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# Mesospheric bore evolution characteristics

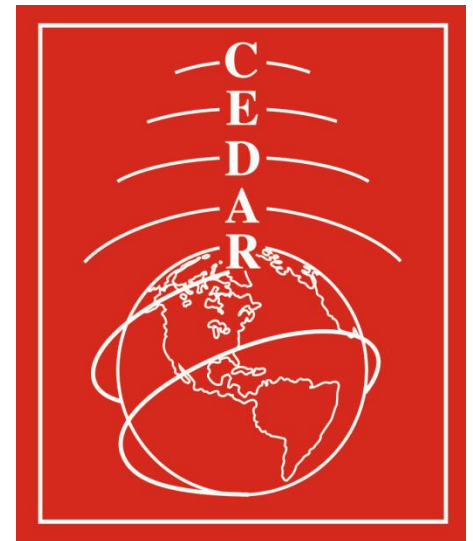
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NorthWest Research Associates

CEDAR Postdoc Report #2

June 27<sup>th</sup>, 2012



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# Mesospheric Bore Evolution Characteristics

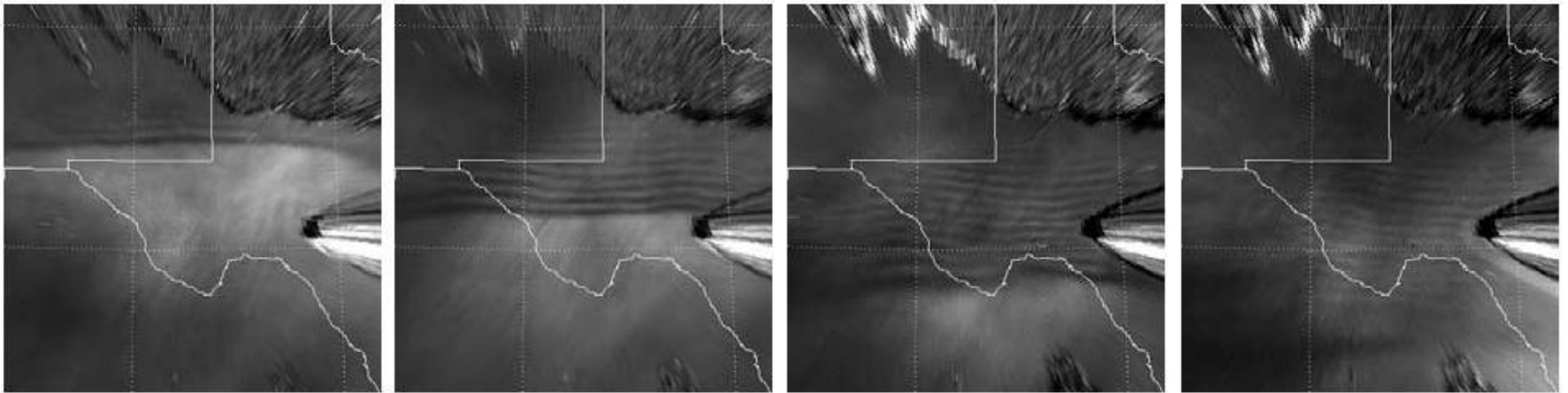
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- What are Mesospheric Bores?
- Numerical Models
- BDO theory
- Results
  - Forcing dependence
  - Ducting environment dependence
- Conclusions

# What are mesospheric bores?

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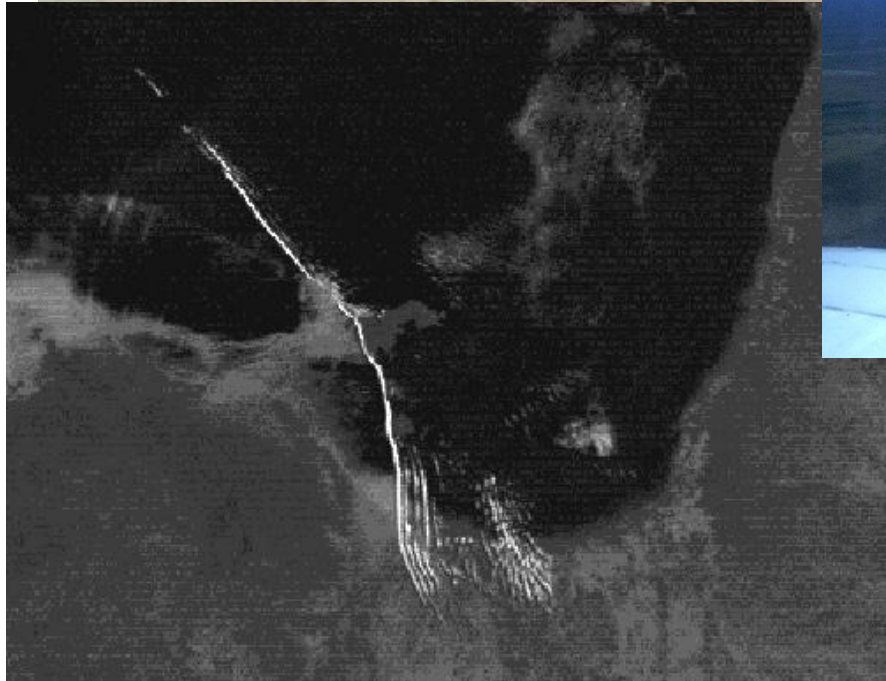
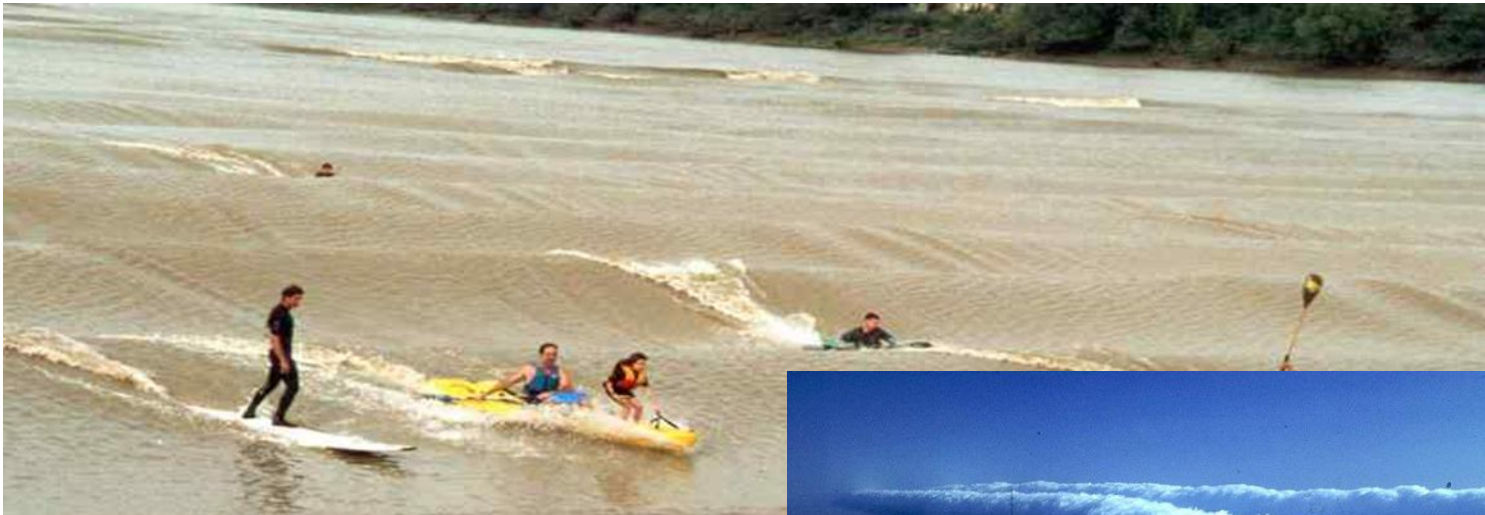
- Roughly 2D, weakly non-linear, ducted wave phenomenon
- Characterized by crest creation
- Observed at roughly 80 – 100 km
- Propagate at speed of  $\sim 75$  m/s
- Length scales of  $\sim 20$  km



4 time ordered images of a propagating bore courtesy of Steve Smith.  
CSU lidar data shows a strong thermal inversion of 50 K between 85 and 90 km.

# Other Bores

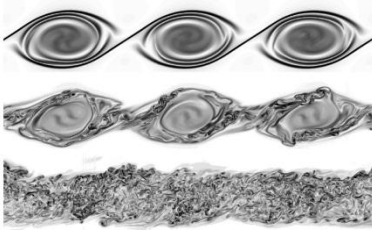
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# Navier-Stokes model

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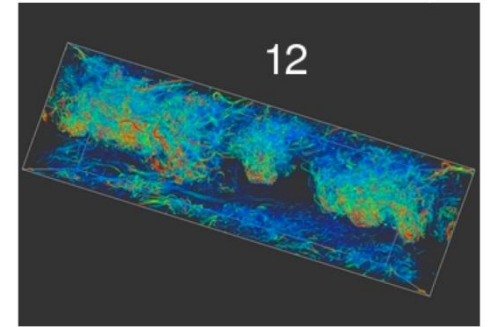
We numerically solve the Navier – Stokes equations



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Momentum  
Continuity  
Heat Equation  
Ideal Gas Law

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- It is a DNS model – Direct Numerical Simulation
- It uses the Boussinesq Approximation – incompressible
- 2-D simulations evolve *potential temperature* and *vertical velocity*

# BDO model : A useful approximation

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The BDO equation makes two approximations.

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1. Fairly-long wavelength  $\rightarrow$  weak dispersion

$$c = c_0(1 - \delta|k|)$$

2. Small-but-finite amplitude  $\rightarrow$  weakly nonlinear effects:

- Steepening
  - No breaking
  - No recirculation
- 
- 

Evolves displacement:

$$\eta(x, z, t) = A(x, t) \phi(z)$$

- Evolution equation
  - Modal equation
- 

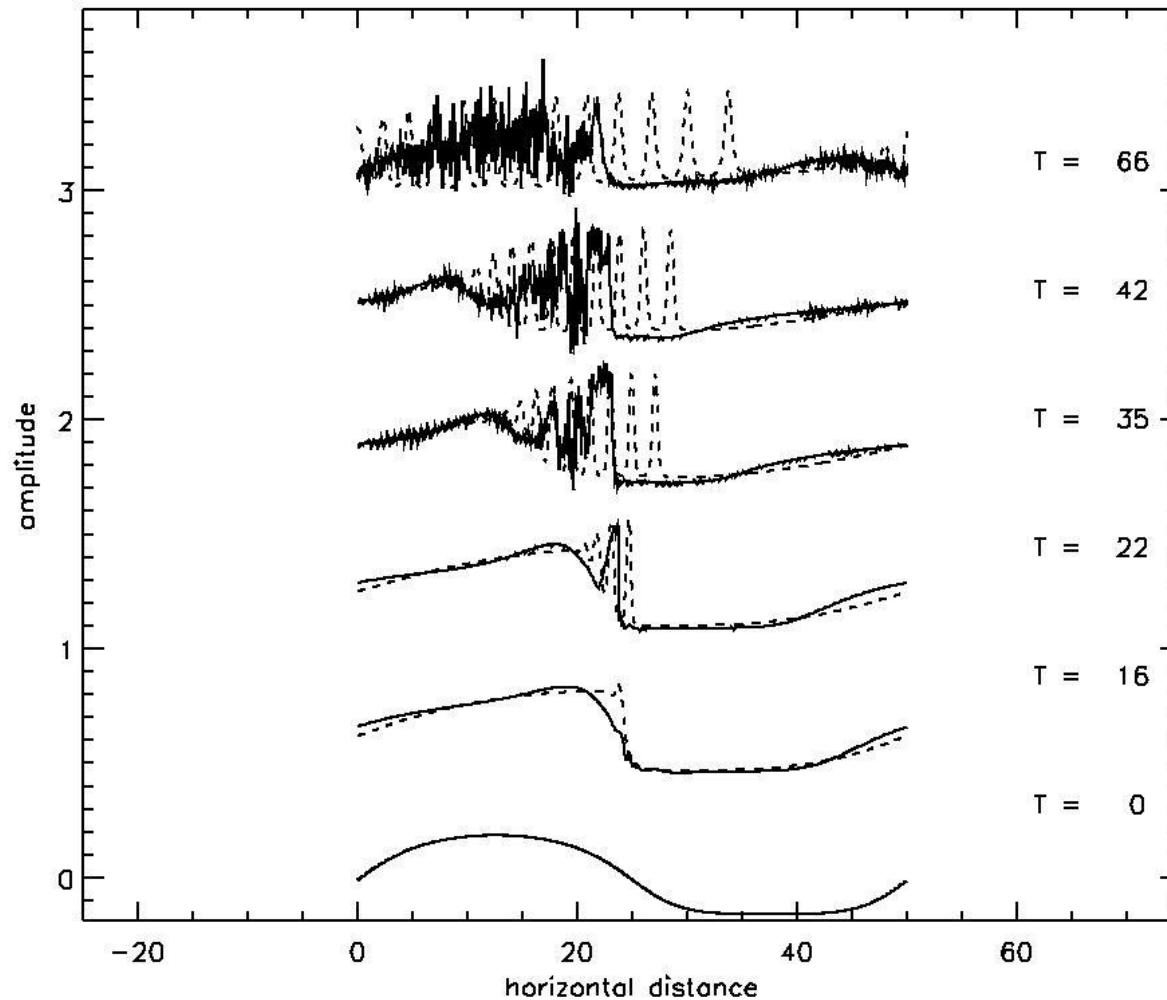
Steady-state solution:

$$A(x, t) = \frac{a\lambda^2}{(x - c_b t)^2 + \lambda^2}, \quad c_b = c_0 + \frac{\delta}{\lambda}, \quad a\lambda = \frac{4\delta}{\alpha}$$

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# The BDO equation : large amplitude limit



- BDO handles nonlinearity through crest creation
- NS model predicts breaking

# Results

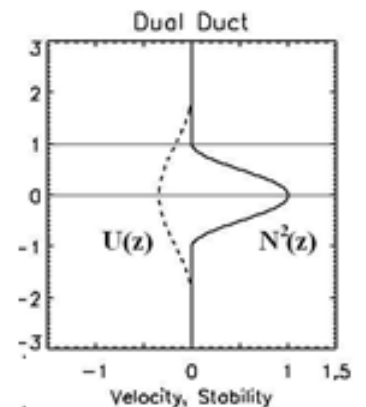
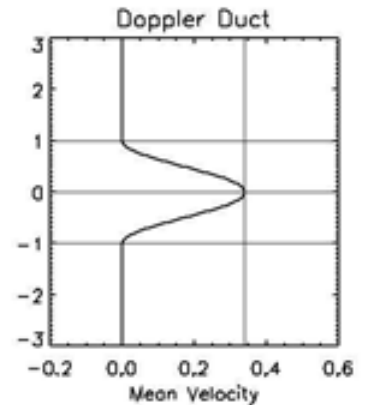
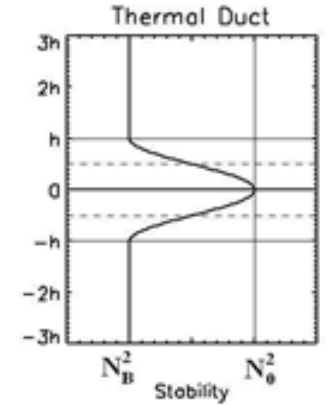
- Forcing geometry effects (*simple thermal duct*)

- Wavelength effects
- Amplitude effects

$$A(x, t_0) \sim \sin\left(\frac{2\pi}{\lambda_x} x\right)$$

- Ducting environment effects

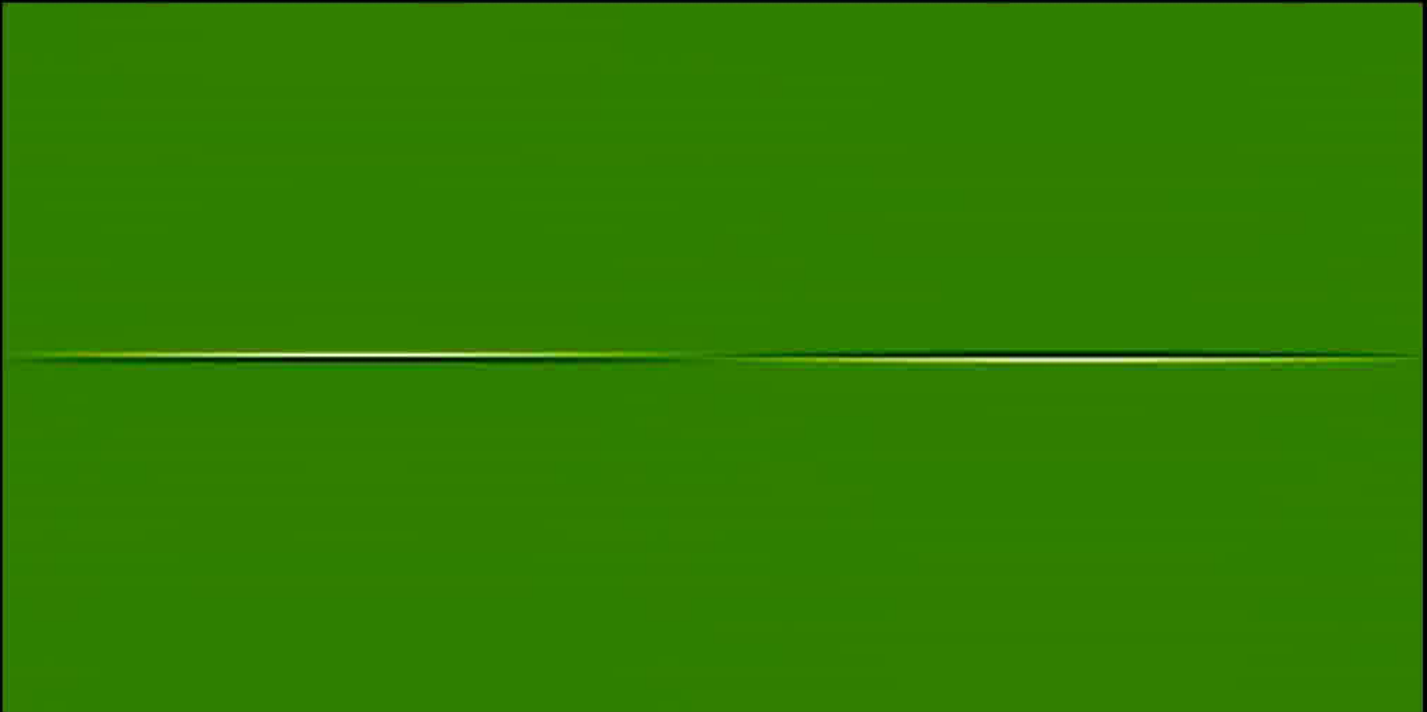
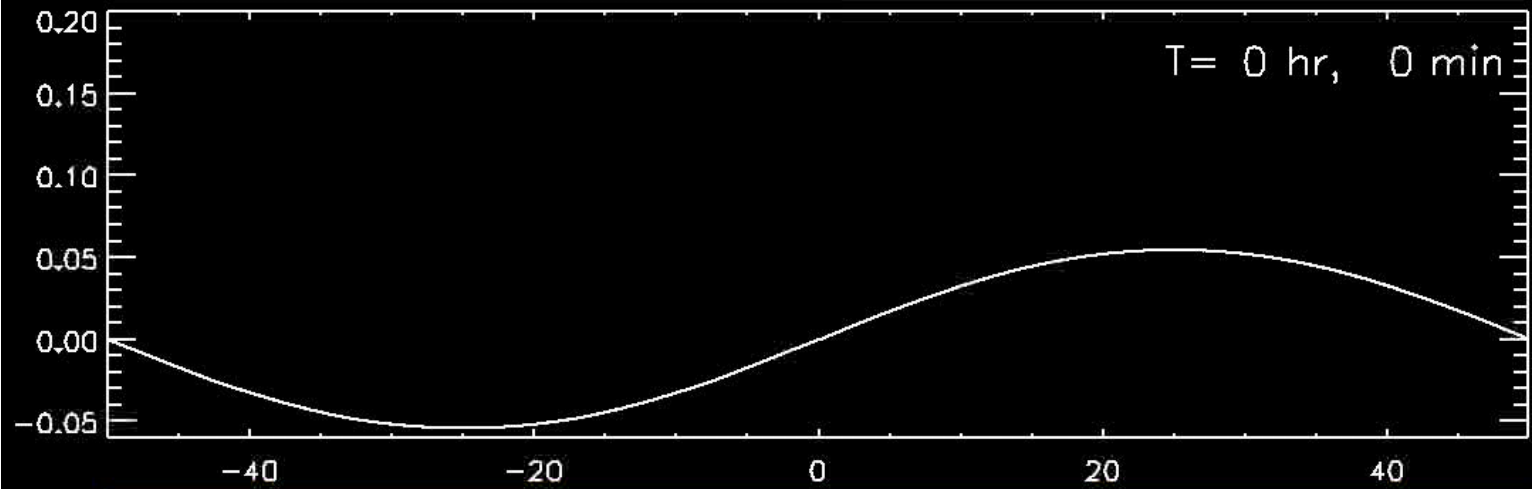
- Duct shape (*cosine v. sech-squared*)
- Duct thickness (*increased h*)
- Viscous effects
- Non-zero background stability
- Isolated Doppler duct
- Co-located ducts (*Headwinds/Tailwinds*)



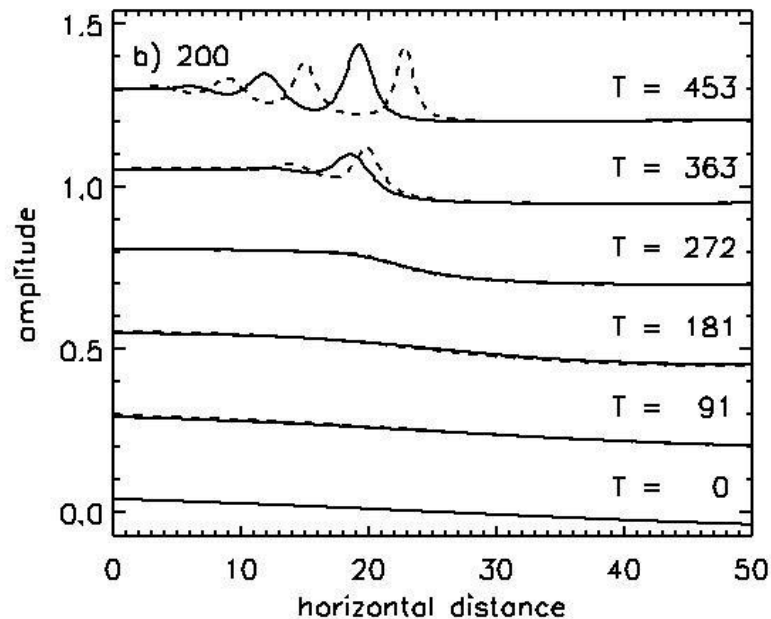
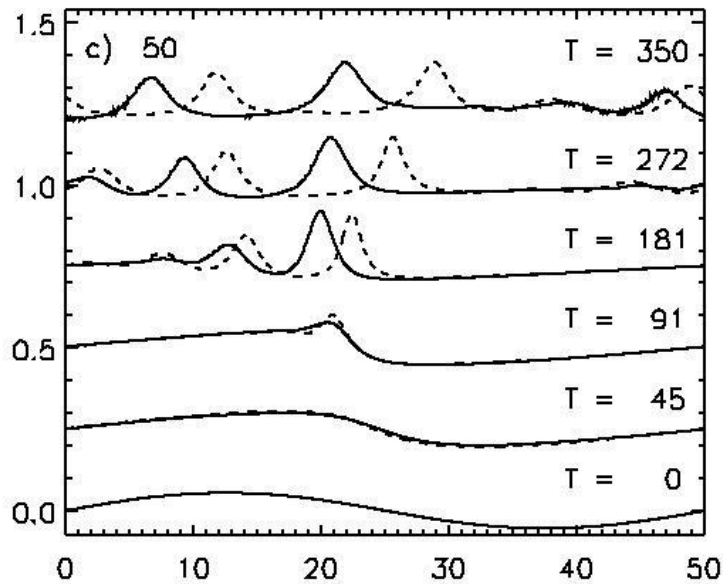
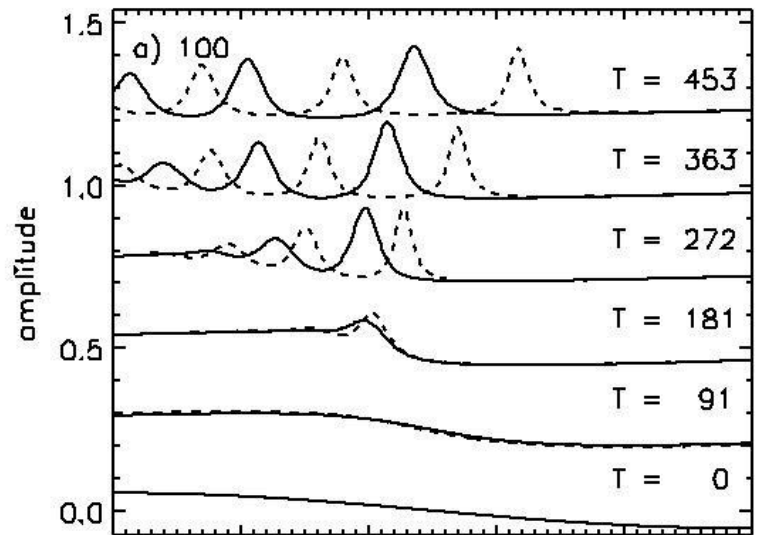


Results : Thermal duct,  $\lambda = 100$ ,  $\eta_0 = 0.1$ ,  $\nu = 0$

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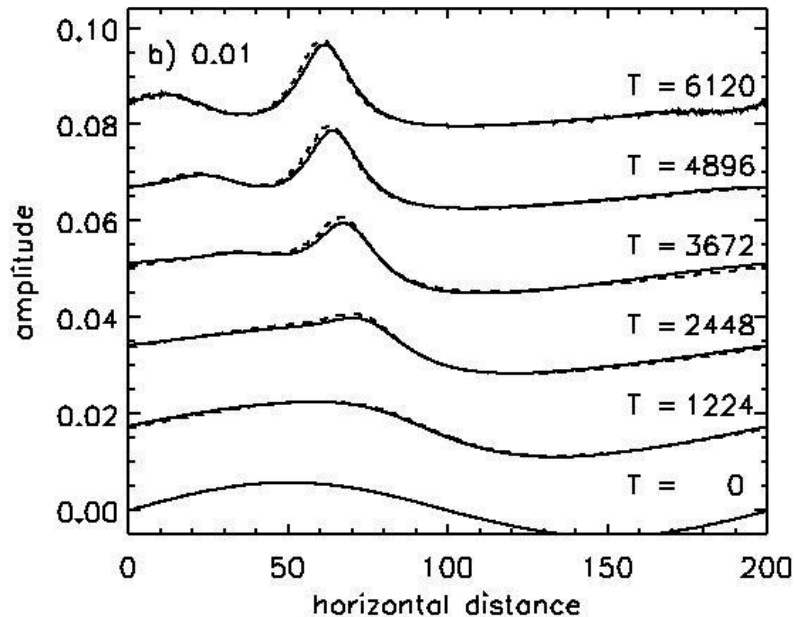
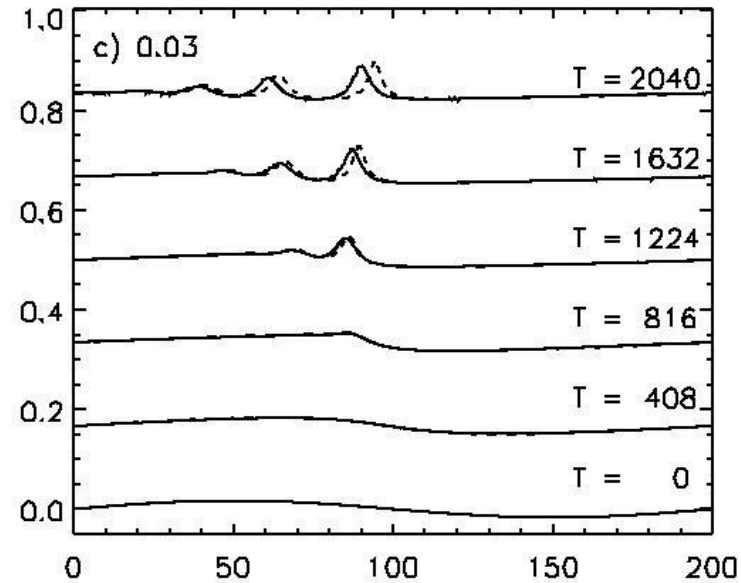
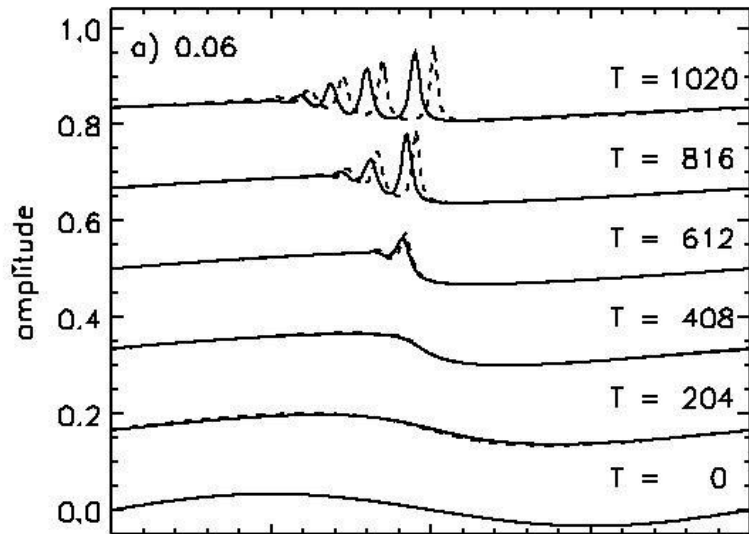


# Results : Sine wave, wavelength variation



- Crest creation time proportional to wavelength.
- Crest geometry is roughly independent of perturbation wavelength.

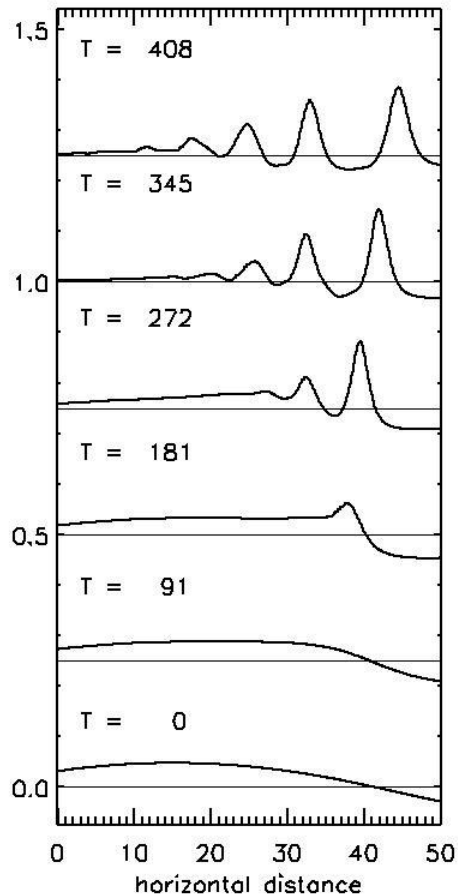
# Results : Sine wave, amplitude variation



- Crest creation time inversely proportional to amplitude.
- Crest geometry is a function of perturbation amplitude.
- NS/BDO agreement improves for smaller amplitudes.

# Results : Duct shape

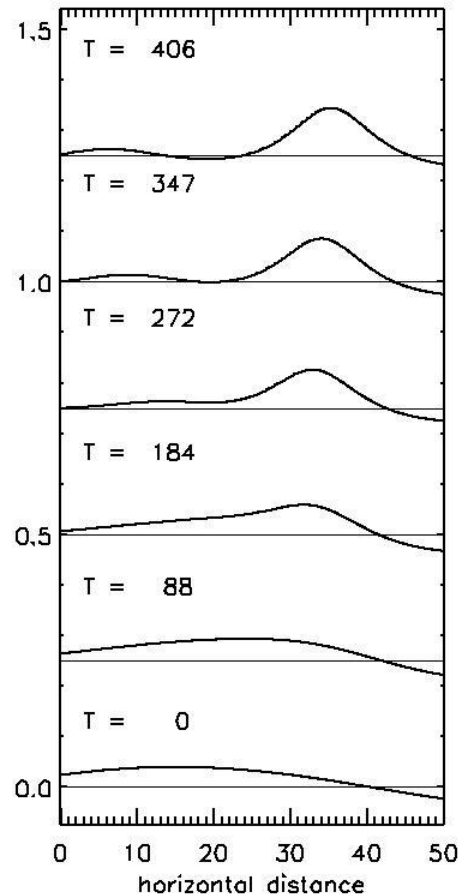
$$\sim N_0^2 \cos(\pi z/h)$$



$$\alpha \sim 1.03 \quad \delta \sim 0.093$$

$$c_0 \sim 0.33$$

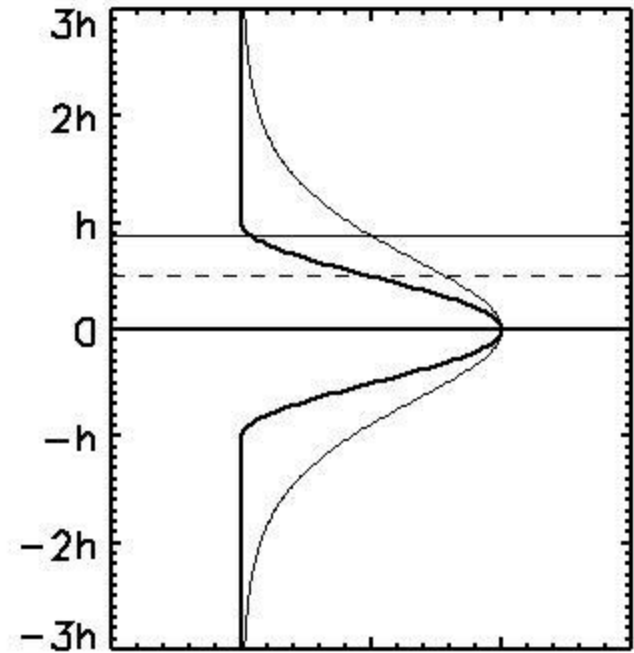
$$\sim N_0^2 \text{sech}^2(z/h)$$



$$\alpha \sim 0.84 \quad \delta \sim 0.53$$

$$c_0 \sim 0.70$$

Thermal Duct

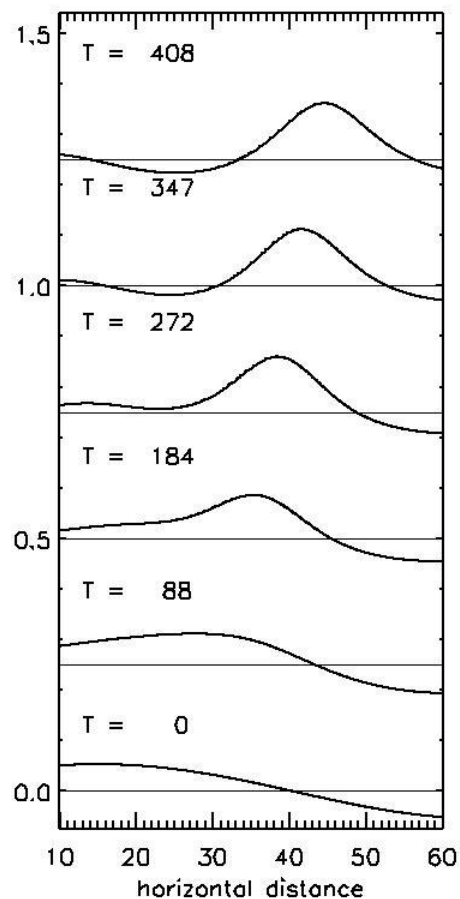


Stability

$$a\lambda = \frac{4\delta}{\alpha}$$

# Results : Duct thickness

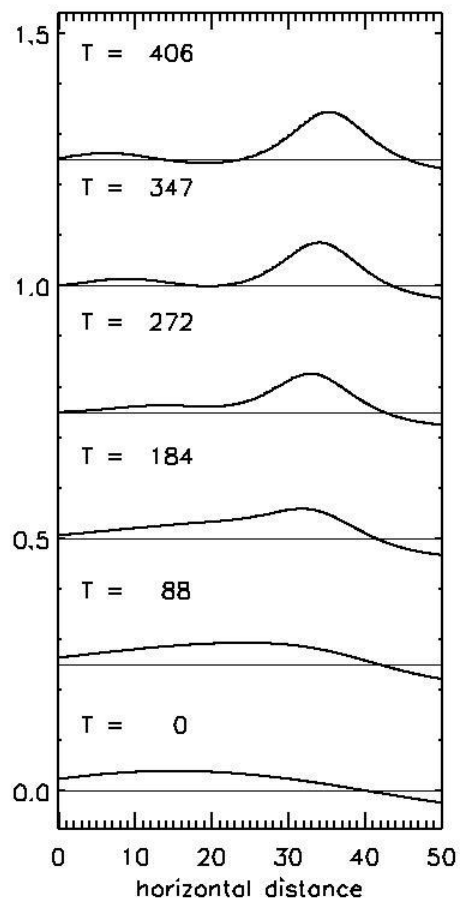
$$\sim N_0^2 \cos(\pi z/h)$$



$$\alpha \sim 1.03 \quad \delta \sim 0.648$$

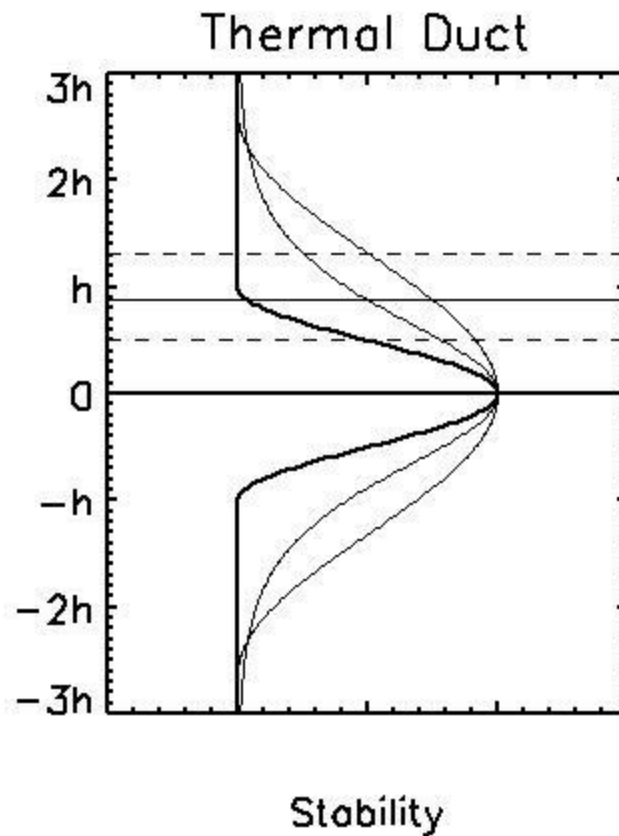
$$c_0 \sim 0.885$$

$$\sim N_0^2 \text{sech}^2(z/h)$$



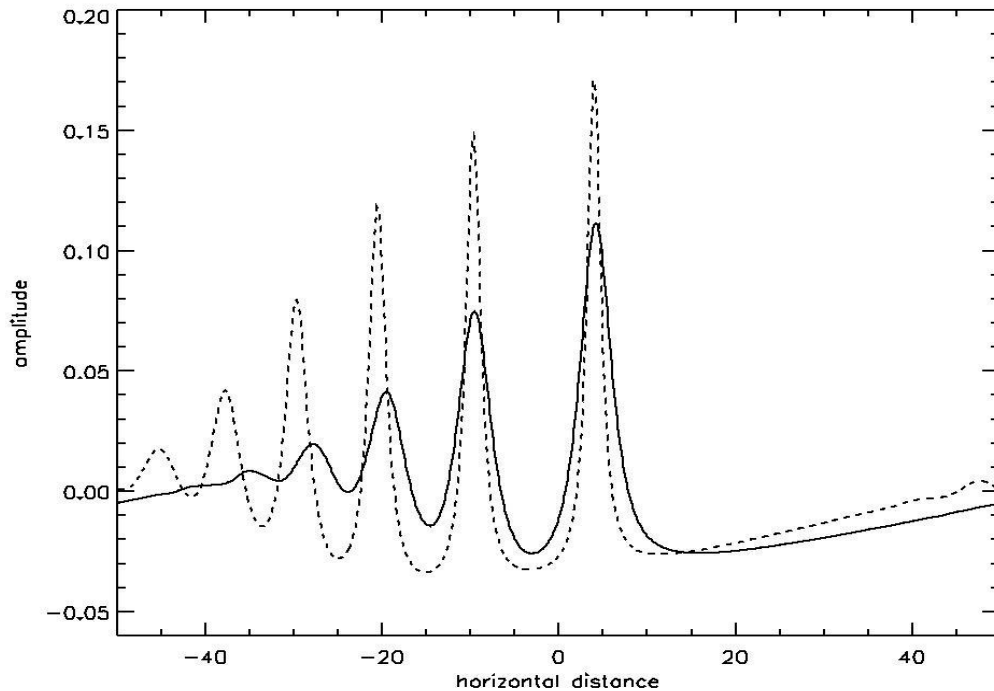
$$\alpha \sim 0.84 \quad \delta \sim 0.53$$

$$c_0 \sim 0.70$$



$$a\lambda = \frac{4\delta}{\alpha}$$

# Results: Viscosity = 100 m<sup>2</sup>/s

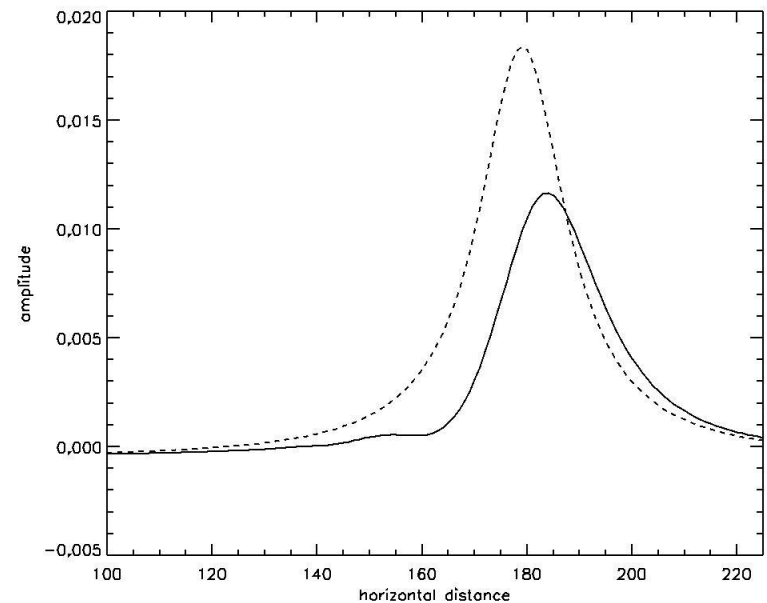


$T = 453 \sim 2 \text{ hrs}, 24 \text{ min}$

$\lambda = 100$

$\eta_0 = 0.1$

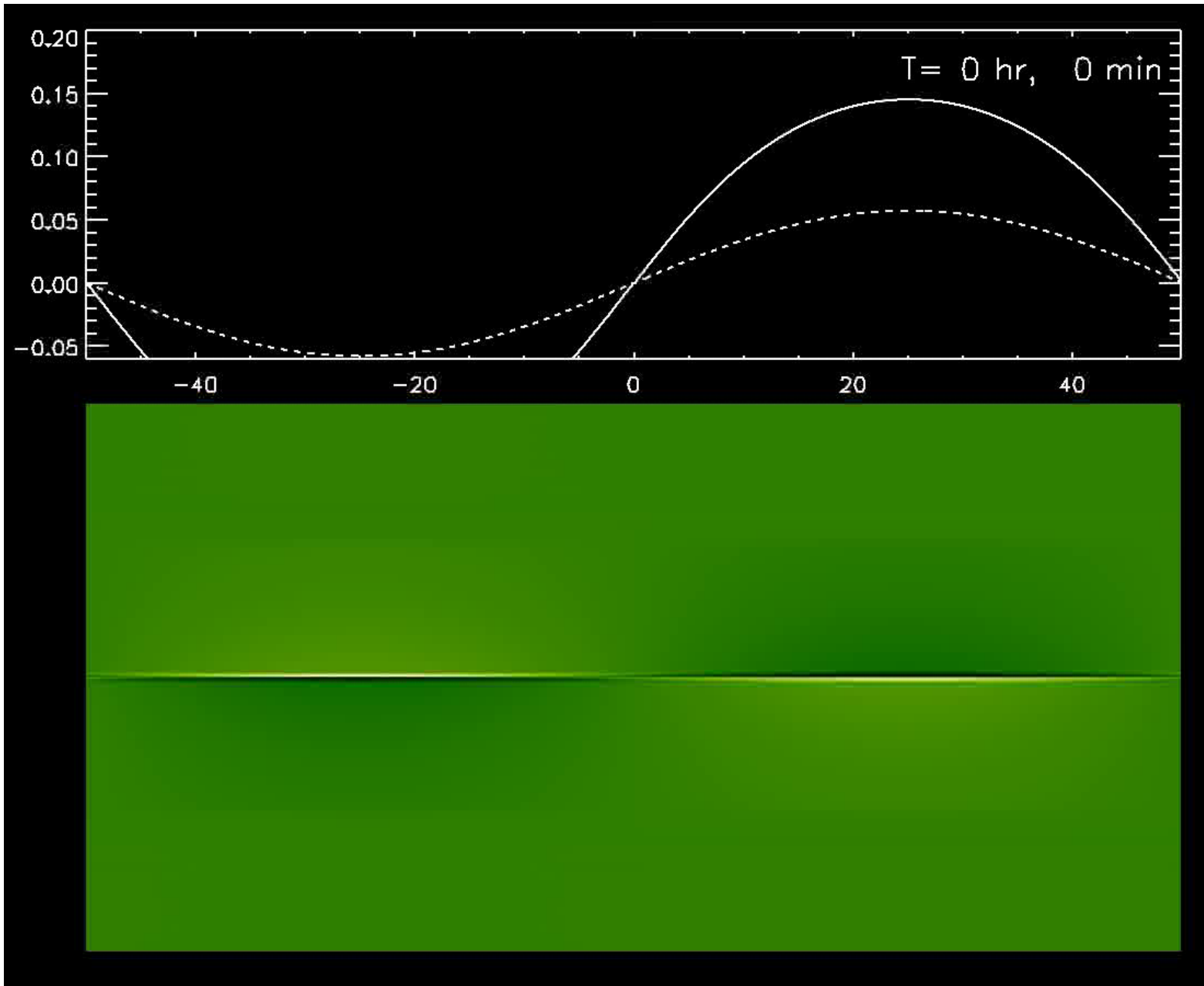
- Viscosity has the anticipated effect of reducing amplitude
- Viscosity has the unanticipated effect of advancing the leading peaks



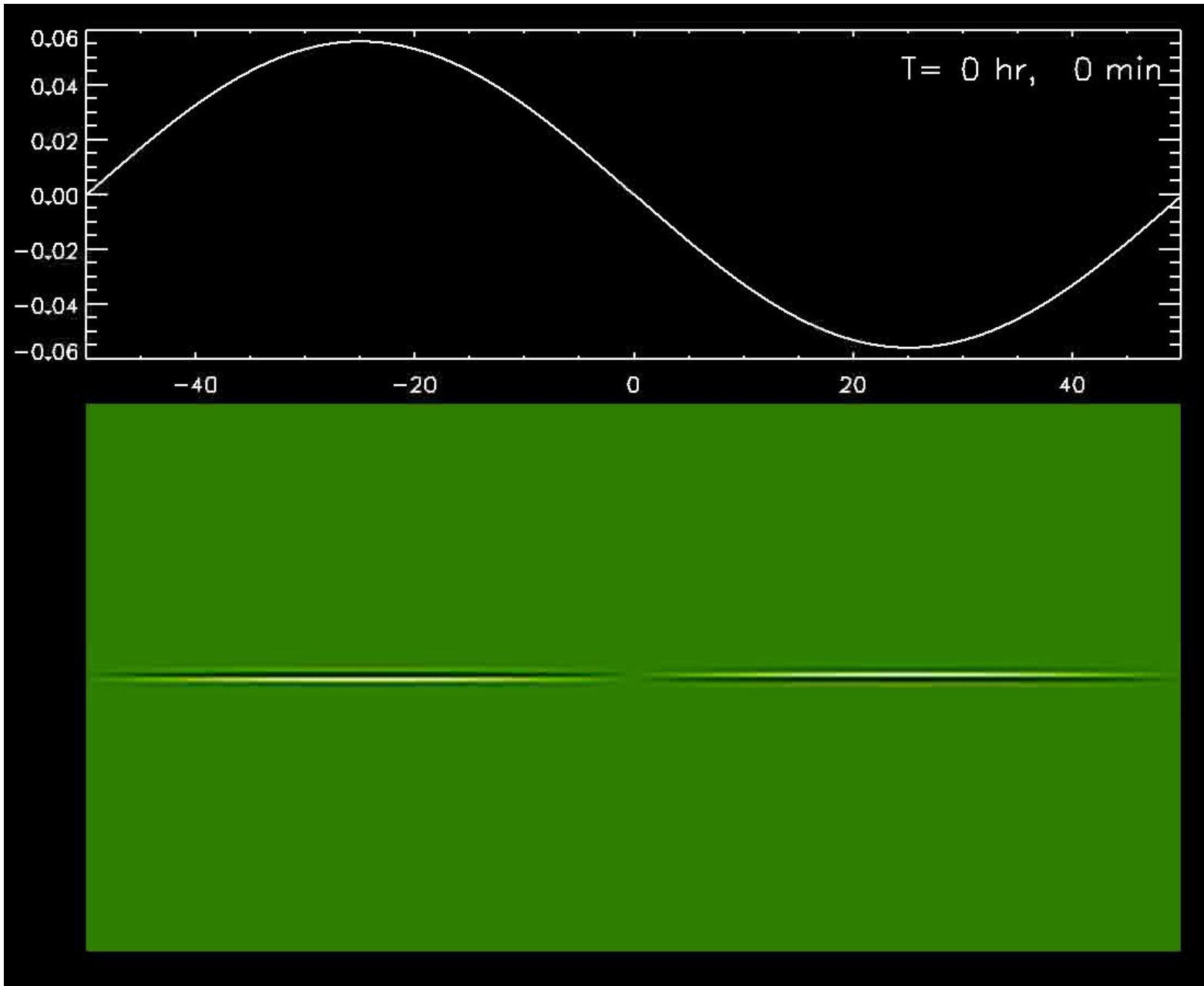
$T = 517 \sim 2 \text{ hrs}, 44 \text{ min}$

$\lambda = 10$

# Results : Non-zero background stability, $\nu = 100 \text{ m}^2/\text{s}$



# Results : Velocity Duct (high viscosity)





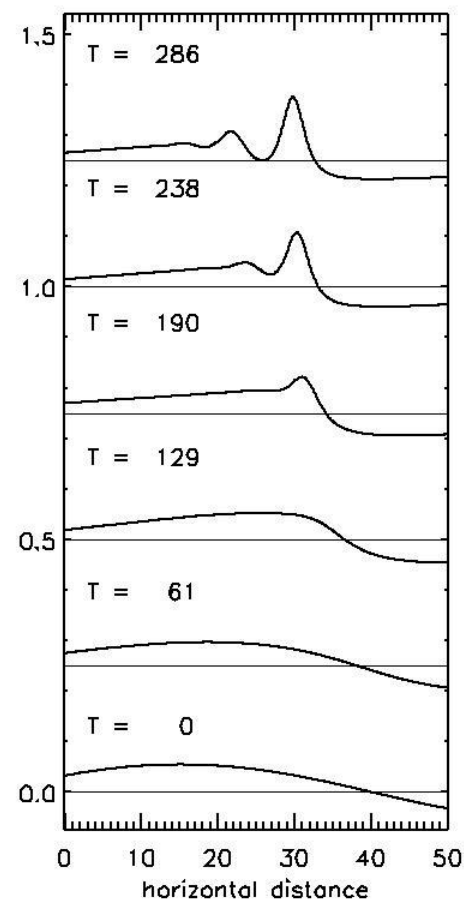
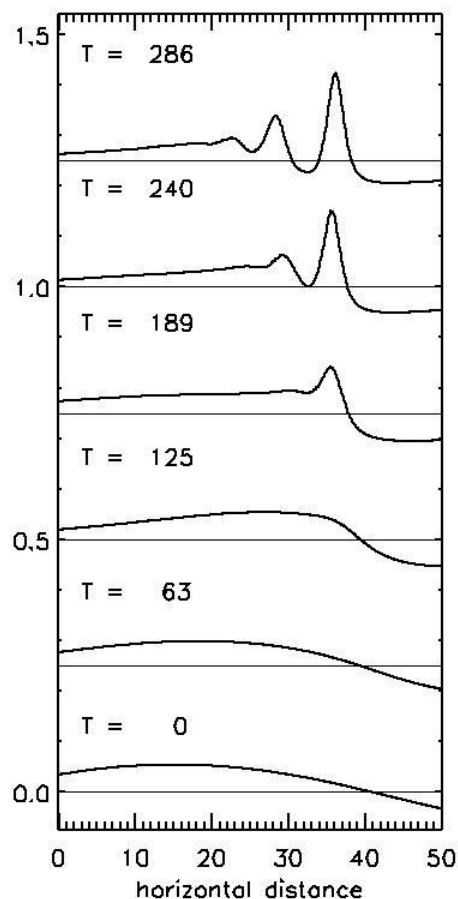
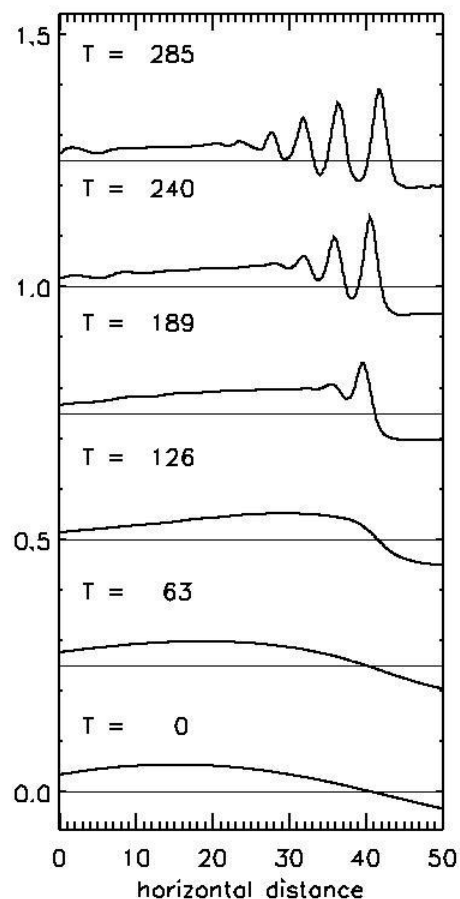
# Results : Headwind

Co-located thermal and doppler duct

$$l_s^2 = \frac{N^2(z)}{(U(z) - c)^2} - \frac{\partial_{zz} U(z)}{(u_0 - c)}$$

$$\sim -U_0 \cos(\pi z / 2)$$

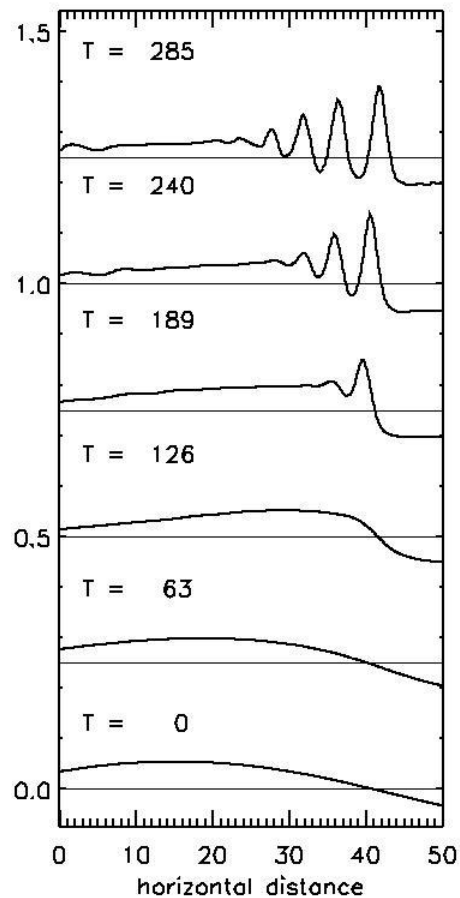
$$\sim -U_0 \cos(\pi z / 10)$$



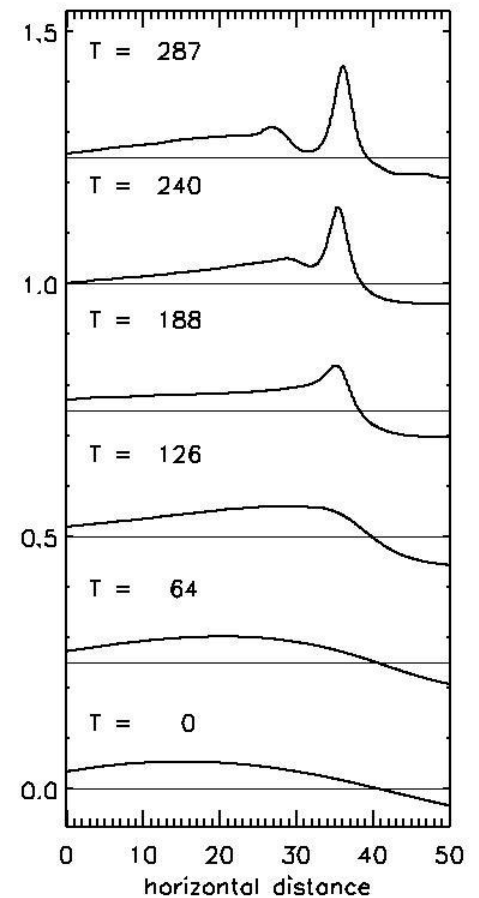
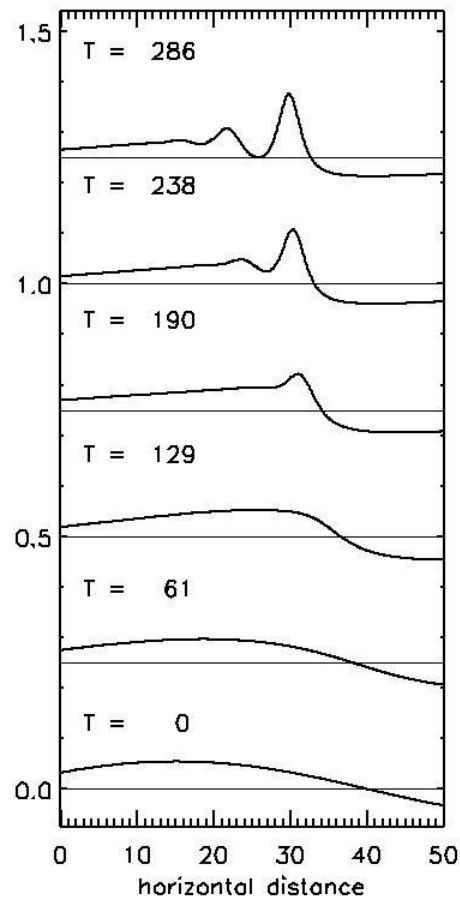
# Results : Tailwind

## Co-located thermal and doppler duct

$$\sim -U_0 \cos(\pi z/2)$$



$$\sim U_0 \cos(\pi z/2)$$



# Conclusions

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- Bore evolution dependence on imposed forcing
- Bore evolution dependence on ducting environment

# Future Work

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- Ultimately, extension to 3D, breaking bores, turbulence
- Temporally varying ducts
- Add complexity to BDO
- Pose more realistic forcings

