



Filtering/smoothing coupled technique implementation to the data assimilation algorithm

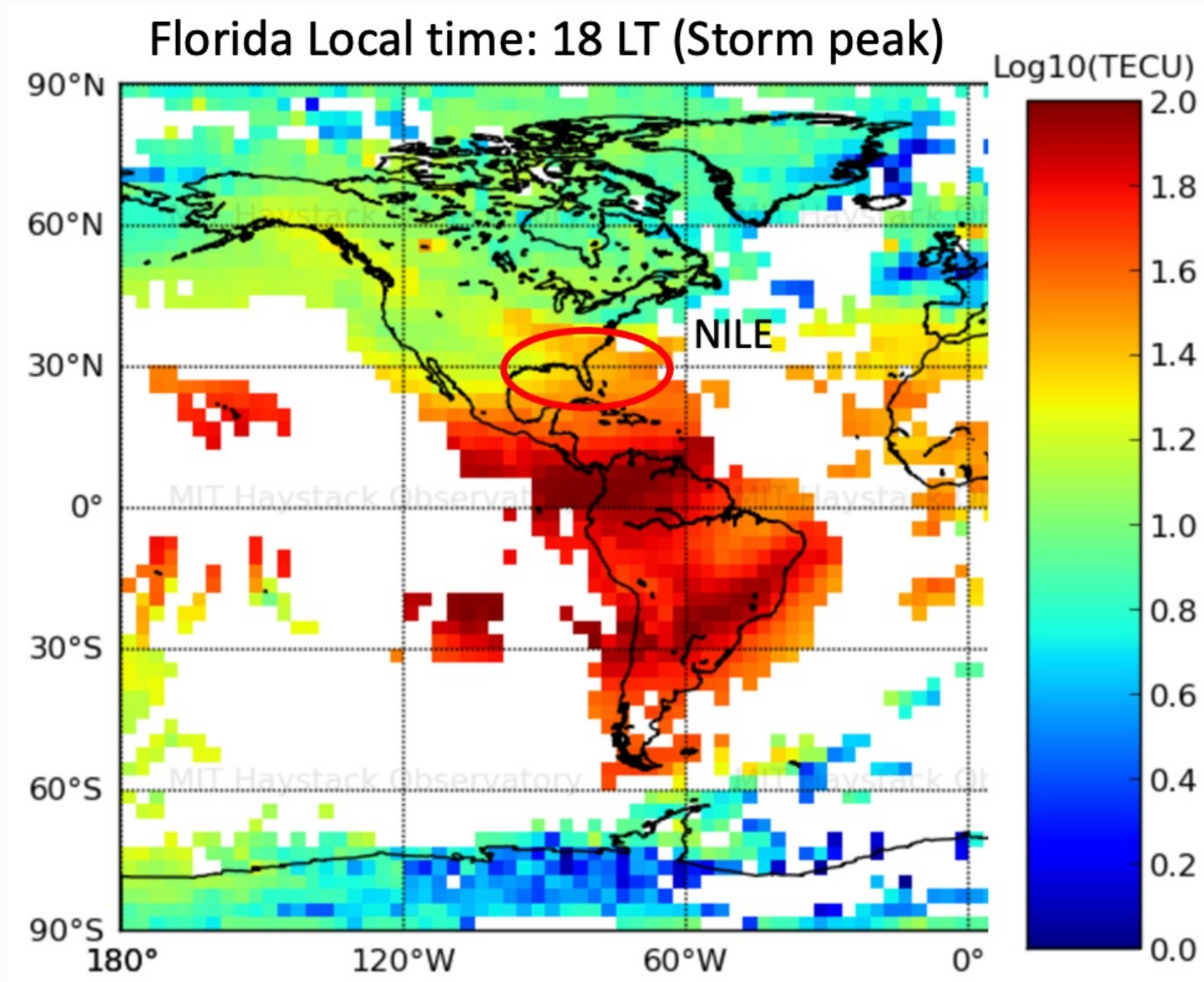
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Motivation

A storm-related phenomenon: **Nighttime Ionospheric Localized Enhancement (NILE)** [Datta-Barua, 2008]

- Enhanced electron density was observed in the Florida region during the local nighttime



- Investigating the NILE mechanism via
 - Developing the data assimilation algorithm: **Estimating Model Parameter Ionospheric Reverse Engineering (EMPIRE)** [Datta-Barua et al., 2009]

Fig. 1 GNSS total electron content map on log scale. Image credit: MIT Madrigal website

Objective

- To Implement the **coupled Kalman filter/smoothing technique** to EMPIRE algorithm
- To inspect the performance at a period of quiet time for **validation and error analysis**

Background – EMPIRE algorithm

EMPIRE algorithm: Reduce the gap between background model estimations and measurements [Miladinovich, 2018]

- Analyze the ionospheric drivers with a **4D global grid map** governed by the **ion continuity equation**
 - 4D global grid map**

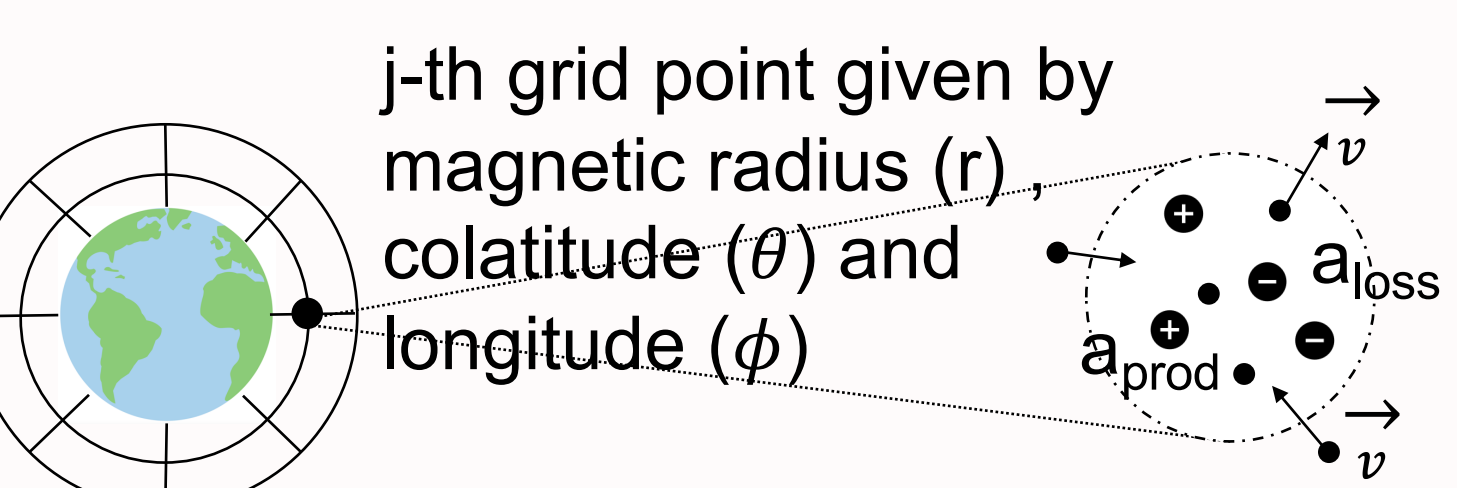


Fig. 2 Global grid map and representation of plasma flow in a constrained volume. Image credit: Aurora López-Rubio

Ion continuity equation

$$\frac{\partial N}{\partial t} = \underbrace{s_{prod}}_{a_{prod,0}} + \underbrace{s_{loss}}_{a_{loss,0}} - \underbrace{\vec{\nabla} \cdot (N\vec{v}_{\perp})}_{a_{\perp}} - \underbrace{\vec{\nabla} \cdot (N\vec{v}_{\parallel})}_{a_{\parallel}}$$

- Measurements: 4D global total electron content density rate $[\partial N/\partial t]$
- Background components $[a_0]$: Production rate $[a_{prod,0}]$, loss rate $[a_{loss,0}]$, Diffusive rate $[a_{dfs,0}]$, Gravitation effect $[a_{grav,0}]$
- Ionospheric drivers to be estimated:**
 - Neutral wind $[\delta a_{\parallel}]$:** Parallel to the earth's magnetic field
 - Ion drifts $[\delta a_{\perp}]$:** Perpendicular to the earth's magnetic field

New implementation – Kalman Smoother

Kalman filter/smoothing coupled technique conceptual flow

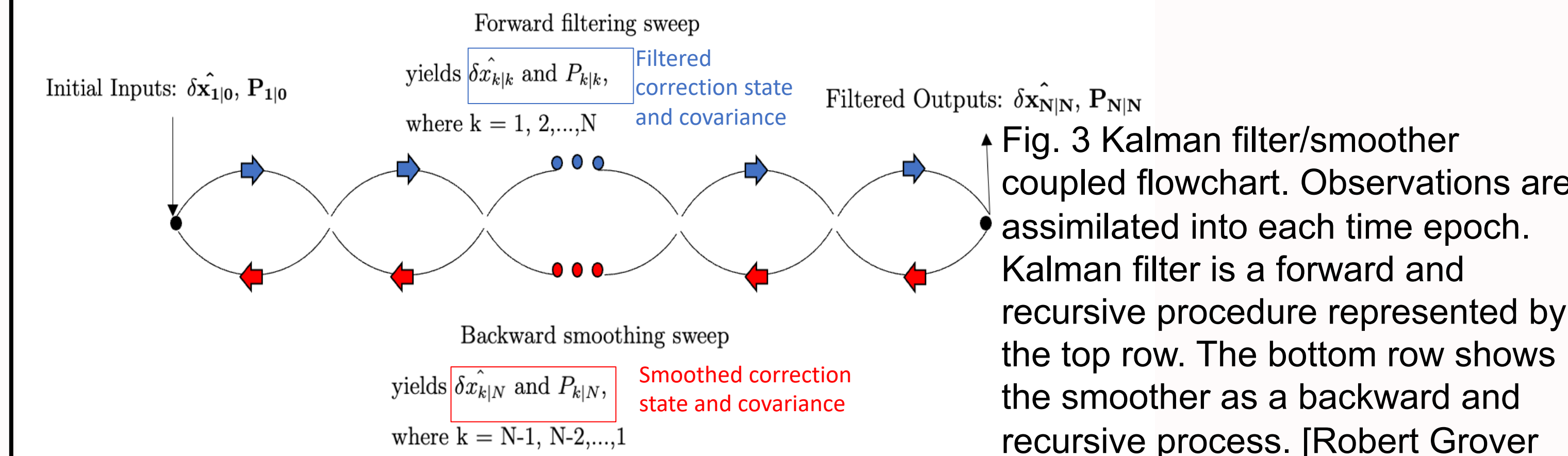


Fig. 3 Kalman filter/smoothing coupled flowchart. Observations are assimilated into each time epoch. Kalman filter is a forward and recursive procedure represented by the top row. The bottom row shows the smoother as a backward and recursive process. [Robert Grover Brown & Patrick Y.C, Hwang, 1983]

Advantages of adding Kalman smoother

- Refine estimates of previous states with all provided measurements
- Provides better analysis for a historical event (i.e., NILE)

Methodology

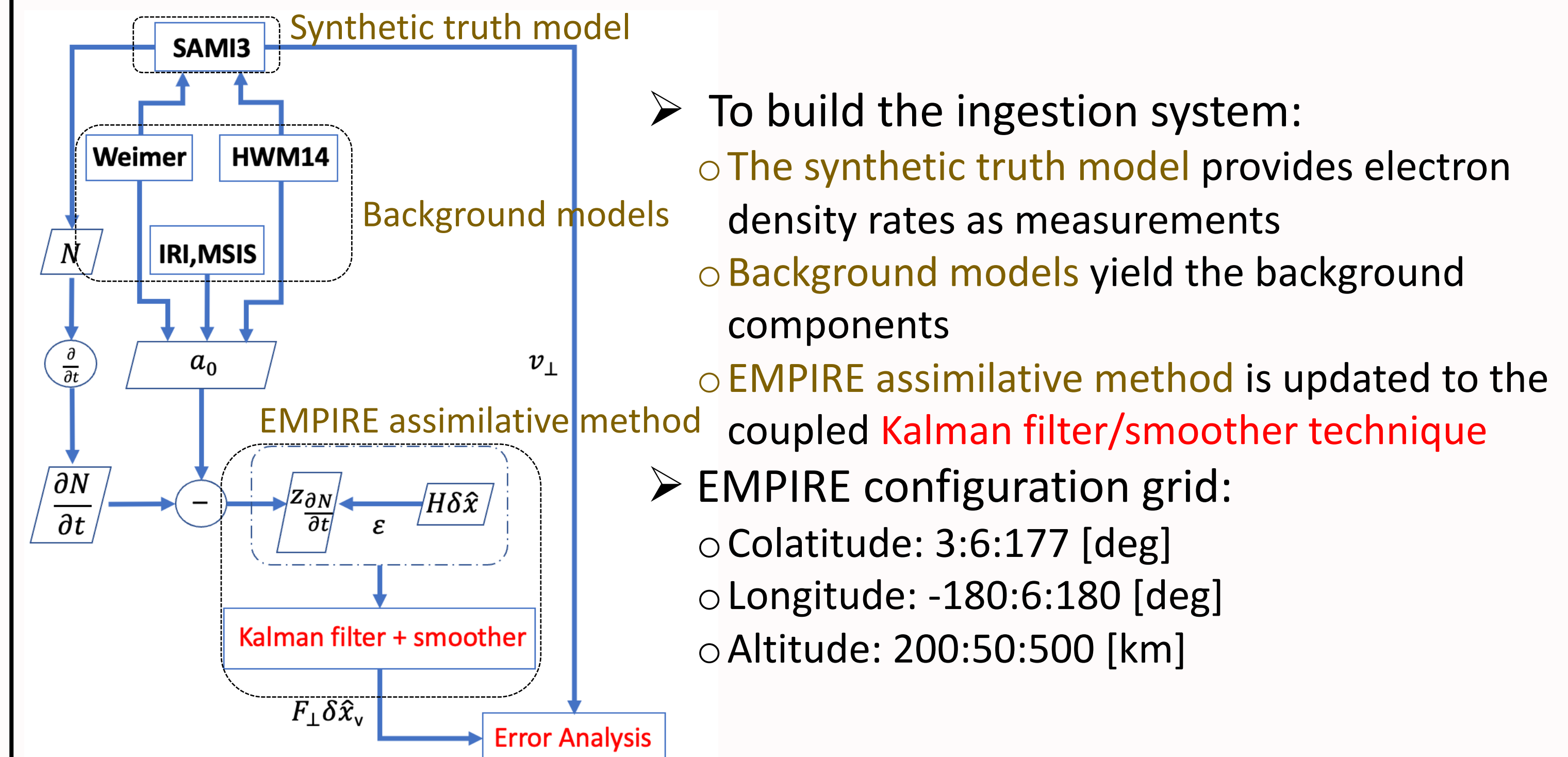


Fig. 4 EMPIRE experiment setup. Red text indicates the new implementation and brown text is connected to the terms in the ion continuity equation. H is the mapping matrix that map the correction state $\delta \hat{x}$ to the observation gap, with error ϵ . F_{\perp} is the mapping matrix map the correction state onto ion velocity space.

Evaluation time period characterization

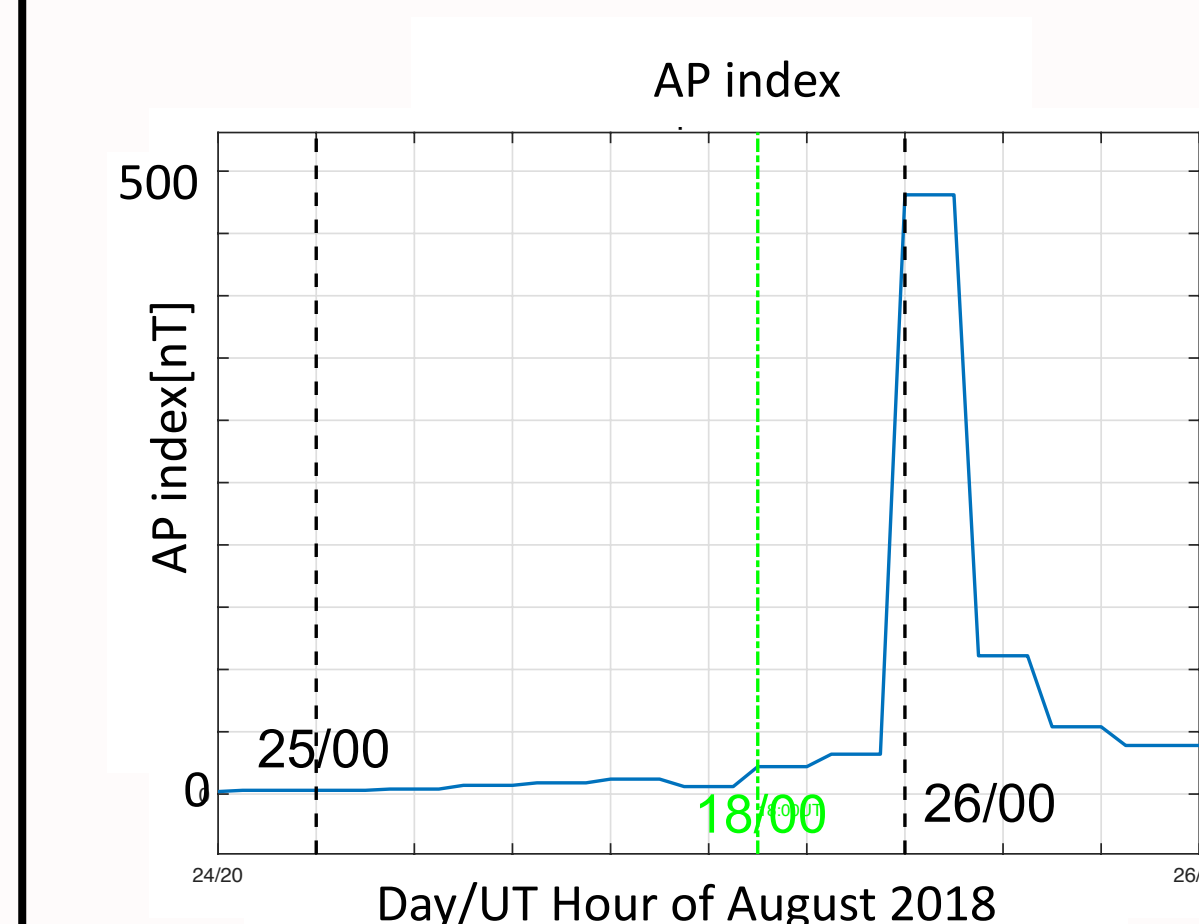


Fig. 5 Geomagnetic activity characterization for August 25th, 2018

Error analysis $\epsilon_{vi} = v_{\perp} - (F_{\perp} \delta x_v + v_{\perp,0})$

Zonal averaged error

$$\bar{\epsilon}_{v_i}(\theta; t) = \frac{1}{n_{\phi}} \sum_{\phi=-180}^{\phi=180} \epsilon_{v_i}(\theta, \phi; t)$$

Time-averaged error

$$\mu_{\epsilon_{v_i}}(\theta) = \frac{1}{n_{qtimes}} \sum_{t=0UT}^{t=18UT} \sum_{\phi=-180}^{\phi=180} \epsilon_{v_i}(\theta, \phi; t)$$

$$\sigma_{\epsilon_{v_i}}(\theta) = \left(\frac{1}{n_{qtimes}} \sum_{t=0UT}^{t=18UT} \sum_{\phi=-180}^{\phi=180} [\epsilon_{v_i}(\theta, \phi; t) - \mu_{\epsilon_{v_i}}(\theta)]^2 \right)^{1/2}$$

Result

Zonal averaged ion drift error

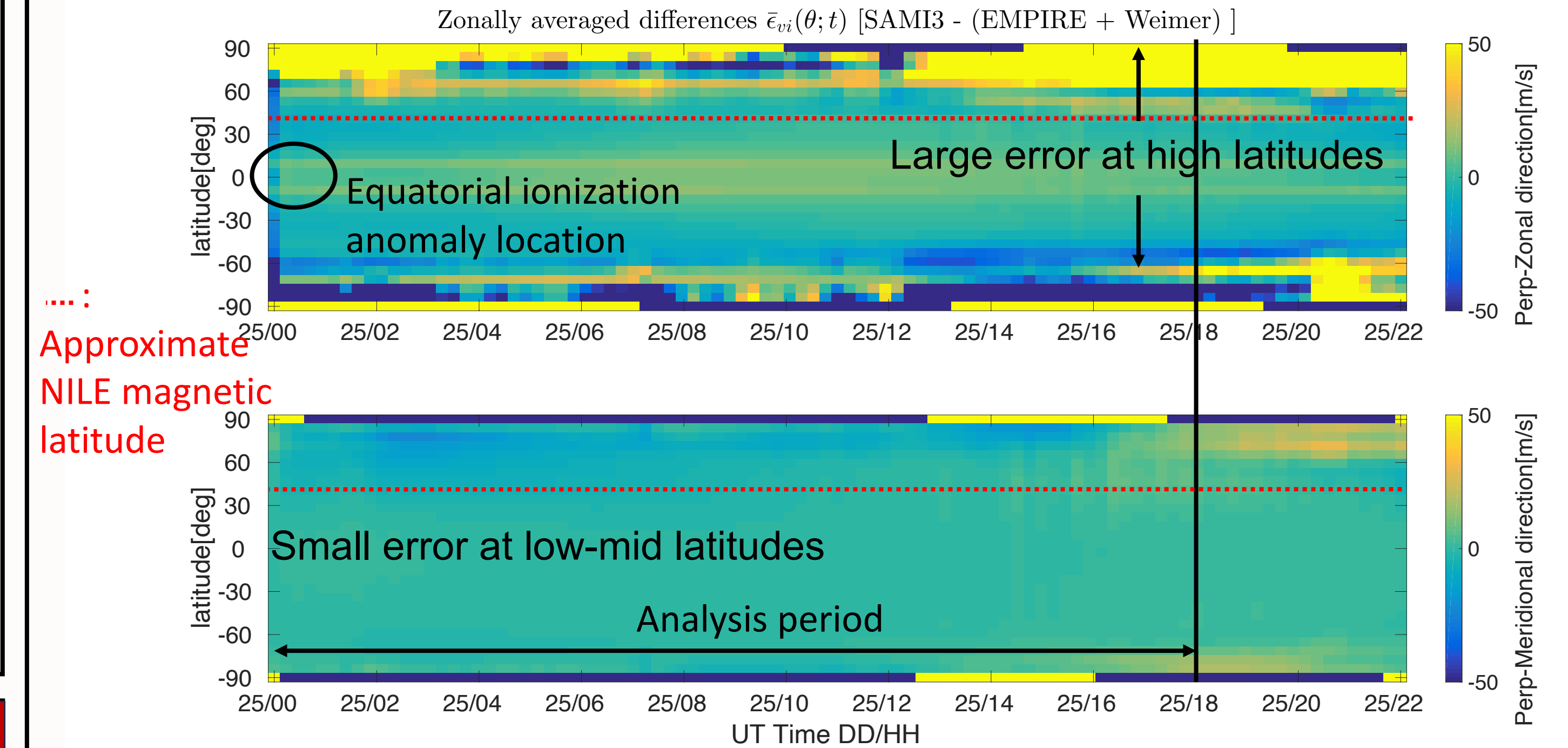


Fig. 6 Zonally averaged ion drift errors across evaluation time

Time averaged error

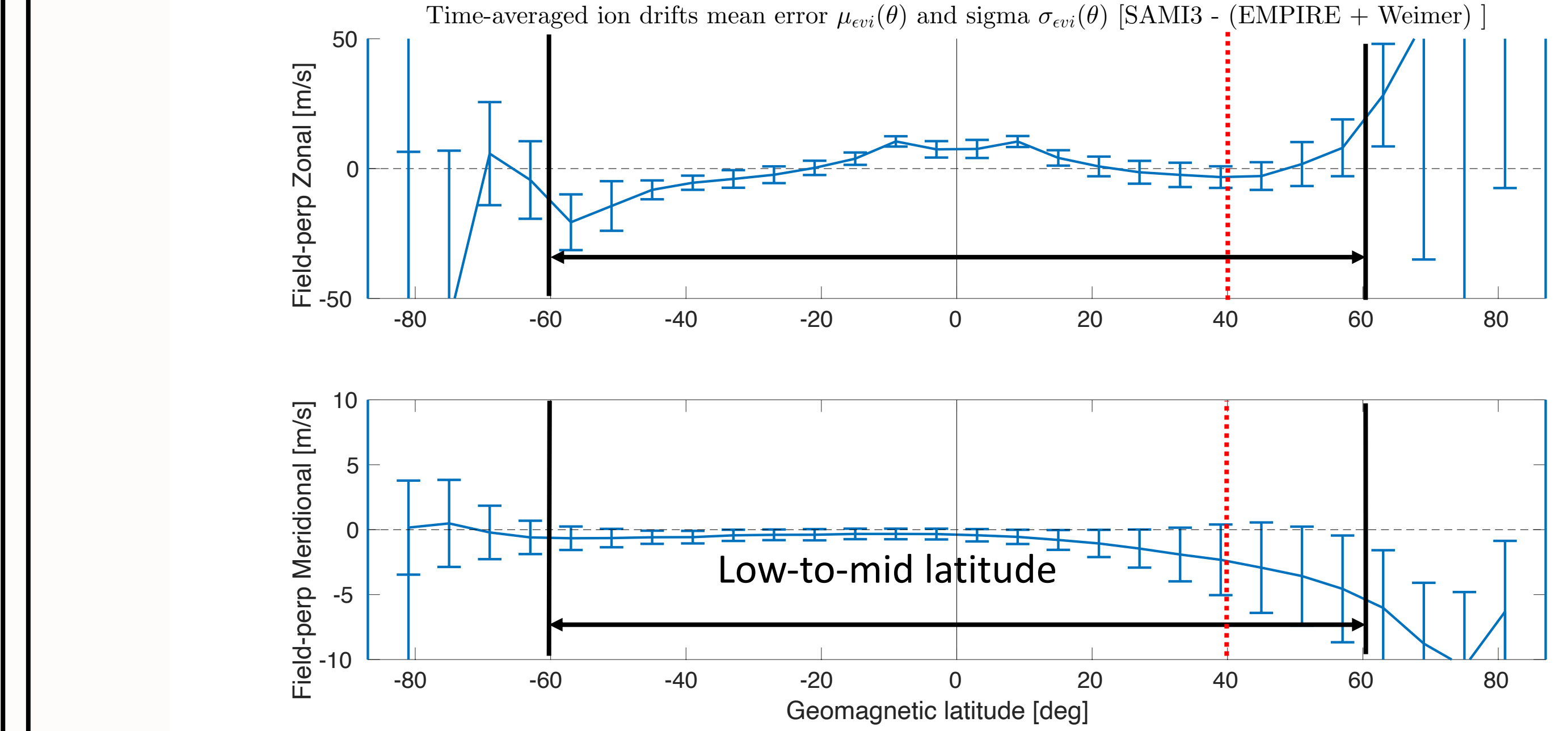


Fig. 7 Time-averaged ion drift mean errors and standard deviation

Conclusion & future work

- For the field-perp zonal direction ion drifts, significant errors are observed at high latitudes, with relatively large errors at the approximate equatorial ionization anomaly location ($\pm 25^{\circ}$ latitude).
- At the low-to-mid latitude band ($0^{\circ} - \pm 60^{\circ}$), the time averaged error is bounded within ± 5 [m/s] for field-perp meridional direction, ± 25 [m/s] for Field-perp zonal direction
- Future work:** Implement the Kalman filter/smoothing coupled technique to storm time and investigate the NILE phenomenon with the current knowledge on the ion drift error during the quiet time

Acknowledgement

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