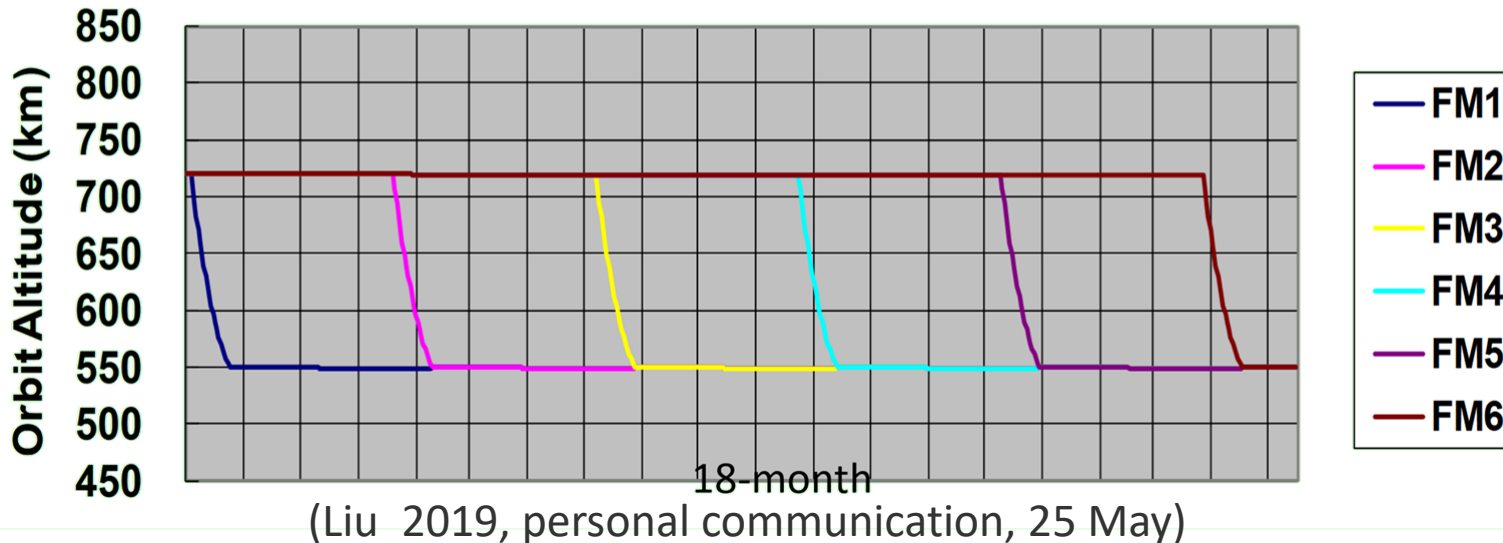
LD-40~36 days Launch Date (LD)

Pre-Ship Review & Operations
Readiness Review

Shipping Satellites from
NSPO to Launch Site

Mission Readiness
Review & ESC#12

FORMOSAT-7 Constellation Altitude Deployment Profile



Satellites will be separated to 6 orbital planes with 60-deg separation to a mission orbit of 520 km altitude **19 months after launch.**



Conclusions

- Optimization of EnSRF parameters (e.g. covariance localization) is important for each observing system. (Hsu et al., JGR, 2017)
- OSE shows that data assimilation of F-3/C RO sTEC can **introduce observed variability into the model**. (Hsu et al., ESS, 2018)
- OSSEs show that **F-7/C-2 can improve the mid- and low-latitude ionospheric specification considerably by 33%**. (Hsu et al., ESS, 2018)
- **F-7/C-2 are going to be launched on 24th June !**

Relevant Poster: DATA03, Poster Section, Tuesday

References

- Hsu, C.-T., Matsuo, T., Yue, X., Fang, T.-W., Fuller-Rowell, T., Ide, K., & Liu, J.-Y. (2018). Assessment of the impact of FORMOSAT-7/COSMIC-2 GNSS RO observations on midlatitude and low-latitude ionosphere specification: Observing system simulation experiments using Ensemble Square Root Filter. *J. Geophys. Res.: Space Phys.*, 123, 2296–2314.
- Hsu, C.-T., Matsuo, T., & Liu, J.-Y. (2018). Impact of assimilating the FORMOSAT-3/COSMIC and FORMOSAT-7/COSMIC-2 RO data on the midlatitude and low-latitude ionospheric specification. *Earth and Space Sci.*, 5, 875–890.
- Whitaker, J. & Hamill, T. M. (2002) Ensemble data assimilation without perturbed observations. *Mon. Wea. Rev.*, 130, 1913–1924.