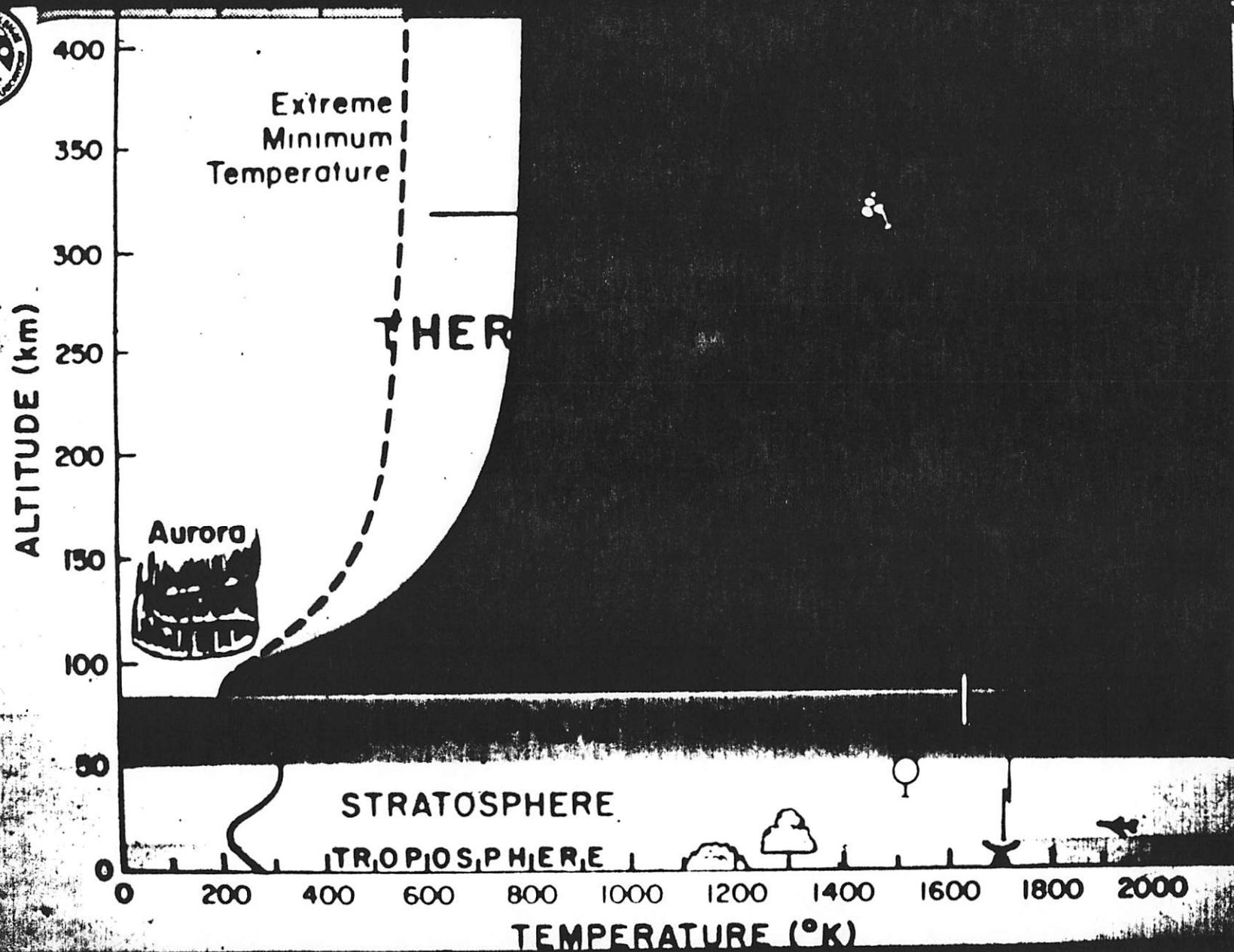


1992 CEDAR Workshop
Boulder, CO
June 21-26, 1992

Tutorial Lecture

by Raymond Roble
National Center for Atmospheric
Research

Overview of the
Thermosphere/Ionosphere General
Circulation Model (TIGCM)



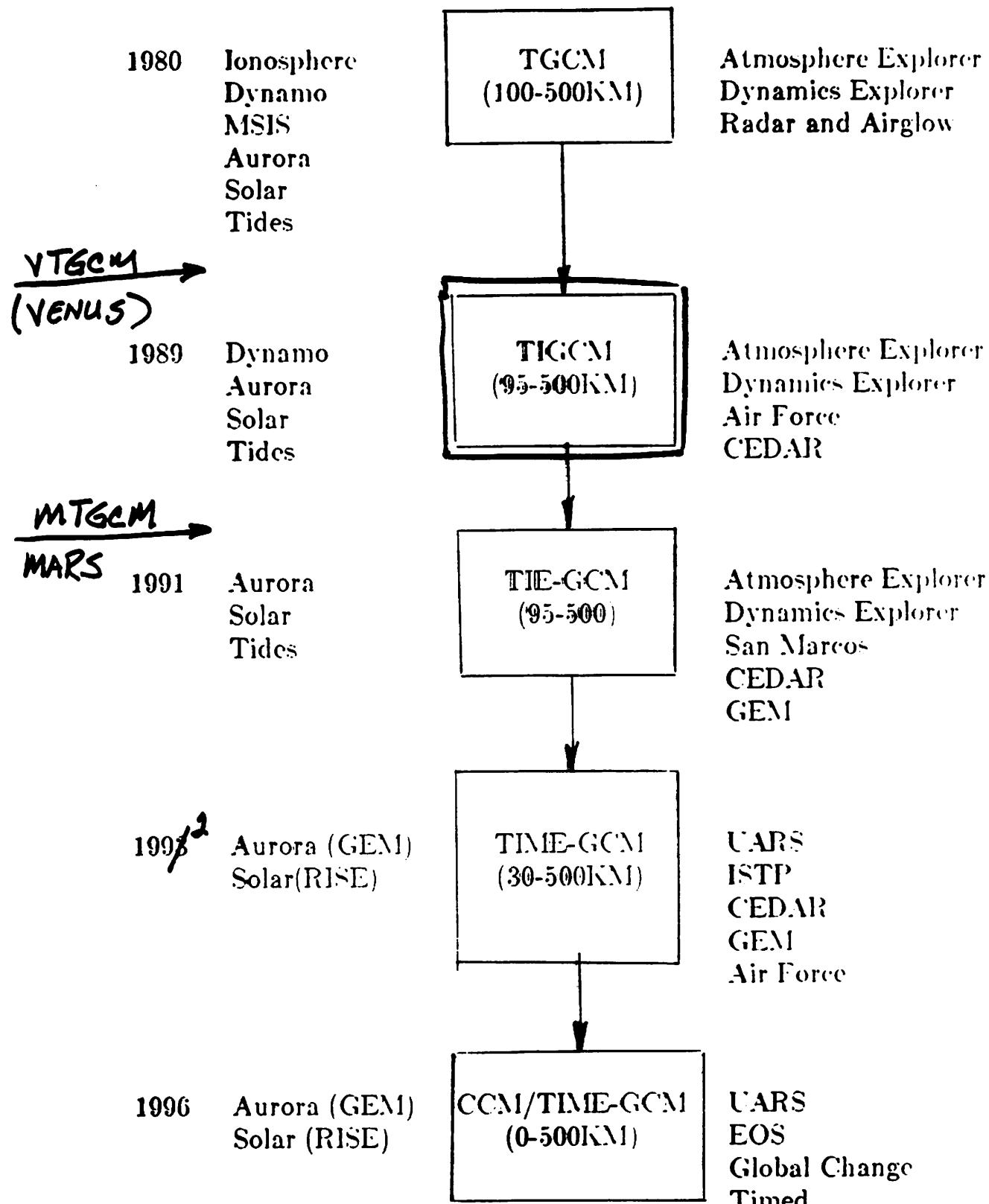
NCAR
THERMOSPHERE/IONOSPHERE
GENERAL CIRCULATION MODEL
(TIGCM)
(TGC M)

- Primitive equations of dynamic meteorology adapted to thermospheric heights
- Horizontal grid 5° latitude x 5° longitude, geographic
- Vertical grid -- 25 constant pressure surfaces, 2 grid points per scale height, 95 to 500 km
- Time step 240 or 300 S

INPUT

- Solar EUV and UV radiation 5 to 250 nm
- Empirical ionospheric convection and auroral particle precipitation models

LONG RANGE MODEL DEVELOPMENT



$$Z = -\ln \frac{P}{P_c}$$

THERMODYNAMIC EQUATION

$$P_0 = 5 \times 10^{-7} \text{ mb}$$

$\sim 25^\circ \text{ F.m.}$

$$\underline{\frac{\partial T}{\partial t}} = \frac{ge^z}{P_0 C_p} \frac{\partial}{\partial z} \left\{ \frac{K_T}{H} \frac{\partial T}{\partial z} + \frac{K_E H^2 C_p \rho}{P_r} \left(\frac{g}{C_p} + \frac{1}{H} \frac{\partial T}{\partial z} \right) \right\}$$

Molecular thermal
conduction

Eddy thermal
conduction

$$\underline{- \underline{V} \cdot \nabla T} - \underline{W} \left(\frac{\partial T}{\partial z} + \frac{RT}{C_p m} \right) + \underline{\frac{(Q-L)}{C_p}}$$

horizontal
advection

vertical advection
and adiabatic
expansion

heat sources and
radiative losses

Upper Boundary Conditions

No heat source or heat
sink at upper boundary

$$\frac{\partial T}{\partial z} = 0$$

Lower Boundary Conditions

Temperature specified

$$T = T_s (z = -7)$$

THE EASTWARD MOMENTUM EQUATION

$$\begin{aligned}
 \frac{\partial u}{\partial t} = & \frac{ge^z}{P_0} \frac{\partial}{\partial z} \left(\frac{\mu}{H} \frac{\partial u}{\partial z} \right) + \left(f + \frac{u}{r} \tan \phi - \lambda_{xy} \right) v \\
 -\lambda_{xz} u - \nabla \cdot \nabla u - w \frac{\partial u}{\partial z} - \frac{1}{r \cos \phi} \frac{\partial \Phi'}{\partial \lambda} + (F_\lambda + \lambda_{zy} v_I + \lambda_{xz} u_I)
 \end{aligned}$$

THE NORTHWARD MOMENTUM EQUATION

$$\begin{aligned}
 \frac{\partial v}{\partial t} = & \frac{ge^z}{P_0} \frac{\partial}{\partial z} \left(\frac{\mu}{H} \frac{\partial v}{\partial z} \right) - \left(f + \frac{u}{r} \tan \phi - \lambda_{yx} \right) u \\
 -\lambda_{yy} v - \nabla \cdot \nabla v - w \frac{\partial v}{\partial z} - \frac{1}{r} \frac{\partial \Phi'}{\partial \phi} + (F_\phi + \lambda_{yy} v_I - \lambda_{yx} u_I)
 \end{aligned}$$

THE CONTINUITY EQUATION

$$\frac{1}{r \cos \phi} \frac{\partial}{\partial \phi} (v \cos \phi) + \frac{1}{r \cos \phi} \frac{\partial u}{\partial \lambda} + e^z \frac{\partial}{\partial z} (e^{-z} w) = 0$$

THE HYDROSTATIC EQUATION

$$\frac{\partial \Phi}{\partial z} = \frac{RT}{m}$$

Upper Boundary Conditions

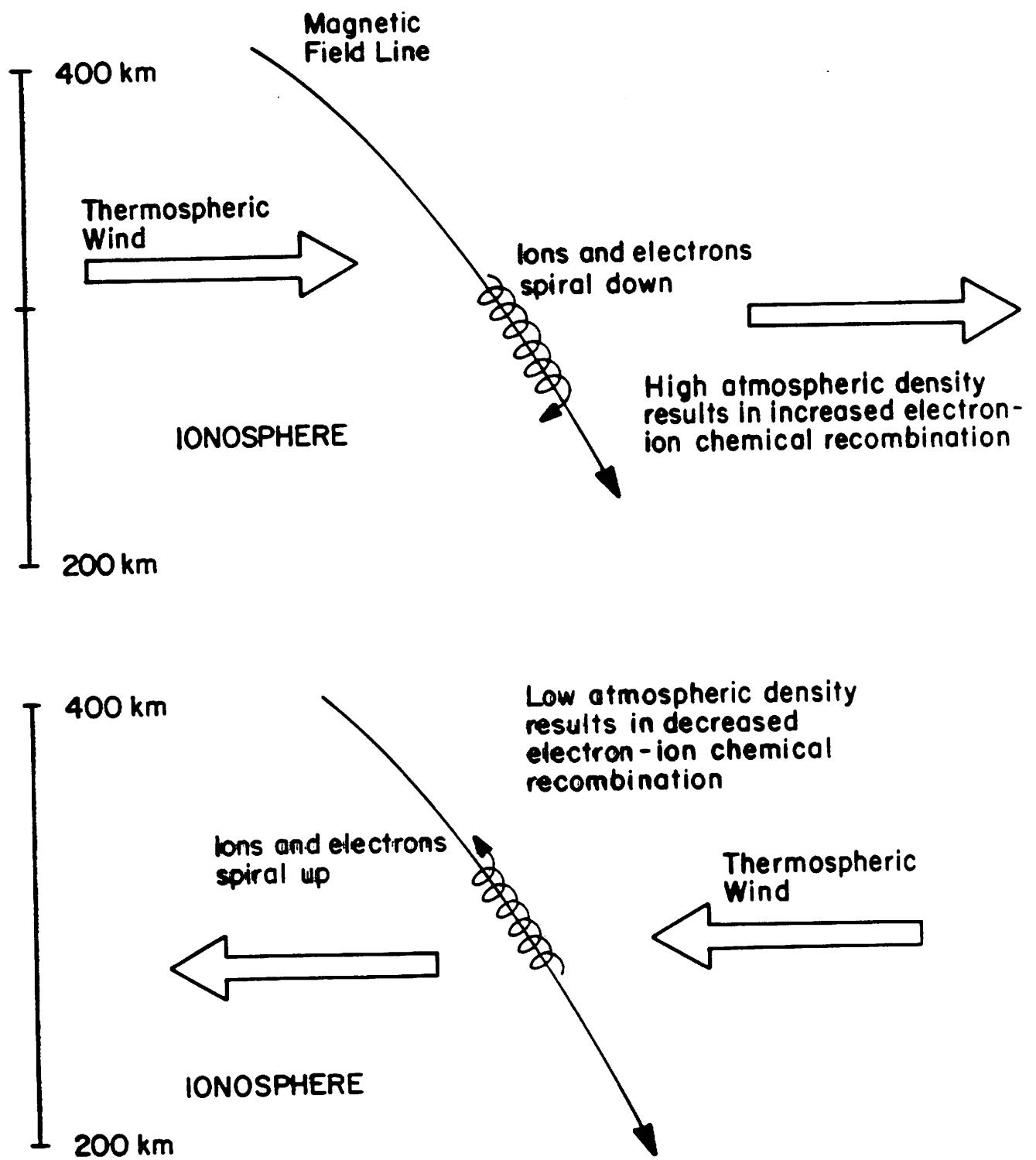
No sources of momentum at upper boundary

$$\frac{\partial u}{\partial z} = \frac{\partial v}{\partial z} = \frac{\partial w}{\partial z} = 0$$

Lower Boundary Conditions

Specified

$$\begin{aligned}
 U &= U_s (z = -7) \\
 V &= V_s (z = -7) \\
 \Phi &= \Phi_s (z = -7)
 \end{aligned}$$



ION DRAG PARAMETERS

$$\lambda_{xx} = \lambda_1 (1 - \sin^2 \delta \cos^2 I)$$

$$\lambda_{yy} = \lambda_1 (1 - \cos^2 \delta \cos^2 I)$$

$$\lambda_{xy} = + \lambda_1 \sin \delta \cos \delta \cos^2 I + \lambda_2 \sin I$$

$$\lambda_{yx} = + \lambda_1 \sin \delta \cos \delta \cos^2 I + \lambda_2 \sin I$$

where δ is the magnetic declination angle, I is the magnetic dip angle and

$$\lambda_1 = \frac{\sigma_P B^2}{\rho} \quad \lambda_2 = \frac{\sigma_H B^2}{\rho}$$

where σ_P and σ_H are the Pedersen and Hall electrical conductivity, respectively, B is the strength of the magnetic field $= 0.282 \sqrt{1 + 3 \cdot \cos^2 \phi_m}$ Gauss, ϕ_M is the magnetic colatitude, and ρ is the TGCM density.

JOULE HEATING

The Joule heating for displaced poles is

$$Q_J = \underline{\lambda_{xx} (U_I - U_n)^2} + \underline{\lambda_{yy} (V_i - V_n)^2} + (\lambda_{xy} - \lambda_{yx}) \cancel{(U_i - U_n)} \cancel{(V_i - V_n)}$$

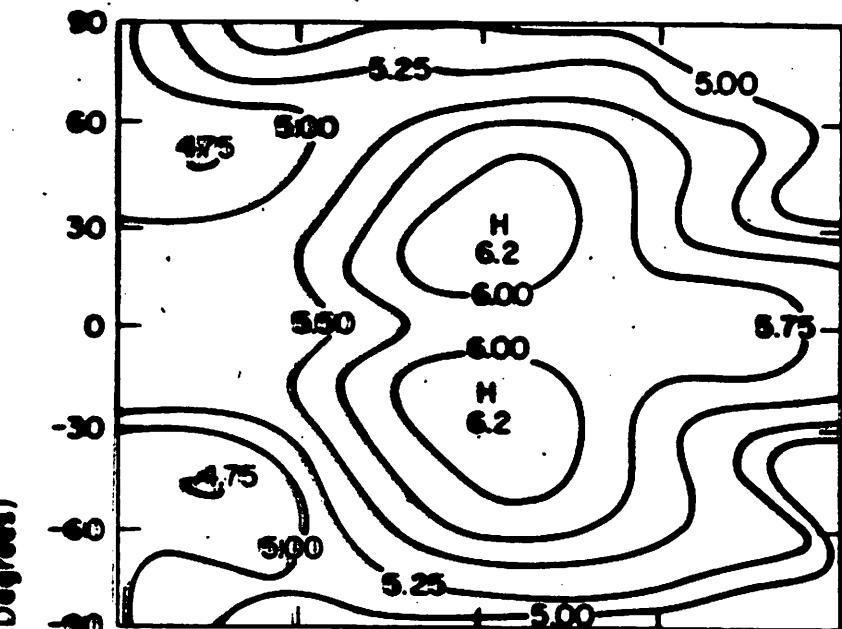
where U_i and V_i are the geographic zonal and meridional ion drift velocities defined by the Heelis *et al.* (1982) empirical model and U_n and V_n are the zonal and meridional neutral wind components determined at a given time step in the TGCM.

EMPIRICAL ELECTRON DENSITY MODEL (CHIU, 1975)

$$\log_{10} (\text{Ne}, \text{cm}^{-3})$$

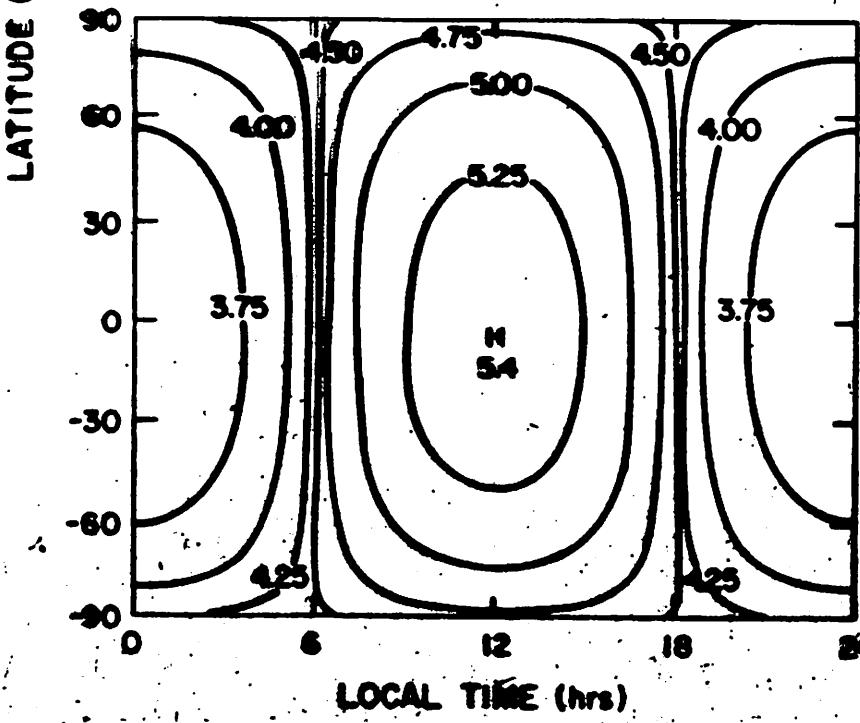
EQUINOX $F_{10.7} \sim 150$

300 KM



a

120 KM

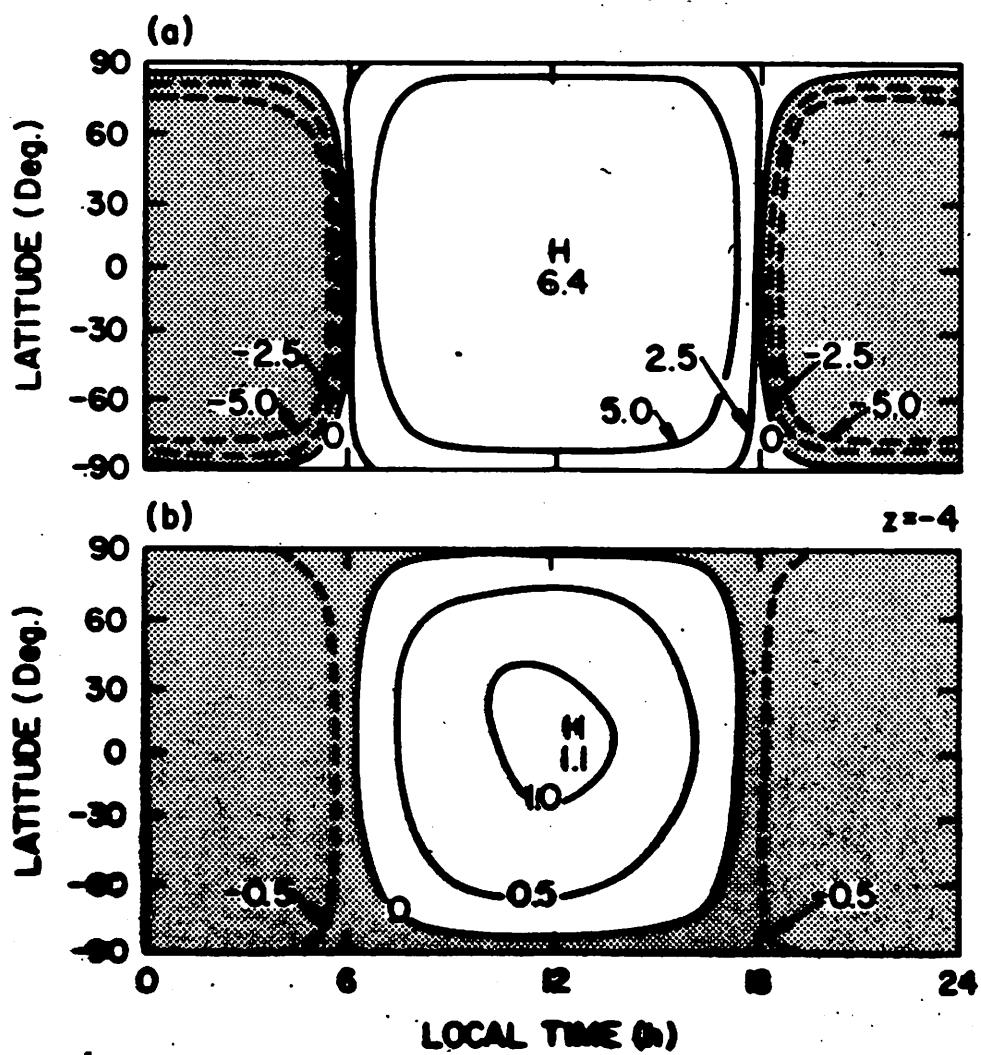


b

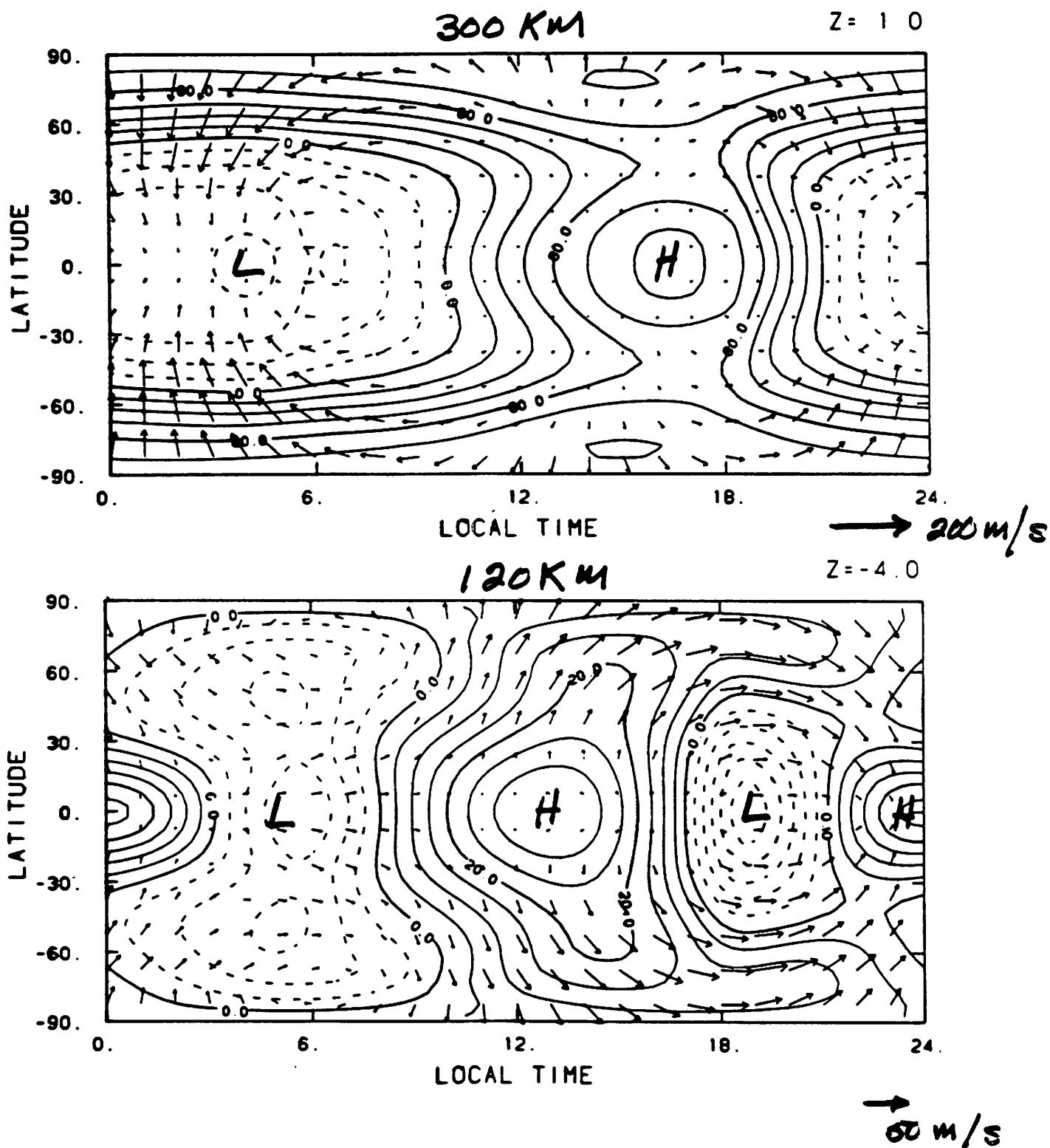
PRESCRIBED SOLAR HEATING (ϵ)

$$\log_{10} (Q, \text{ERGS GM}^{-1} \text{s}^{-1})$$

EQUINOX $F_{10.7} \sim 150$



PERTURBATION TEMPERATURE (ΔT , K)
 VECTORS OF NEUTRAL WIND (m/s)



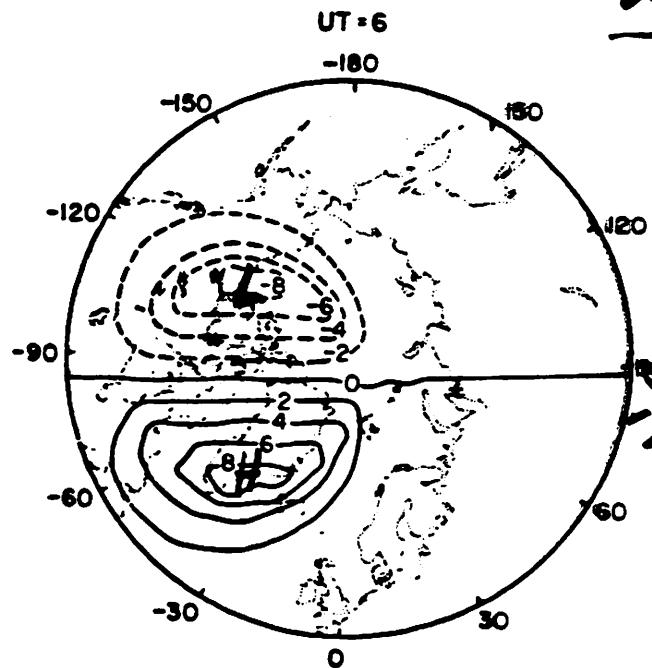
EQUINOX $F_{10.7} = 150$

SOLAR HEATING ONLY

IONOSPHERIC

POTENTIAL (VOLTS)

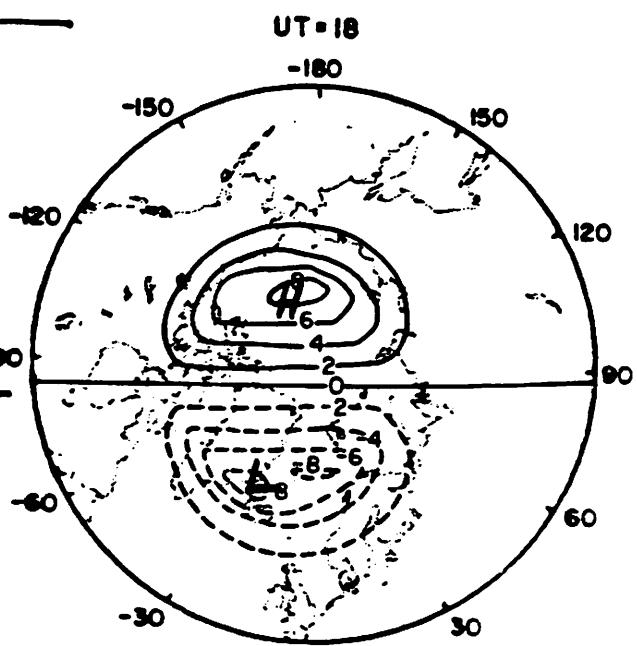
20KV



(a)

LONGITUDE

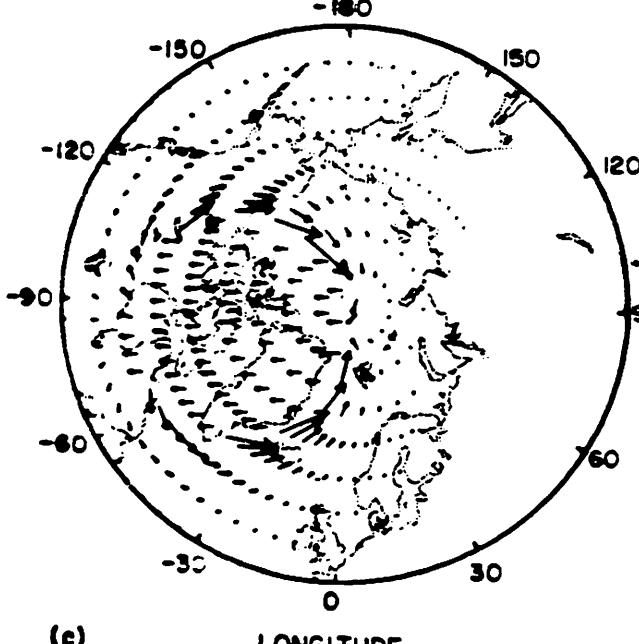
UT = 6



(b)

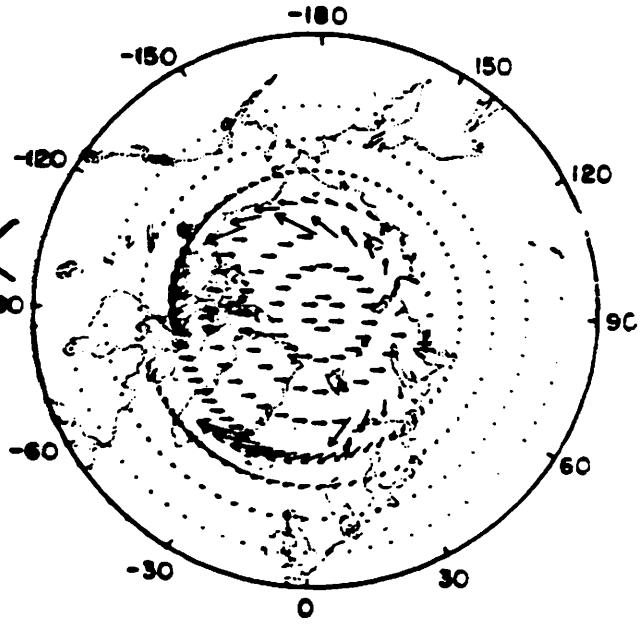
LONGITUDE

UT = 18



(c)

LONGITUDE



(d)

LONGITUDE

ION

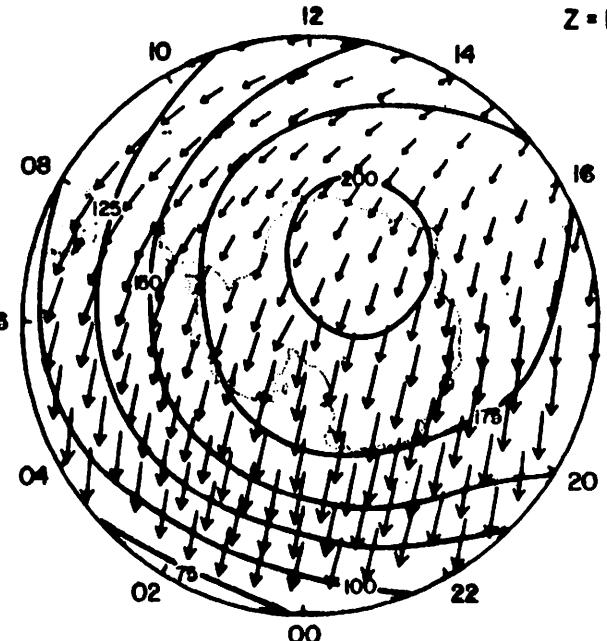
DRIFT

\rightarrow
500 m/s

M (MOMENTUM)

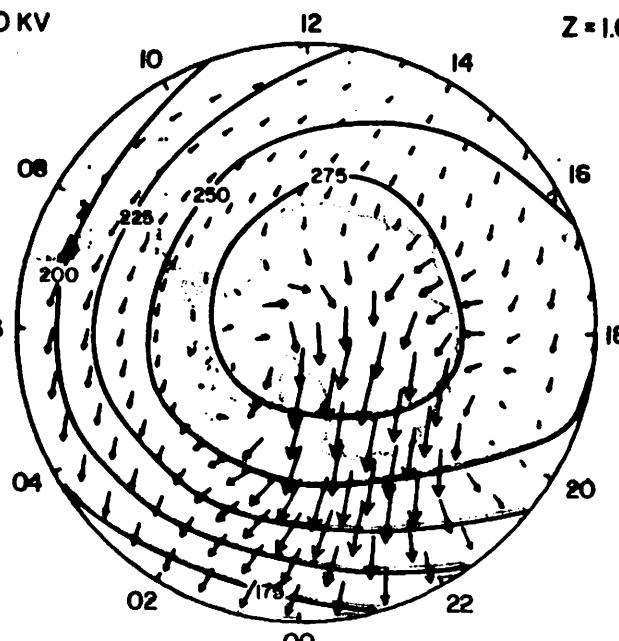
Q_J (JOULE)

SOLAR ONLY



(a)

$Z = 1.0$ 20 KV



20 KV

$Z = 1.0$

$\Delta T \sim 275 K$
 $V \sim 200 m/s$

LOCAL TIME

60 KV (b)

60 KV

LOCAL TIME

$Z = 1.0$

$\Delta T \sim 450 K$
 $V \sim 400 m/s$

EQUINOX

300 KM

(c)

LOCAL TIME

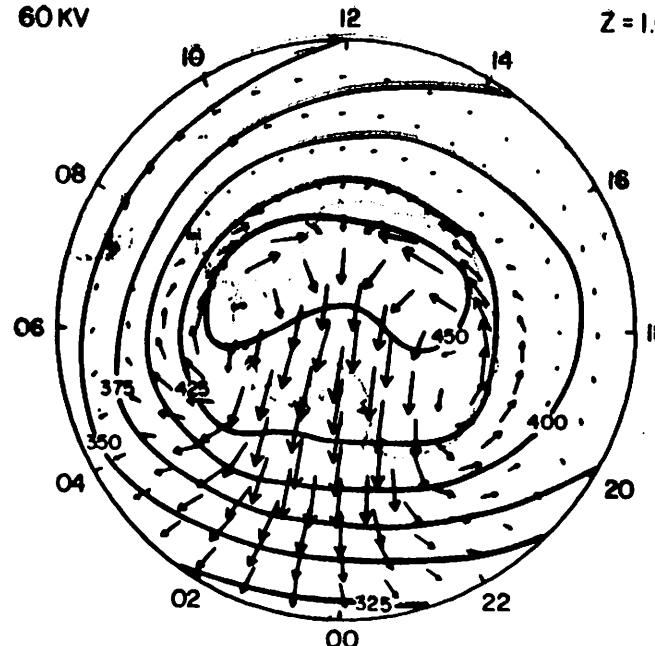


Figure 2

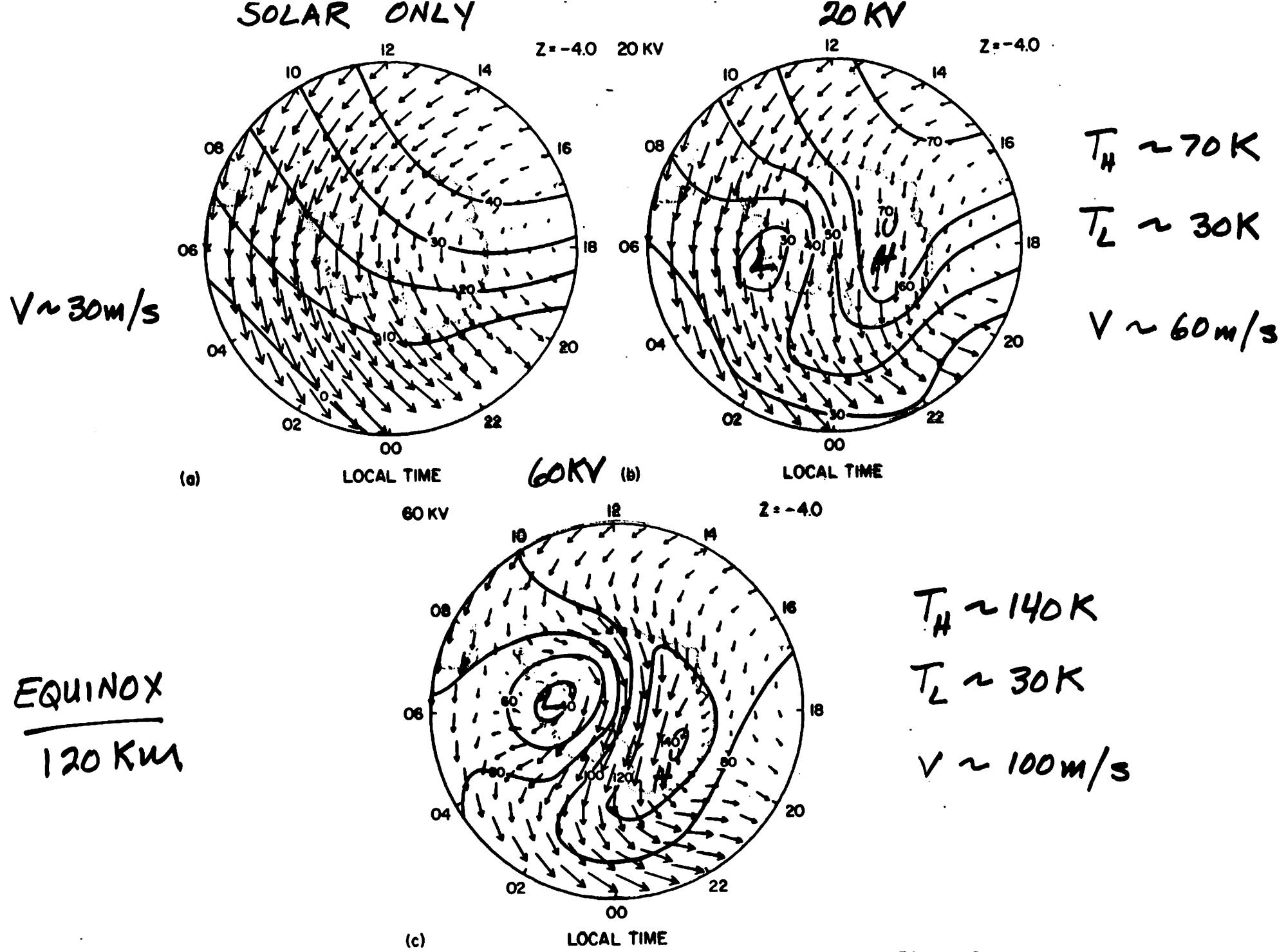


Figure 3

day=83021

TIGCM Neutral Temperature (deg K)

UT = 5.0 ZP = 2.0

de2 orbit=8121(S)

12

1.32e+03

6

18

1.14e+03

500 m/s

0

Local Time (hrs)

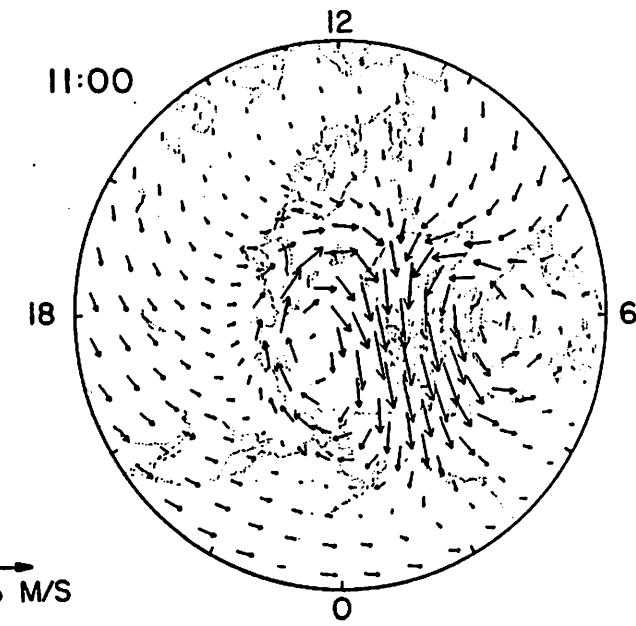
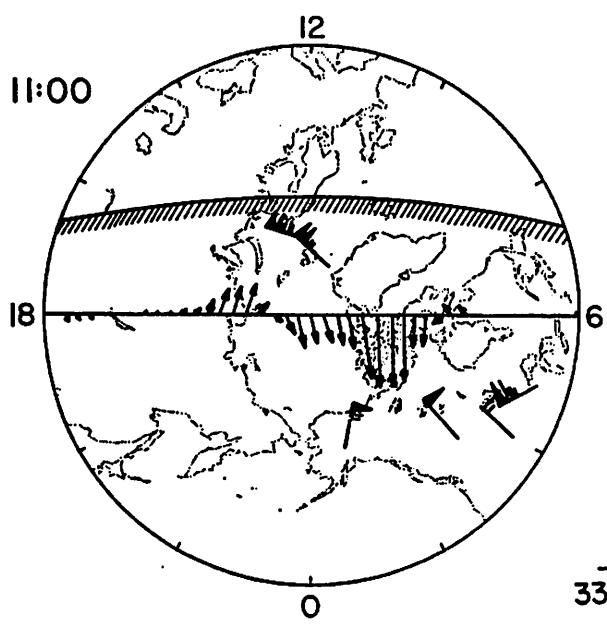
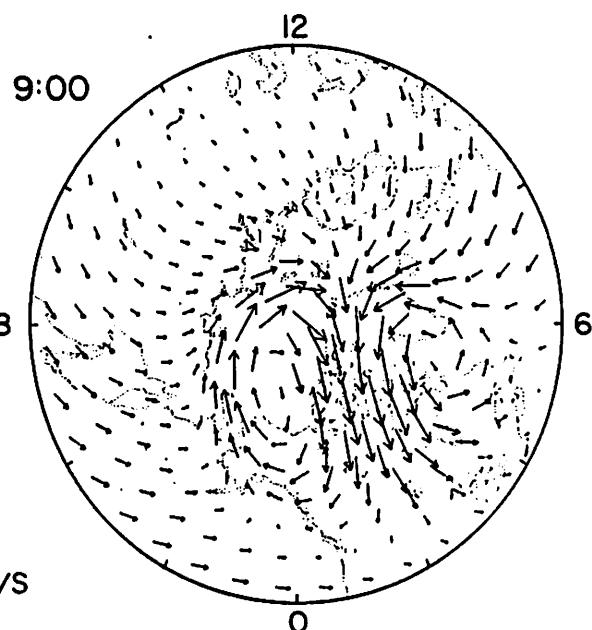
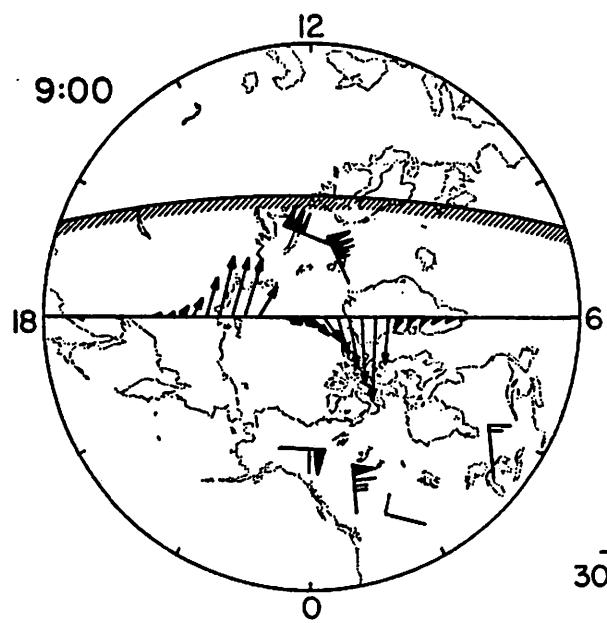
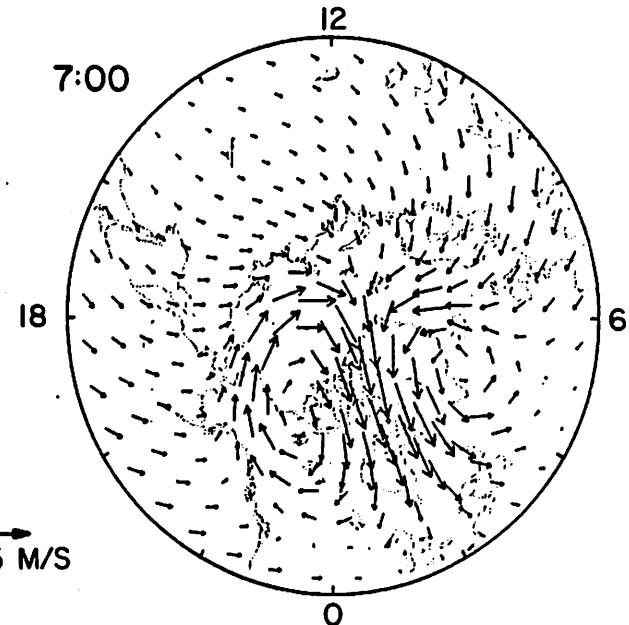
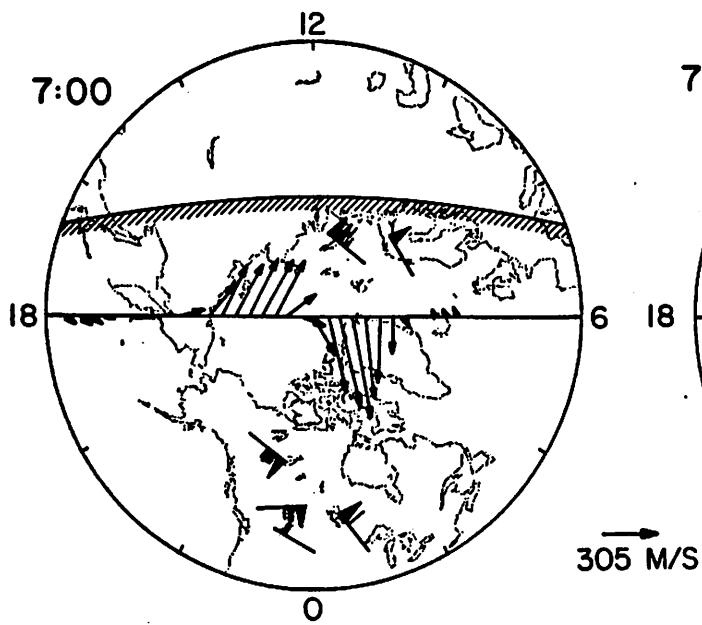
History=ROBLE/RGR89/JADE09

Perimeter latitude=-37.5 deg

9.60e+02

DE-2 / GBFPI
AVERAGE NEUTRAL WINDS
DEC 1981

NCAR / TGCM
MODEL PREDICTIONS

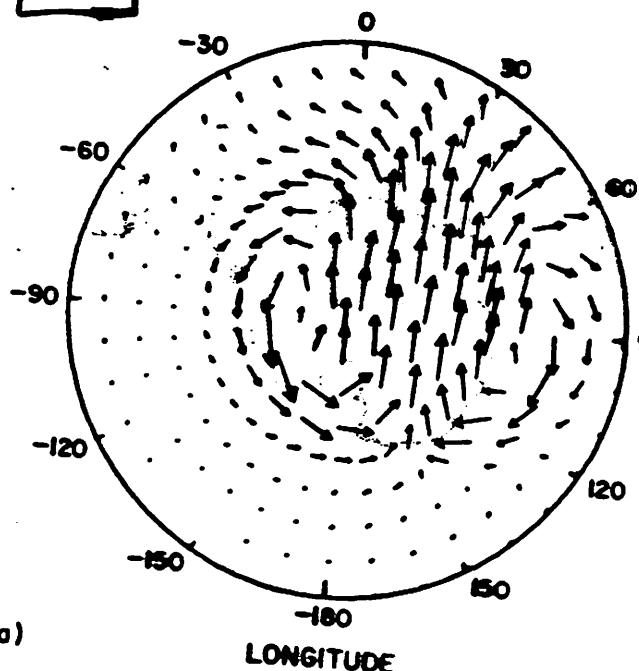


60 KV · EQUINOX

$$V \sim 400 \text{ m s}^{-1}$$

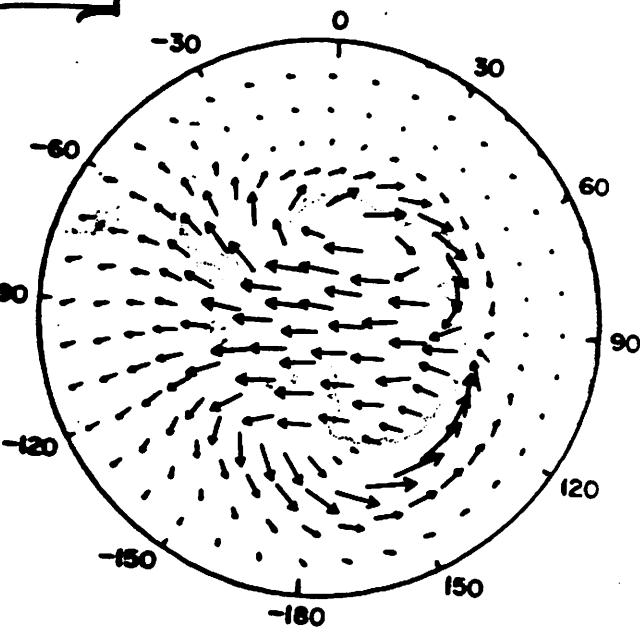
300 KM

UT = 0

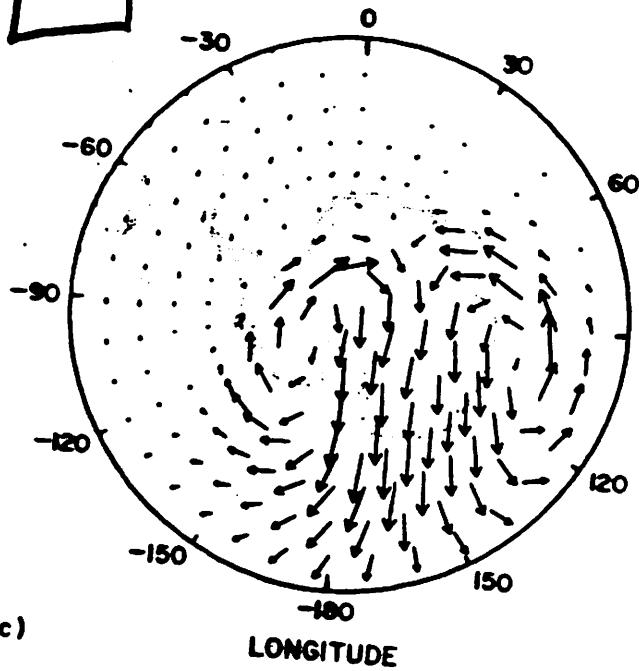


(a)

UT = 6

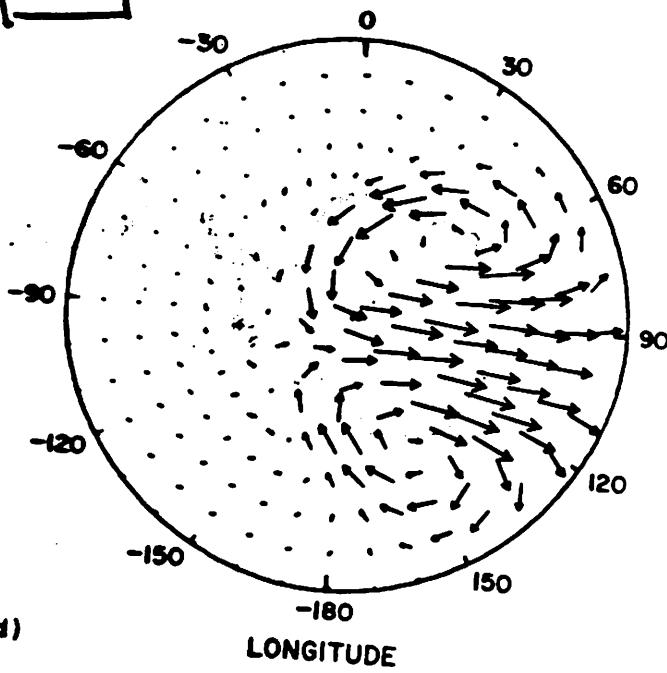


UT = 12



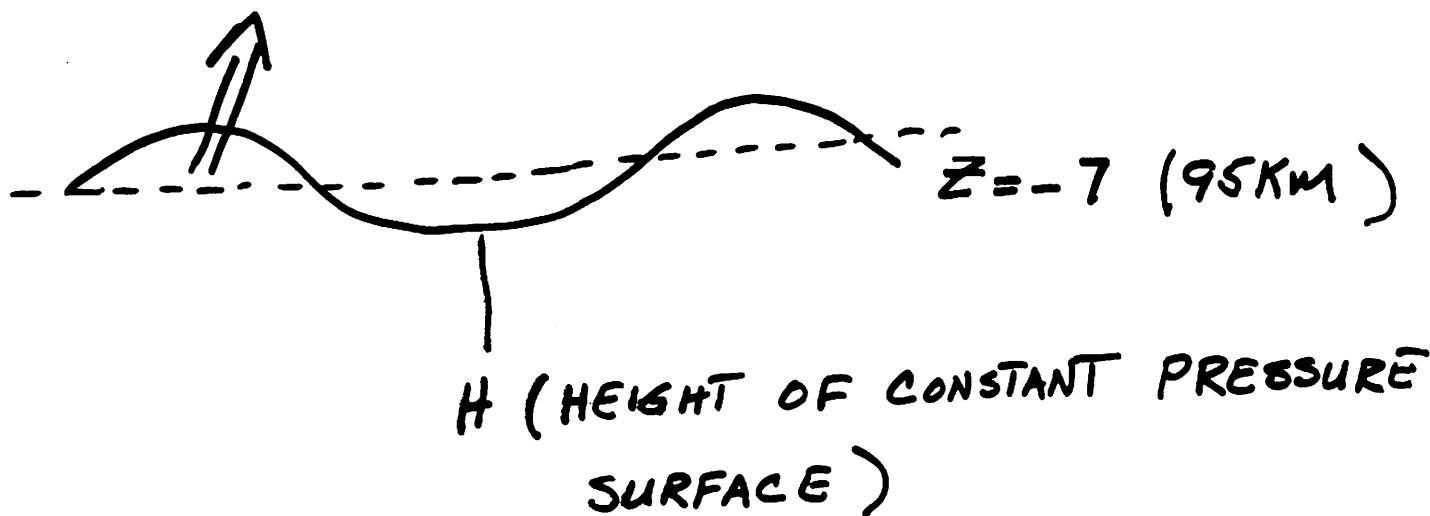
(c)

UT = 18



(d)

TIDAL FORCINGS (FESEN et.al. 1986)



Φ_2 (97 km)

HOUGH FUNCTIONS (SEMI-DIURNAL)

2-2
2-3
2-4
2-5
2-6 } SPECIFY AMPLITUDES
AND PHASES
FORBES & VIAL (1991)
LTCS - STUDIES

RECENTLY ADDED DIURNAL TIDE

(FORBES ET AL. 1992)

MAJOR CONSTITUENT TRANSPORT

The three major neutral constituents of the thermosphere - O_2 , O , and N_2 - are considered and used to define the mass mixing ratio of constituent i as

$$\psi_i = n_i m_i \left(\sum_{j=1}^3 n_j m_j \right)^{-1},$$

where n_i is the number density of the i th species, with $i = 1, 2$ and 3 corresponding, respectively, to O_2 , O , and N_2 ; m_i is the mass of the i th species. We furthermore define mixing ratios of O_2 and O as the vector

$$\underline{\psi} = \begin{pmatrix} \psi_{O_2} \\ \psi_O \end{pmatrix}$$

and therefore by definition the N_2 mixing ratio is obtained by $\psi_{N_2} = 1 - \psi_{O_2} - \psi_O$.

$$\frac{\partial}{\partial t} \underline{\psi} = -e^z r^{-1} \frac{\partial}{\partial z} \left[\frac{\bar{m}}{m_{N_2}} \left(\frac{T_\infty}{T} \right)^{0.25} \underline{\alpha}^{-1} L \underline{\psi} \right]_{\substack{\text{MOLECULAR} \\ \text{EDDY}}} + e^z \frac{\partial}{\partial z} \left(K(z) e^{-z} \left(\frac{\partial}{\partial z} \underline{\psi} + \frac{1}{\bar{m}} \frac{\partial \bar{m}}{\partial z} \right) \right)_{\substack{\text{DIFFUSION} \\ \text{EDDY}}} - \left(\underline{V} \cdot \nabla \underline{\psi} + w \frac{\partial}{\partial z} \underline{\psi} \right)_{\substack{[\text{HOR.} + \text{VER.}] \text{ ADV} \\ \text{SOURC.} + \text{SAK}}} + \underline{S} - \underline{R}.$$

Upper Boundary Conditions

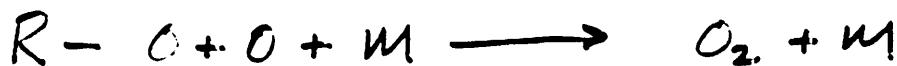
At the upper boundary condition, diffusive equilibrium is assumed so that $L \underline{\psi} = 0$.

Lower Boundary Conditions

At the lower boundary, we utilize the observation that the atomic oxygen concentration $n(O)$ peaks near 97 km and assume that $\partial n(O)/\partial z = 0$. This assumption and conservation of total oxygen atoms implies

$$\frac{\partial}{\partial z} \psi_2 = \psi_2 \quad \psi_1 + \psi_2 = \text{constant}$$

S - PHOTODISSOCIATION (EUV + SRC)

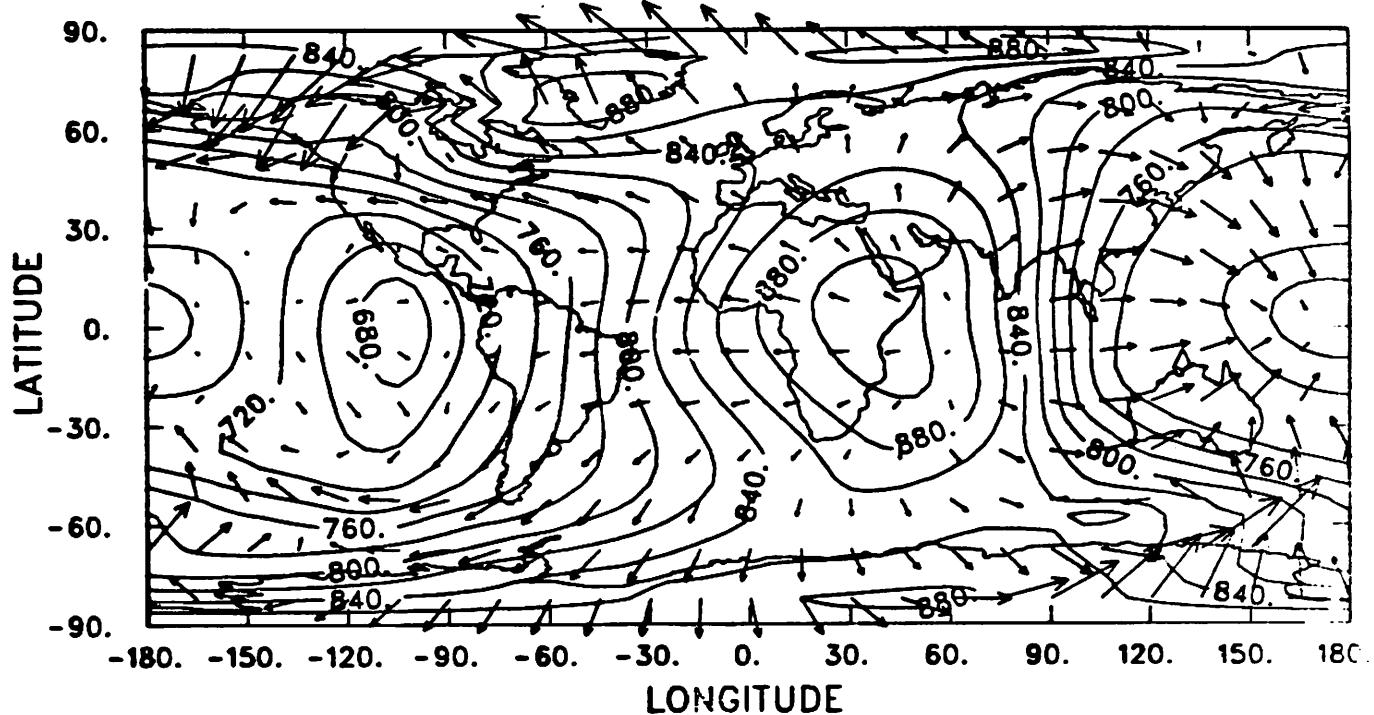


EQUINOX - SOLAR MINIMUM
EARTH

UT = 12.00

300 KM

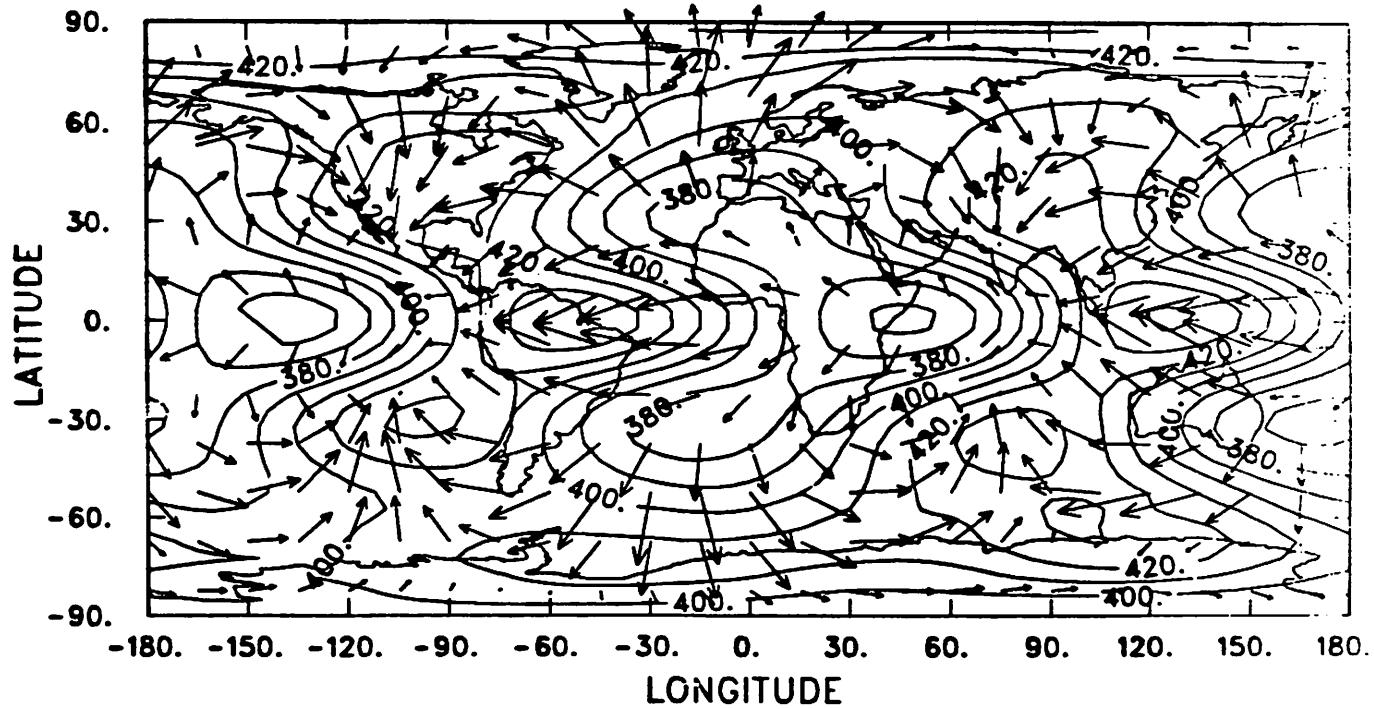
Z = 2.0



UT = 12.00

120 KM

Z = -4.0



100 M/S

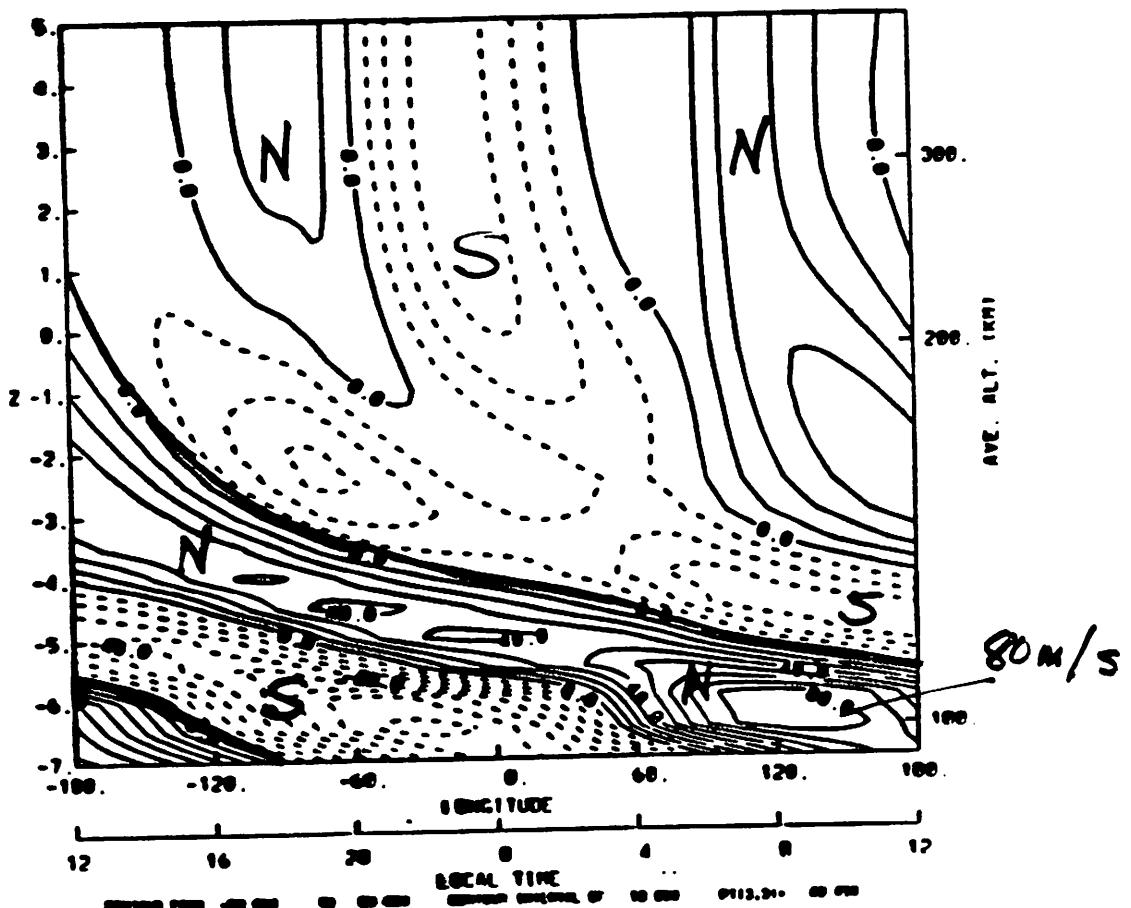
M/S

M/S

MERIDIONAL WIND (M/S) _{17.5N}

FIELD = V

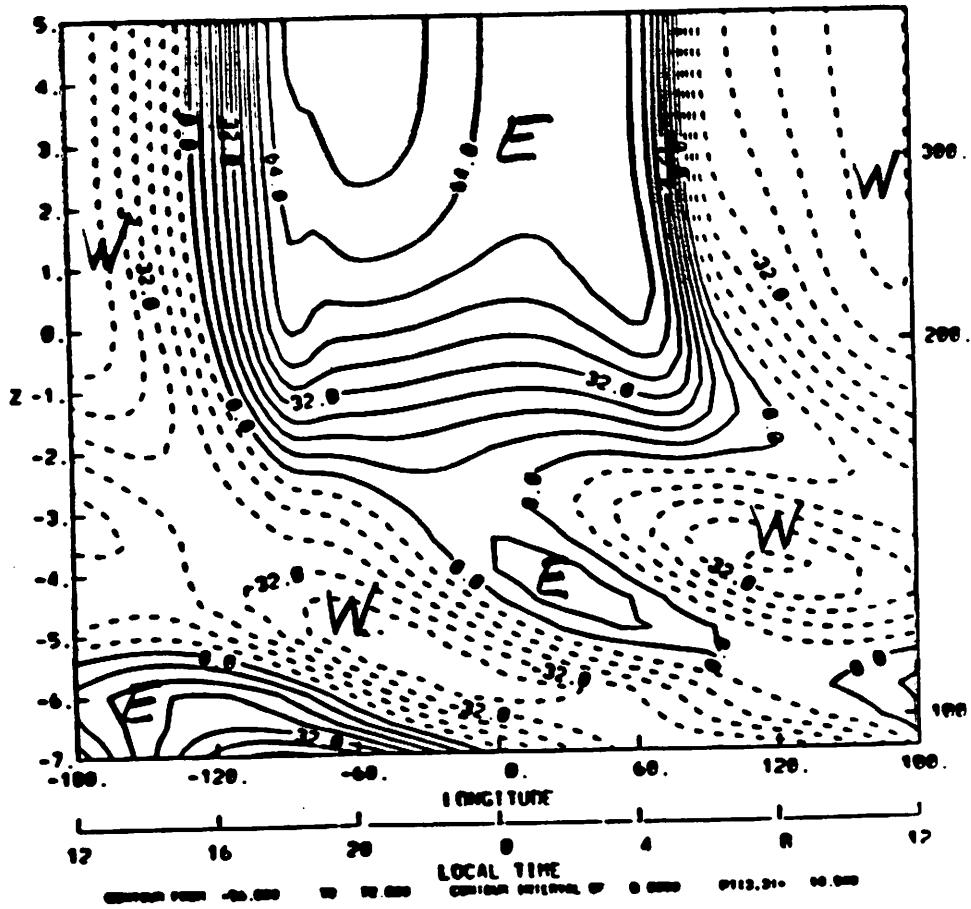
$\Delta \approx 10 \text{ m/s}$



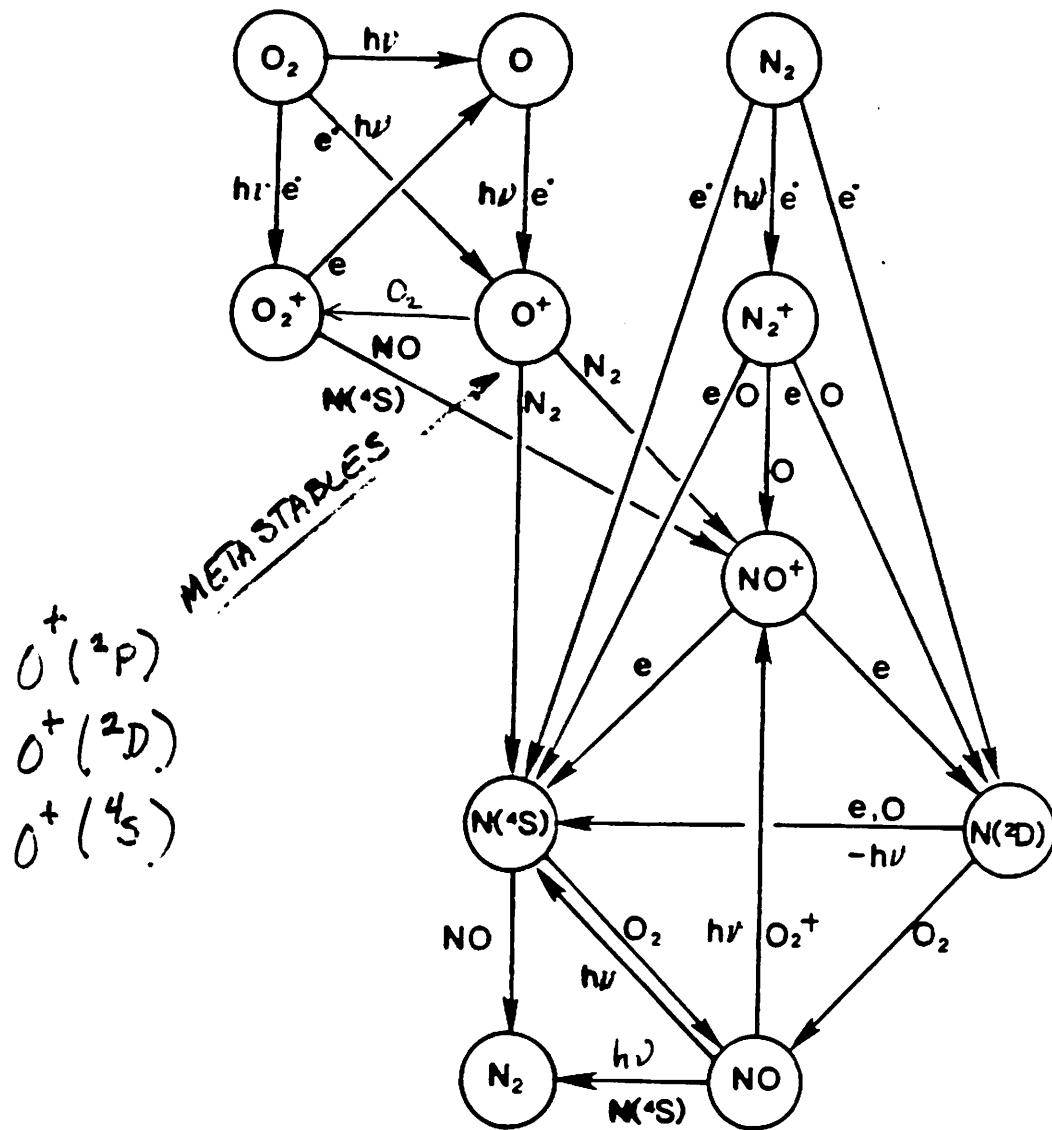
ZONAL WIND (M/S)

FIELD = U

$\Delta \approx 8 \text{ m/s}$



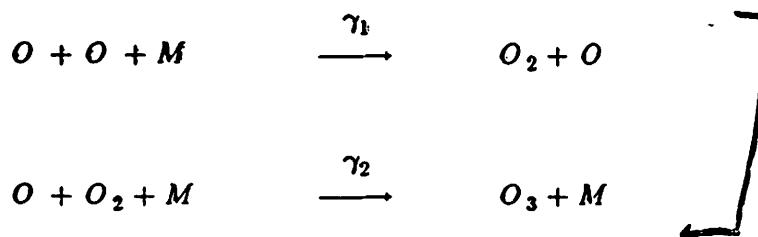
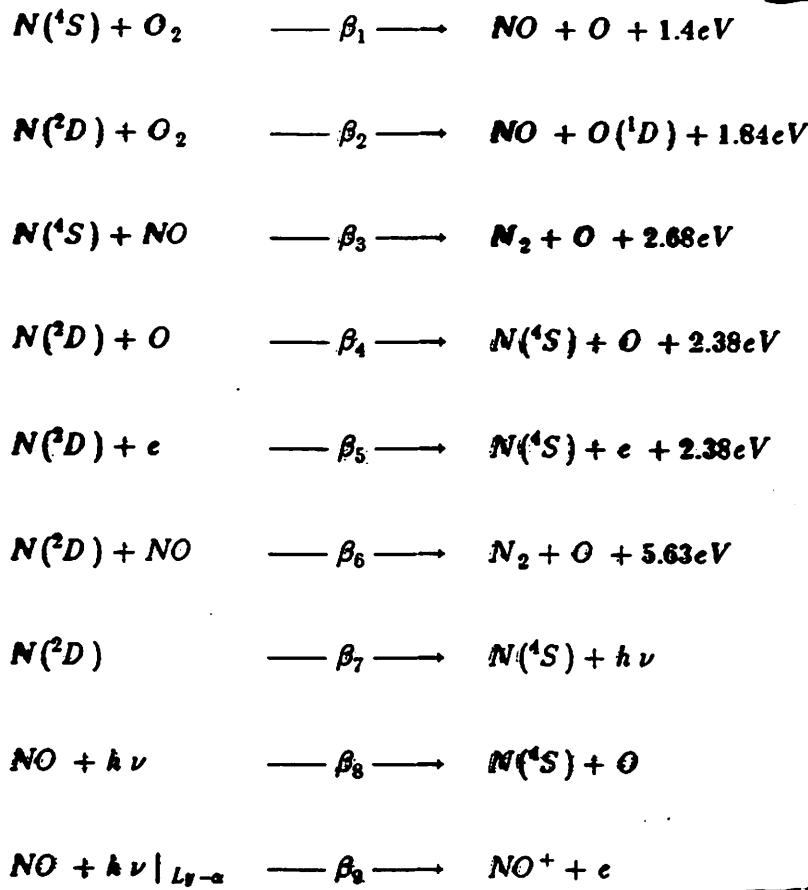
TIGCM CHEMISTRY



TIGCM

Neutral-Neutral Constituent Reactions and Rates used in the Model.

Reactions



MINOR CONSTITUENT TRANSPORT

$$\underline{\frac{\partial \psi_m}{\partial t}} = e^{-z} \frac{\partial}{\partial z} D_m \left(\frac{\partial}{\partial z} - E_m \right) \psi_m$$

Molecular and Thermal Diffusion

$$- \left[\underline{V \cdot \nabla} + \omega \frac{\partial}{\partial z} \right] \psi_m + S_m + e^z \frac{\partial}{\partial z} e^{-z} K_E \left(\frac{\partial}{\partial z} + \frac{1}{m} \frac{\partial \bar{m}}{\partial z} \right) \psi_m$$

Transport

Source & Sink

Eddy Diffusion

where

E_m = gravitational forces + thermal diffusion + frictional interaction with major species

Upper Boundary Conditions

Diffusive Equilibrium:

$$\left(\frac{\partial}{\partial z} - E_m \right) \psi_m = 0$$

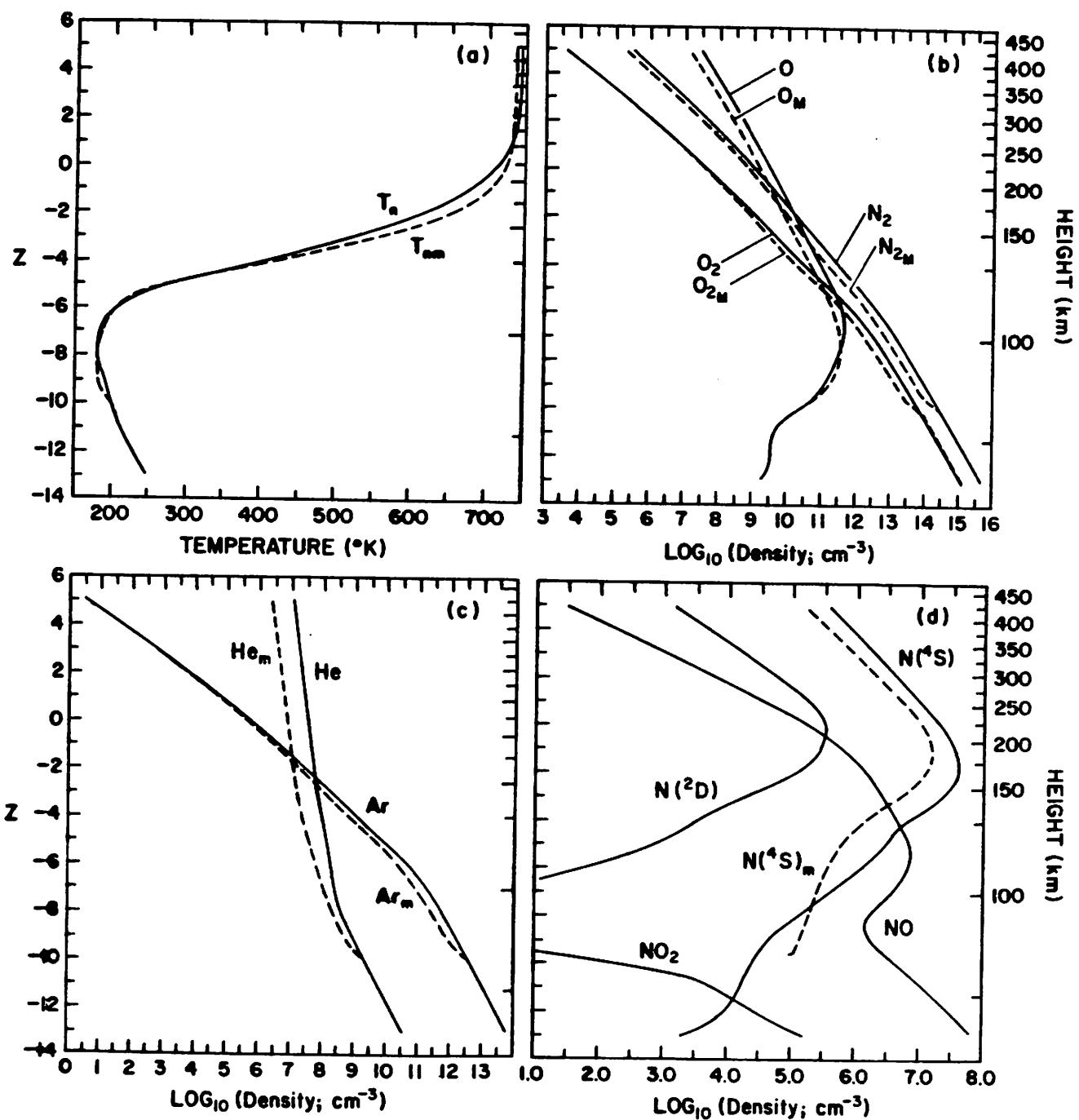
Lower Boundary Conditions

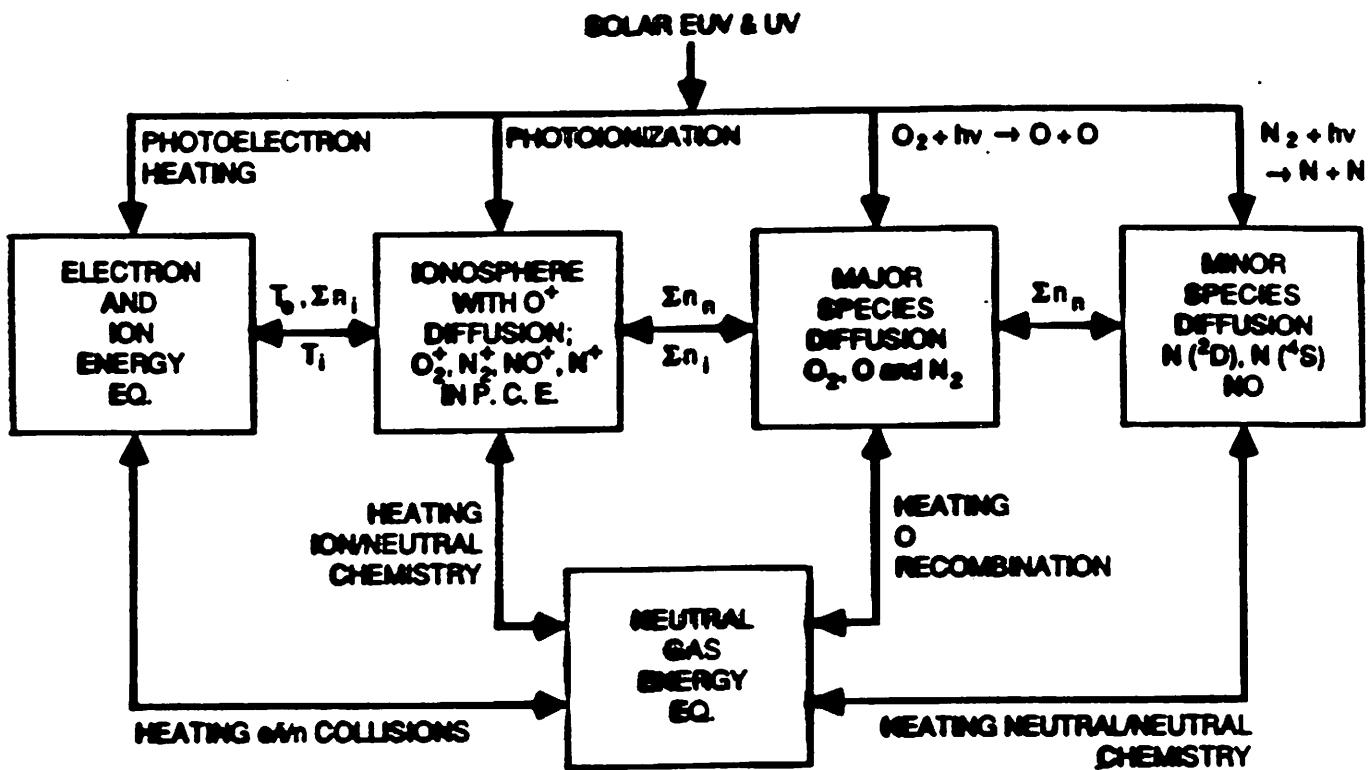
$N(^4S)$ Photochemical Equilibrium

NO Specified Mass Mixing Ratio

1-D

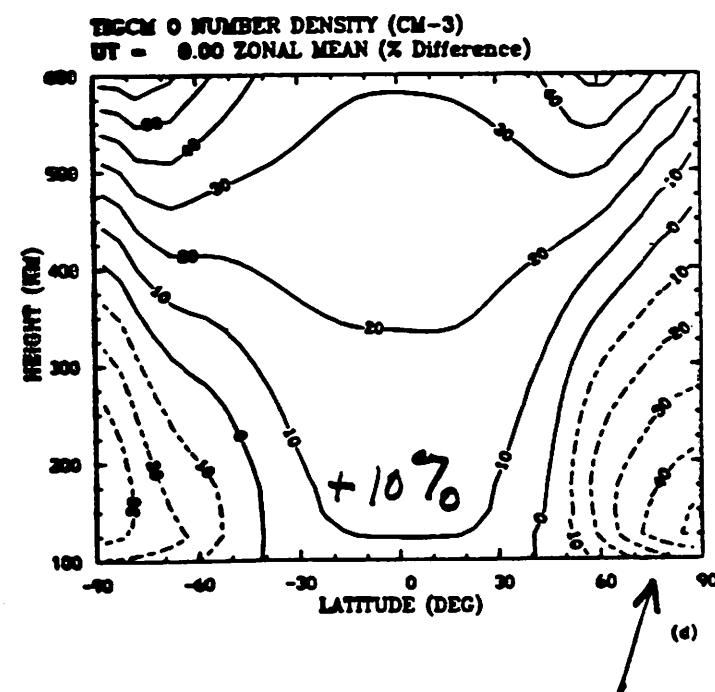
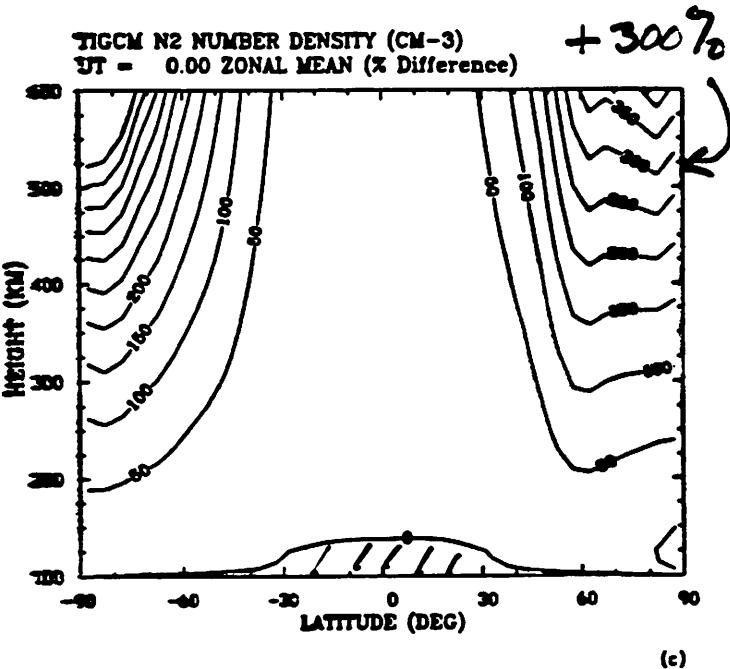
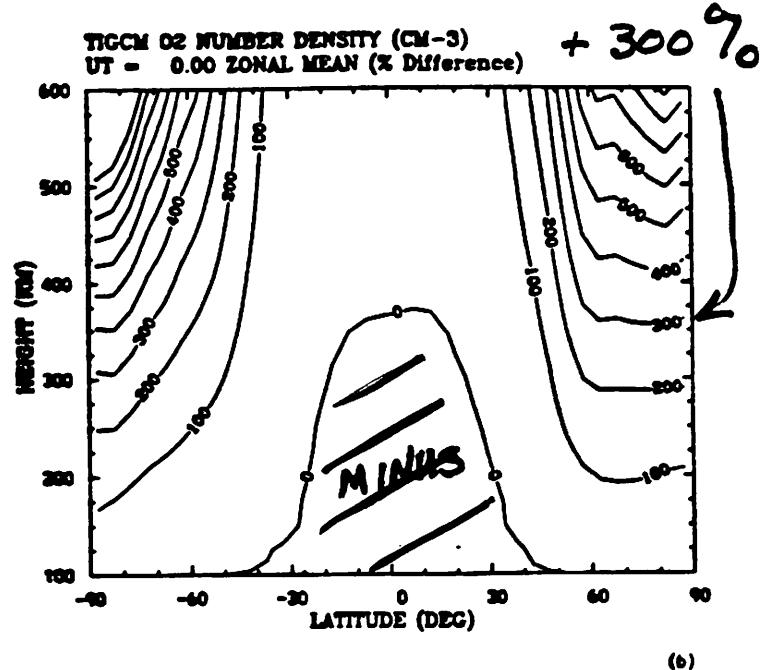
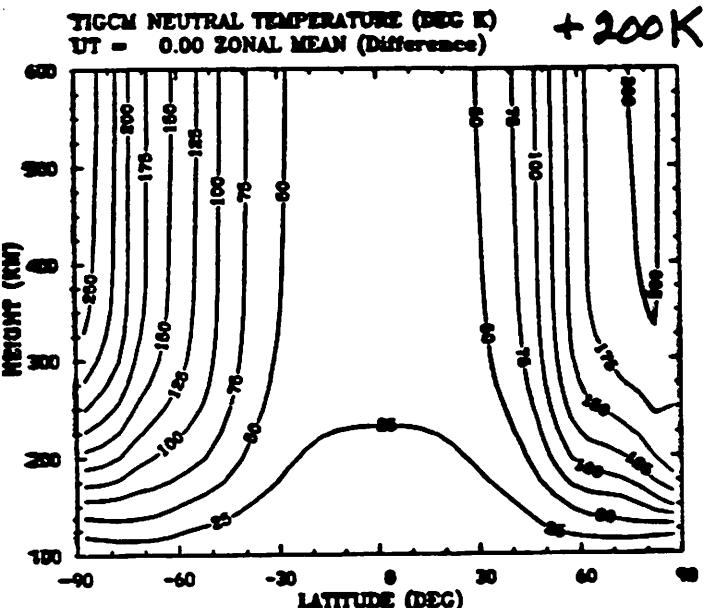
GLOBAL AVERAGE MODEL





EQUINOX (STORM - QUIET)
70KV - 20KV

ΔT (K)



TEMPERATURE , O, O₂ and N₂

changes .

FIGURE 6

EULERIAN IONOSPHERE

O^+ EQUATION WITH HORIZONTAL AND VERTICAL TRANSPORT

$$\frac{\partial n}{\partial t} - Q + Ln = - \nabla \cdot n \underline{V}$$

$\beta = \text{ALONG } \vec{B}$
 $\perp = \text{PERPENDICULAR TO } \vec{B}$

where $\underline{V} = \underline{V}_\beta + \underline{V}_\perp$

$$\underline{V}_\beta = \left[\underline{b} \cdot \frac{1}{\nu} \left(g - \frac{1}{\rho_i} \nabla p_i \right) + \underline{b} \cdot \underline{u} \right] \cdot \underline{b}$$

$$\underline{V}_\perp = \frac{1}{|B|} \underline{E} \times \underline{b}$$

now, $- \nabla \cdot n \underline{V}_\beta = b_z^2 \left(\frac{\partial}{\partial z} + \frac{\nabla \cdot \underline{b}}{b_z} \right) D \left(\frac{\partial}{\partial z} T_p + \frac{g m_i}{k} \right) n$

$- (\underline{b} \cdot \underline{u}) n \nabla \cdot \underline{b} - \underline{b} \cdot \nabla (\underline{b} \cdot \underline{u}) n$

$- \nabla \cdot \underline{v}_\perp = \underline{B} \times \underline{E} \cdot \nabla (n/B^2)$

Upper Boundary Conditions

Mixed boundary condition

$$- b_z^2 D \left(\frac{\partial}{\partial z} T_p + \frac{g m_i}{k} \right) n + n (\underline{b} \cdot \underline{u}) b_z + \frac{n (\underline{E} \times \underline{B})_z}{B^2} = \Phi_z$$

Lower Boundary Conditions

Photochemical equilibrium

$$n = Q / L$$

O_2^+ , N_2^+ , N^+ and NO^+

Once the O^+ distribution is determined the O_2^+ , N_2^+ , N^+ and NO^+ equations are solved simultaneously assuming photochemical equilibrium with the O^+ distribution. From the chemistry specified, the production and loss terms are equated and a fourth order equation for n_e can be derived:

$$a_4 n_e^4 + a_3 n_e^3 + a_2 n_e^2 + a_1 n_e + a_0 = 0$$

where

$$n_e = n(O^+) + n(O_2^+) + n(N_2^+) + n(N^+) + n(NO^+)$$

$$a_3 = \alpha_1 (\alpha_2 E + \alpha_3 C) - \alpha_1 \alpha_2 \alpha_3 (F + G)$$

$$a_2 = \alpha_1 EC - \alpha_1 (\alpha_2 E + \alpha_3 C) (F + G) - \alpha_1 \alpha_2 D - \alpha_1 \alpha_3 B - \alpha_2 \alpha_3 A$$

$$a_1 = -\alpha_1 [EC(F + G) + DC + BE] - \alpha_2 E(A + D) - \alpha_3 C(A + B)$$

$$a_0 = -EC(A + B + D)$$

$$A = k_2 n(O^+) n(N_2) + k_7 n(N^+) n(O_2) + \beta_9 n(NO)$$

$$B = \eta(O_2^+) + k_1 n(O^+) n(O_2) + k_6 n(N^+) n(O_2)$$

$$C = k_4 n(N(^4S)) + k_5 n(NO)$$

$$D = \eta(N_2^+)$$

$$E = k_3 n(O)$$

$$F = n(O^+)$$

$$G = n(N^+).$$

The quartic equation can be solved exactly yielding four roots. Three of the roots are imaginary or not physical leaving one real and physical root, for the electron density, n_e . Once n_e is known, the ion number densities can be determined from

$$n(N_2^+) = D / (E + \alpha_3 n_e)$$

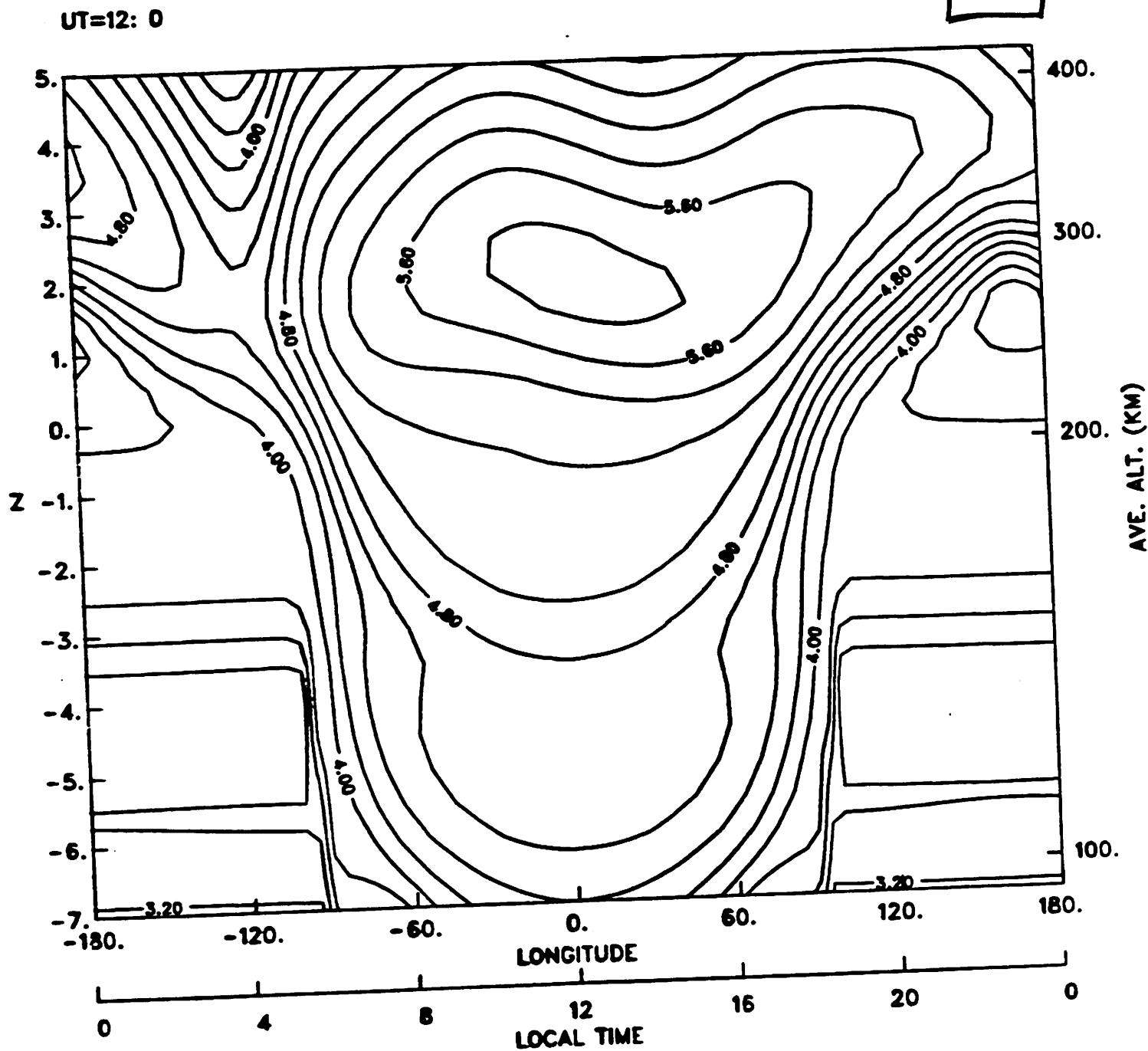
$$n(O_2^+) = B / (C + \alpha_2 n_e)$$

$$n(NO^+) = (A + ED / (E + \alpha_3 n_e) + CB / (C + \alpha_2 n_e)) / (\alpha_1 n_e)$$

$$n(N^+) = \eta(N^+) / ((k_6 + k_7) n(O_2) + k_8 n(O)).$$

ARECIBO

$(\log_{10}(n_e; \text{cm}^{-3}))$

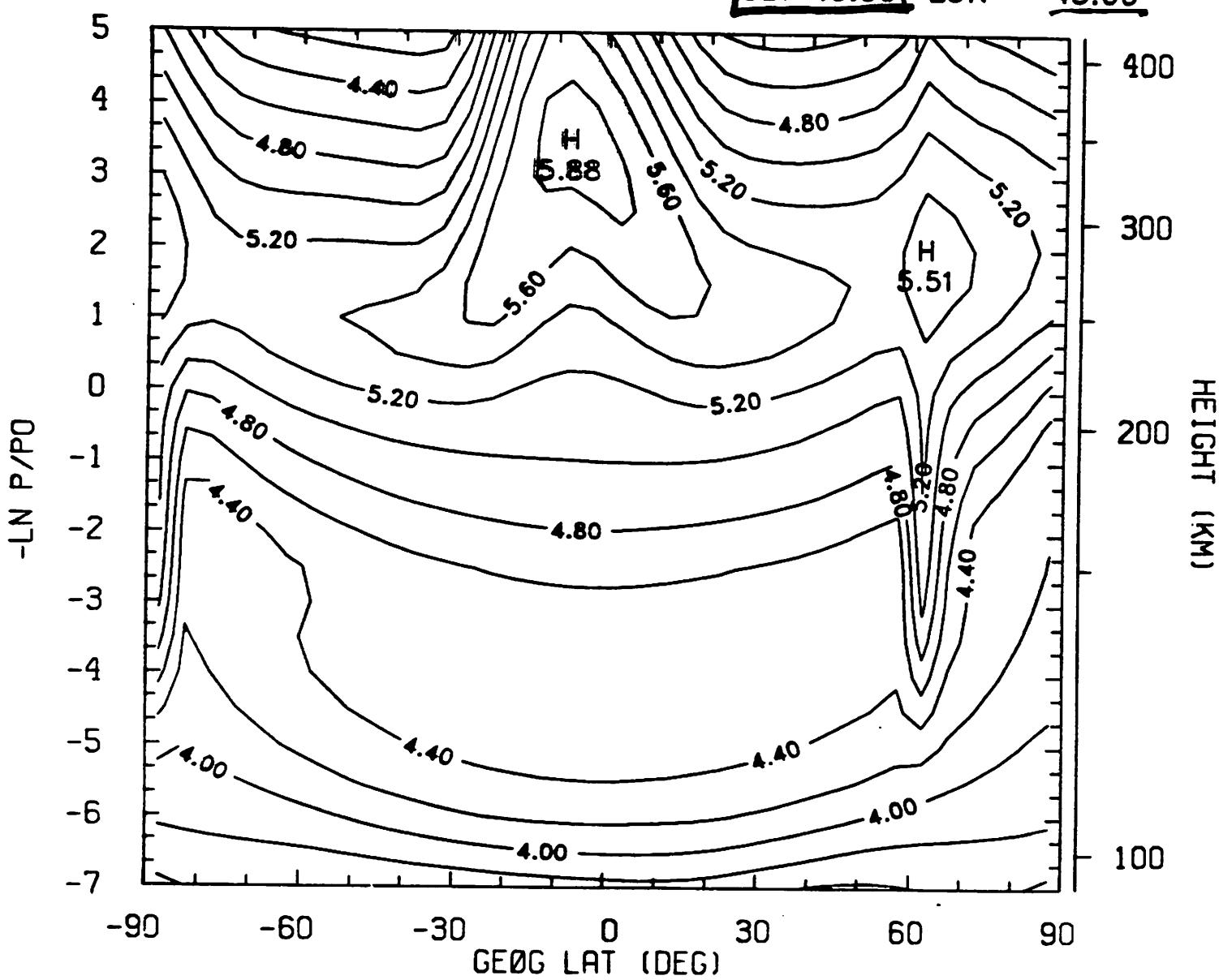


LOG TGCM ELECTRON DENSITY (HIST) (CM-3)

76080 EQSN03,N04

UT=19.00 SLT=16.00

LON= -45.00



TIGCM OUTPUT

- Neutral gas temperature, T_n
- Neutral winds, U, V, W
- Height of constant pressure surface, h
- Neutral composition and density

Major – O, O_2 , and N_2

Minor – $N(^2D), N(^4S), NO, He$, and Ar

- Ion composition

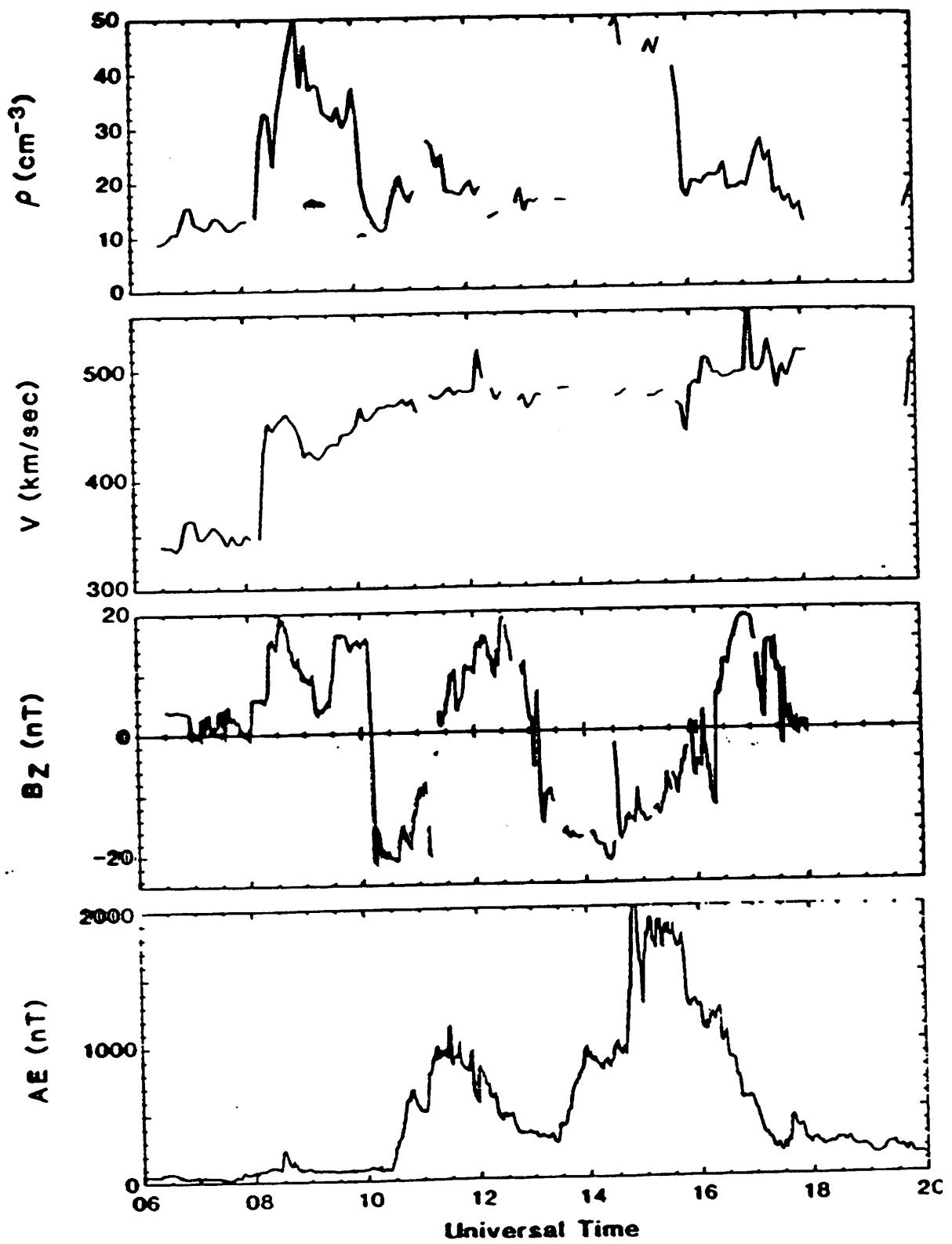
O^+, NO^+, O_2^+, N_2^+ , and $N^+ \sum n_i = n_e$

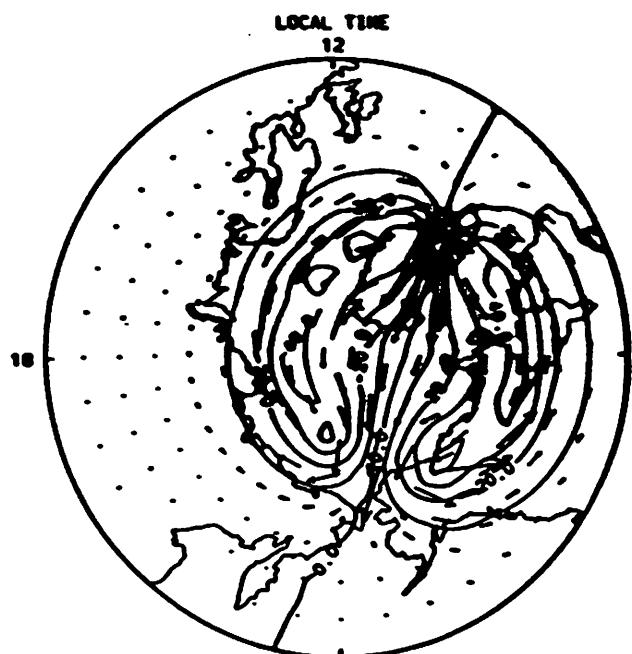
Ion temperature, T_i

Electron temperature, T_e

- Global dynamo — $TIE-GCM$

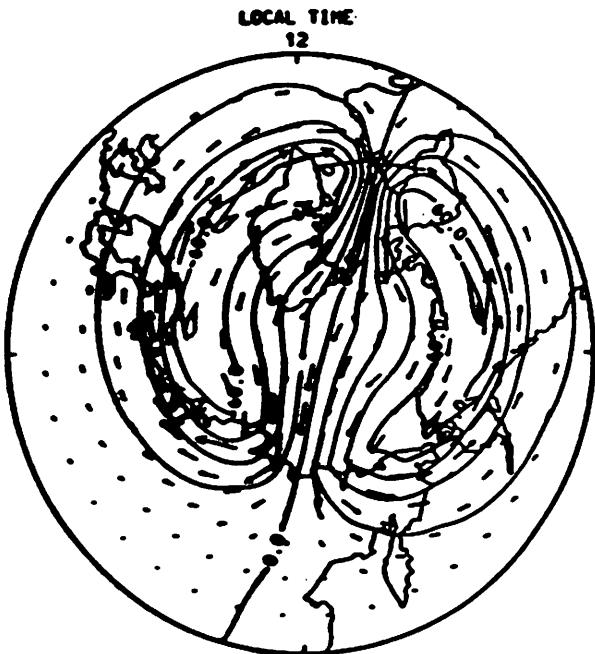
\vec{E}, \vec{J}



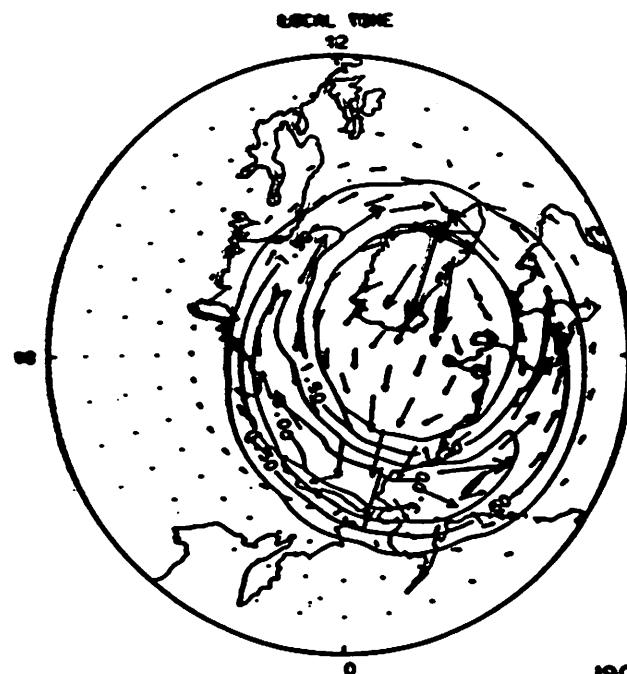


(a)

1900 M/S → (b)



2900 M/S →

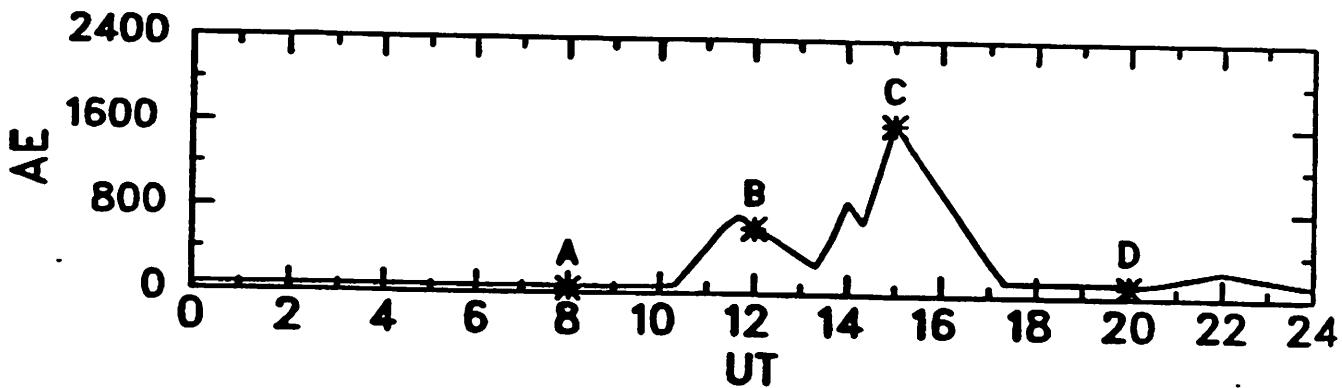
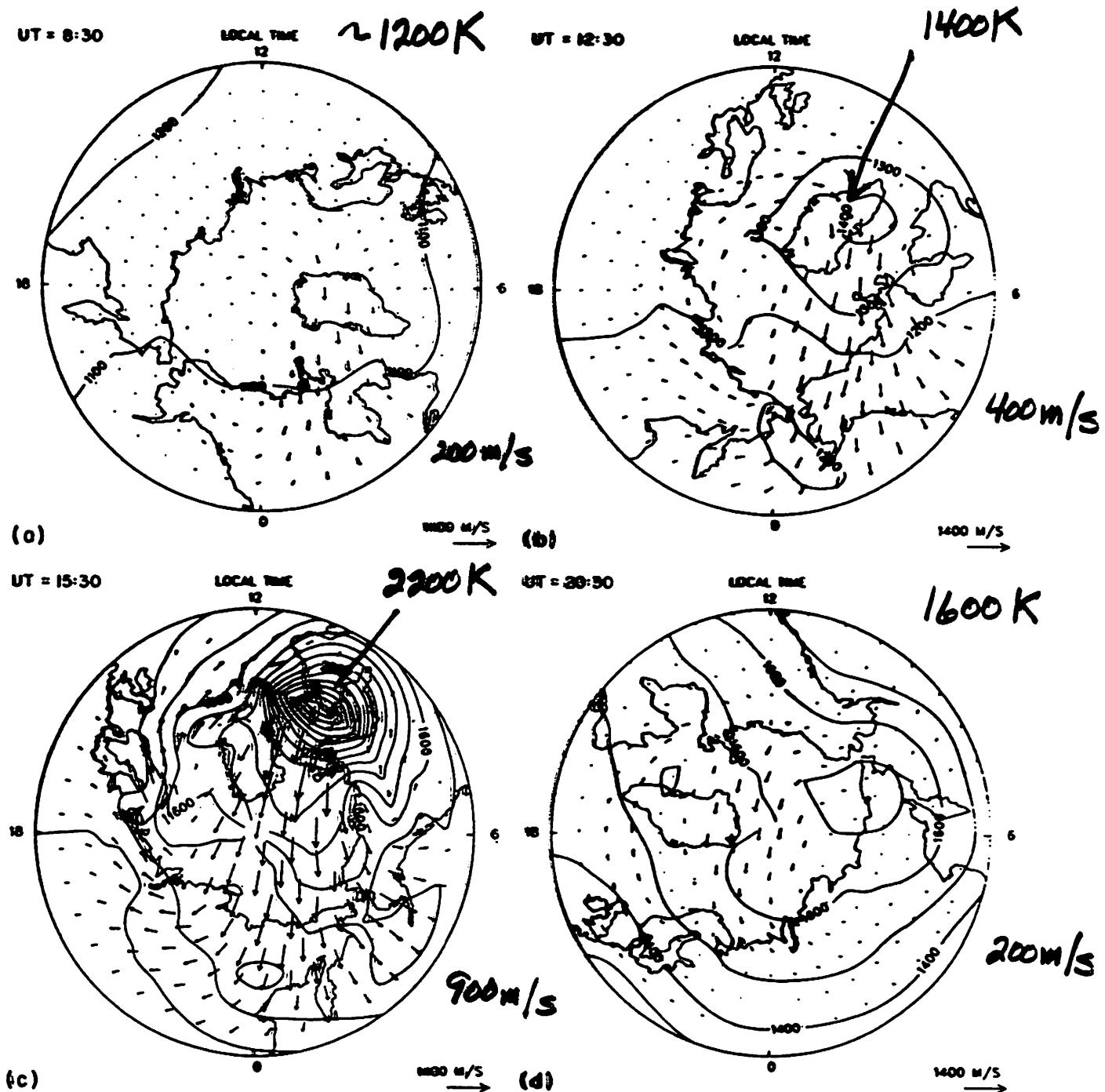


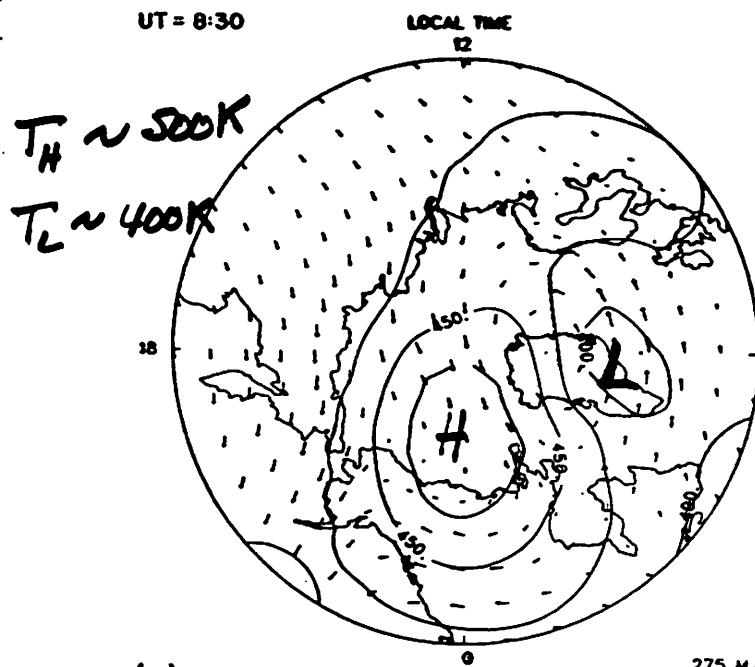
(c)

1900 M/S → (d)

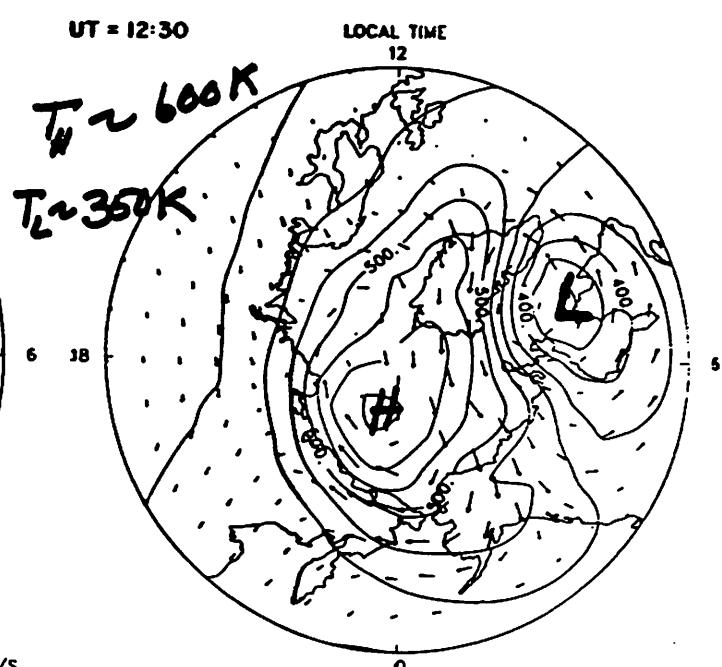


2900 M/S →





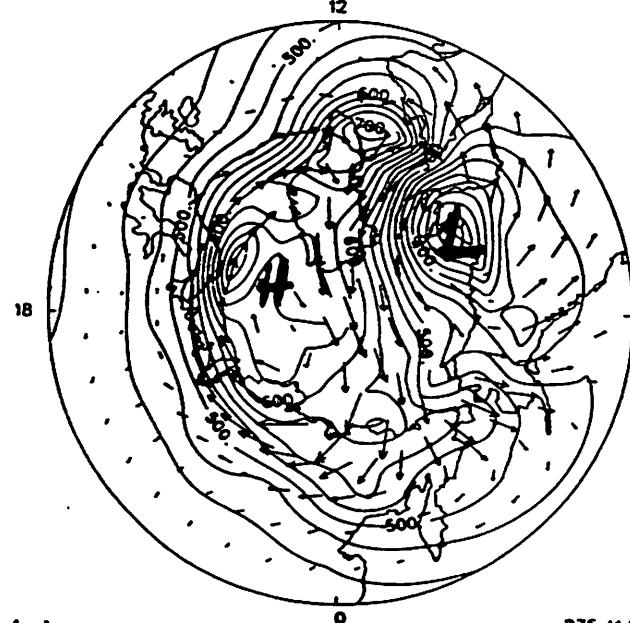
(a)



275 m/s → (b)

UT = 15:30

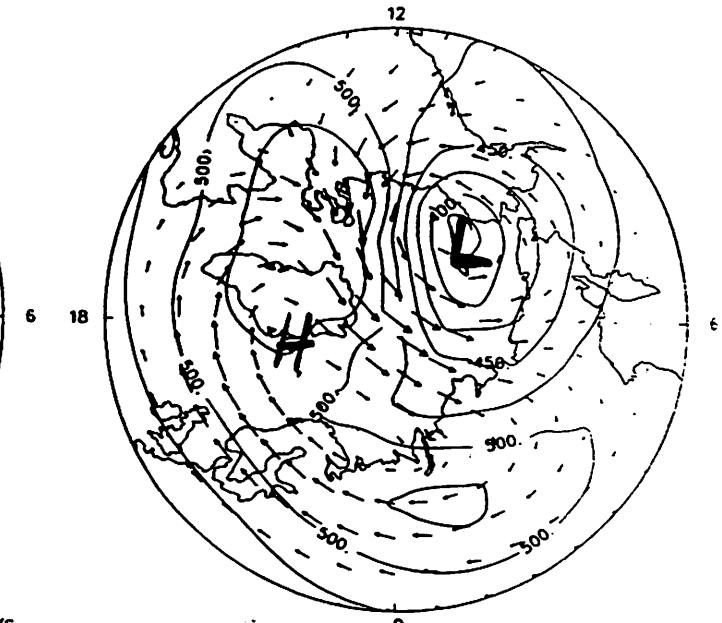
LOCAL TIME



(c)

UT = 20:30

LOCAL TIME



(d)

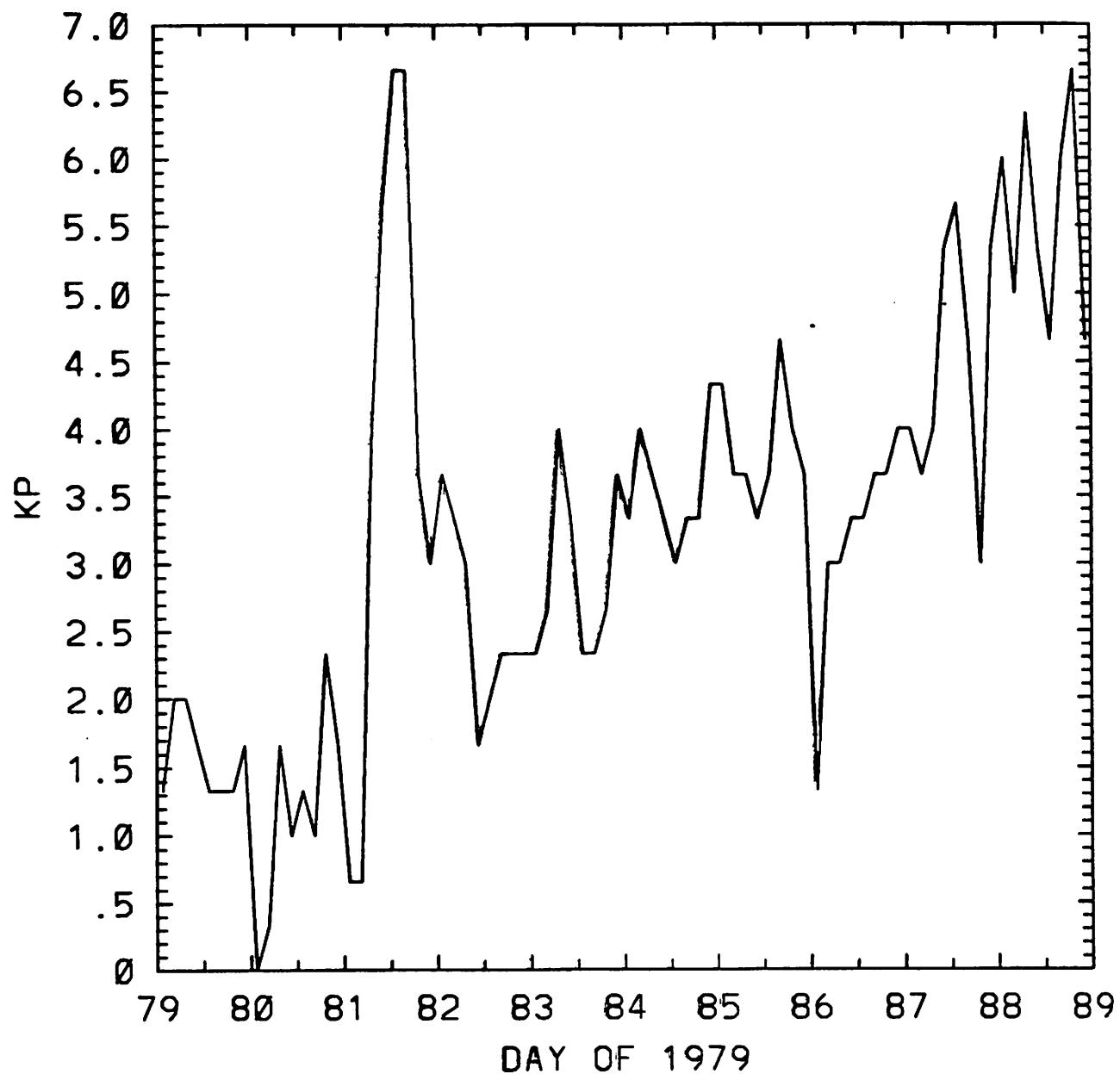
$T_H \sim 650K$

$T_L \sim 300K$

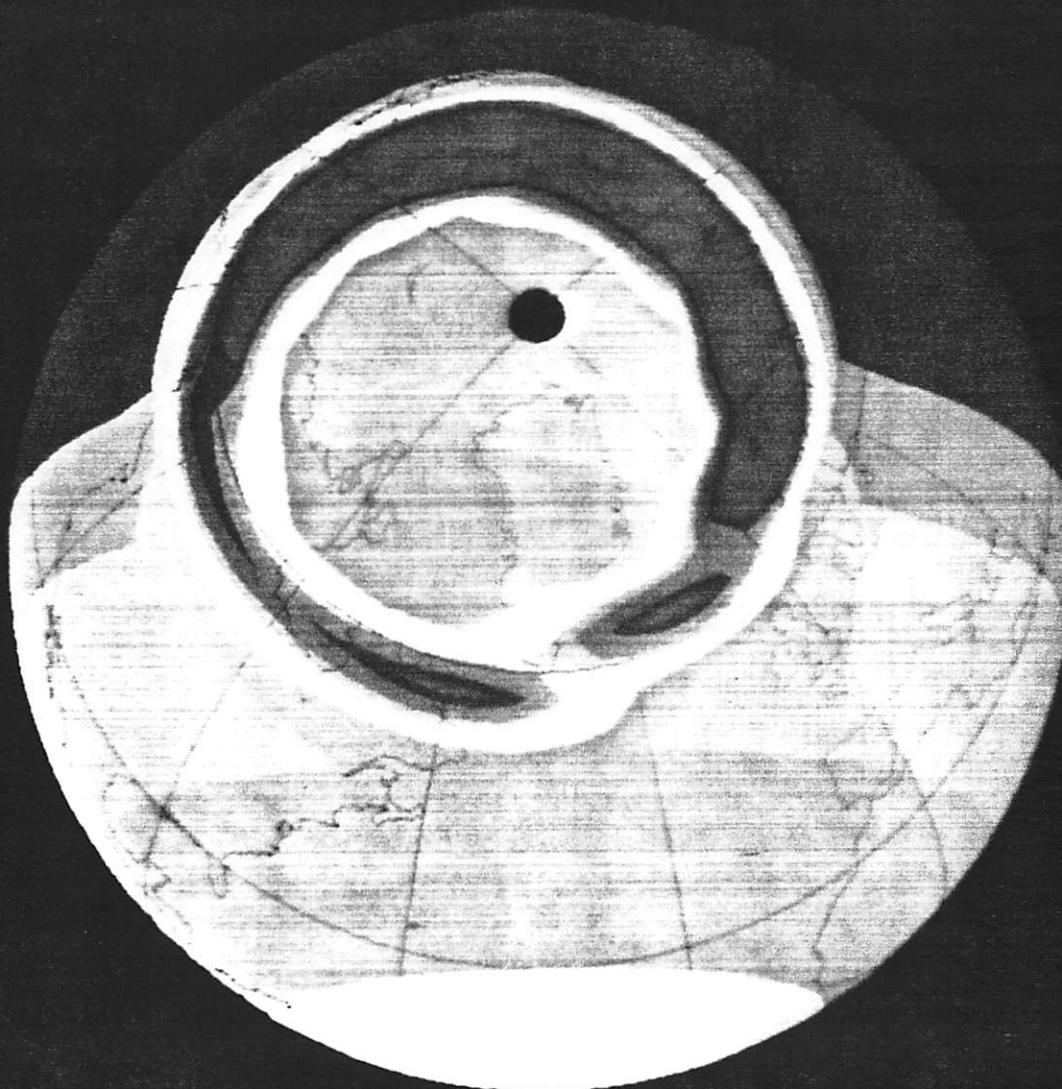
$T_H \sim 500K$

$T_L \sim 350K$

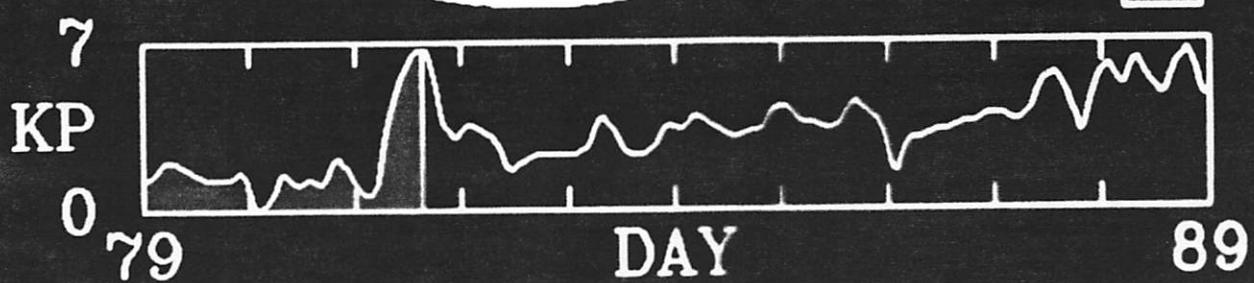
TIGCM INPUTS FOR MARCH/APRIL, 1979



ELECTRON DENSITY (CM⁻³)
DAY=79081 UT=15.00 ZP=-4.0

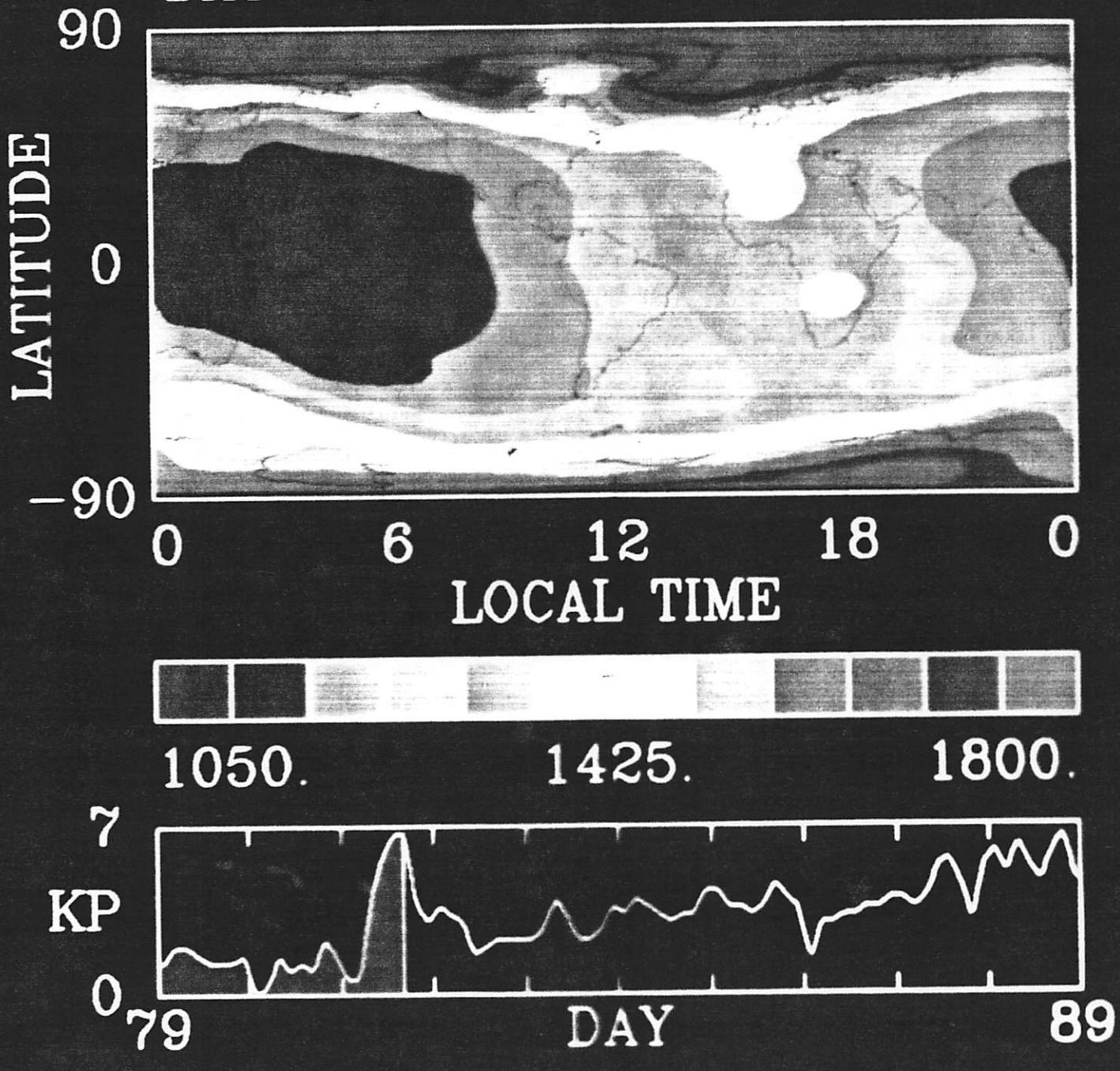


3.00E+05
1.50E+05
0.00E+00



NEUTRAL TEMPERATURE (DEG K)

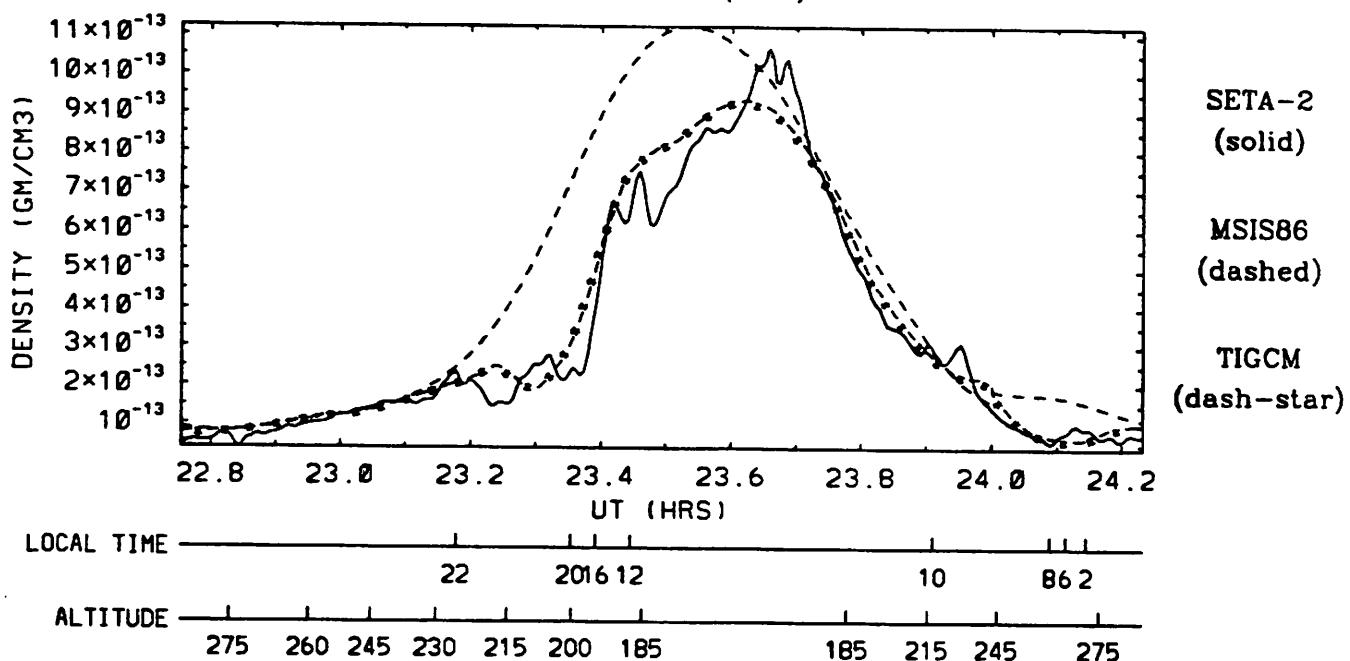
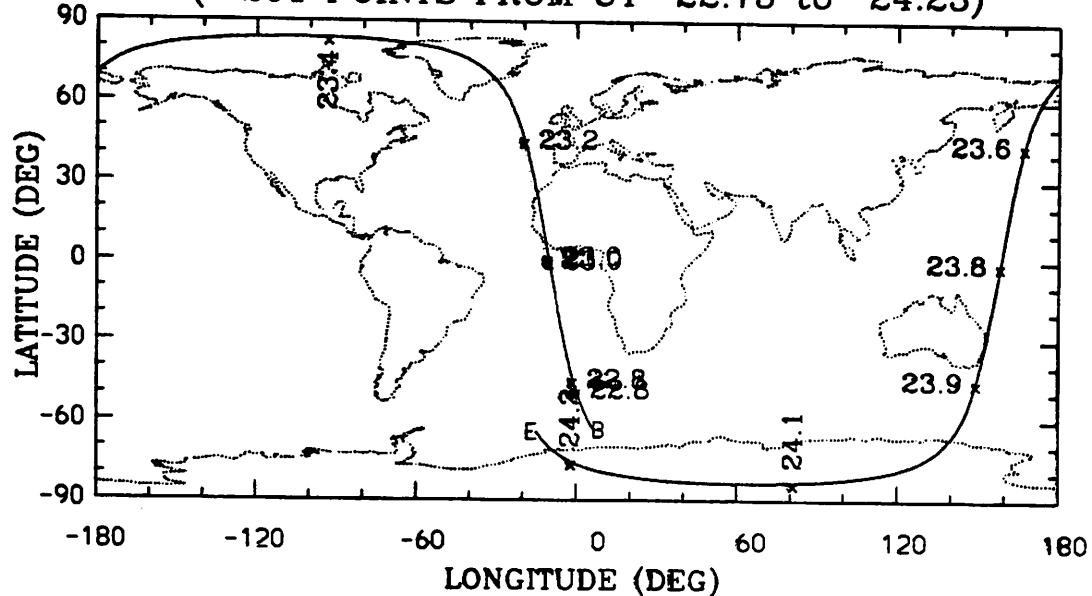
DAY=79081 UT=16.00 ZP= 2.0



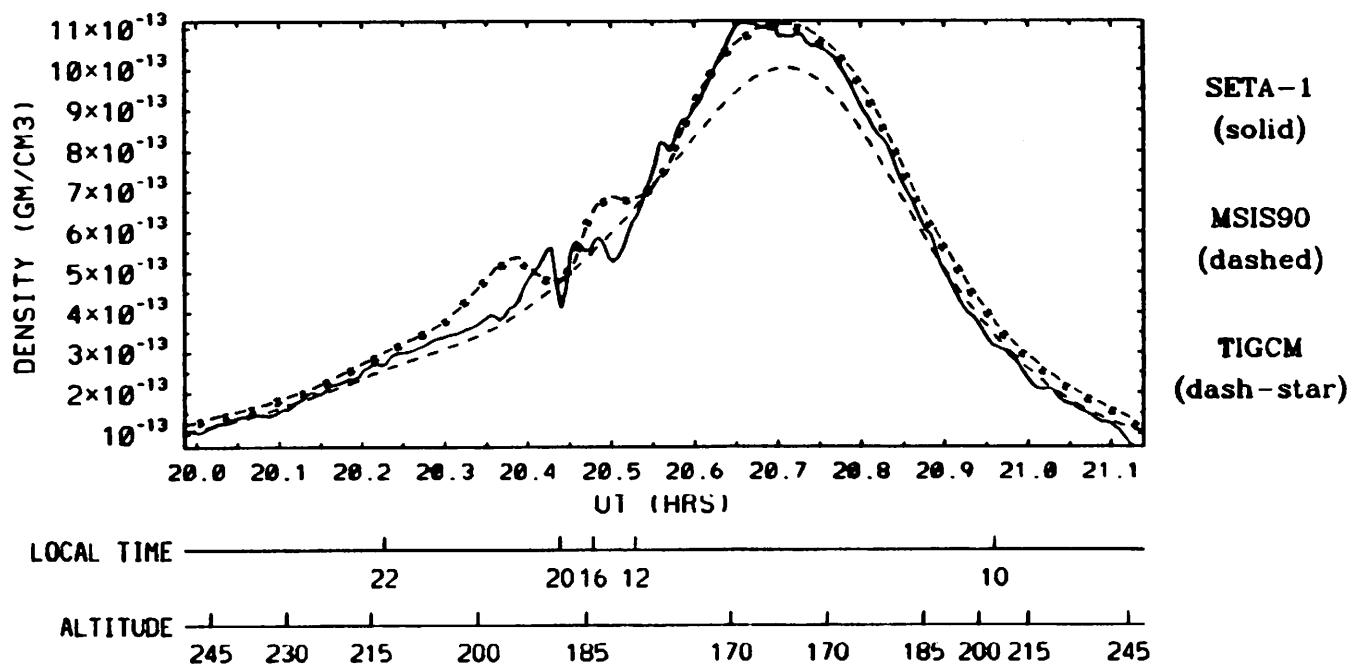
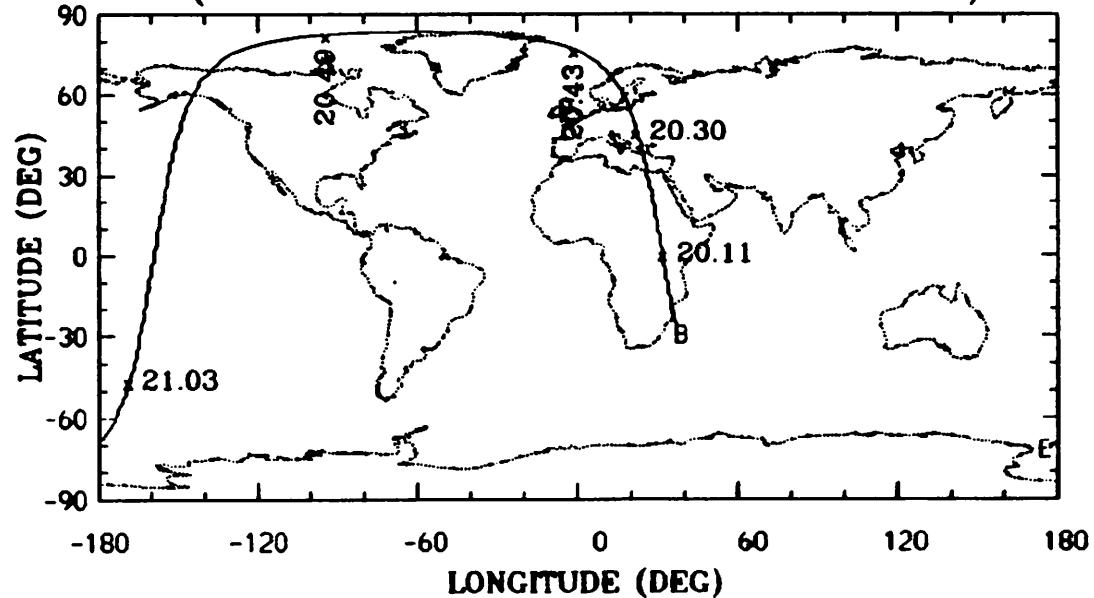
ATOMIC OXYGEN (CM⁻³)
DAY=79088 UT= 6.00 ZP=-4.0

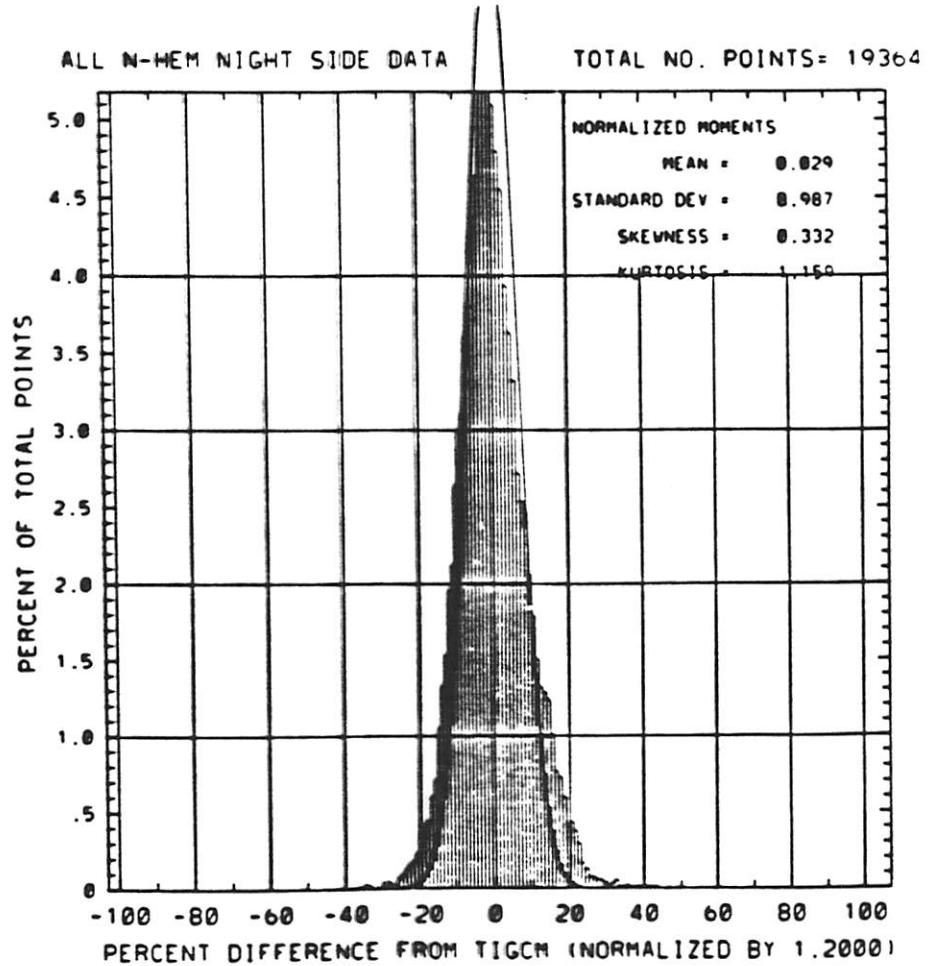
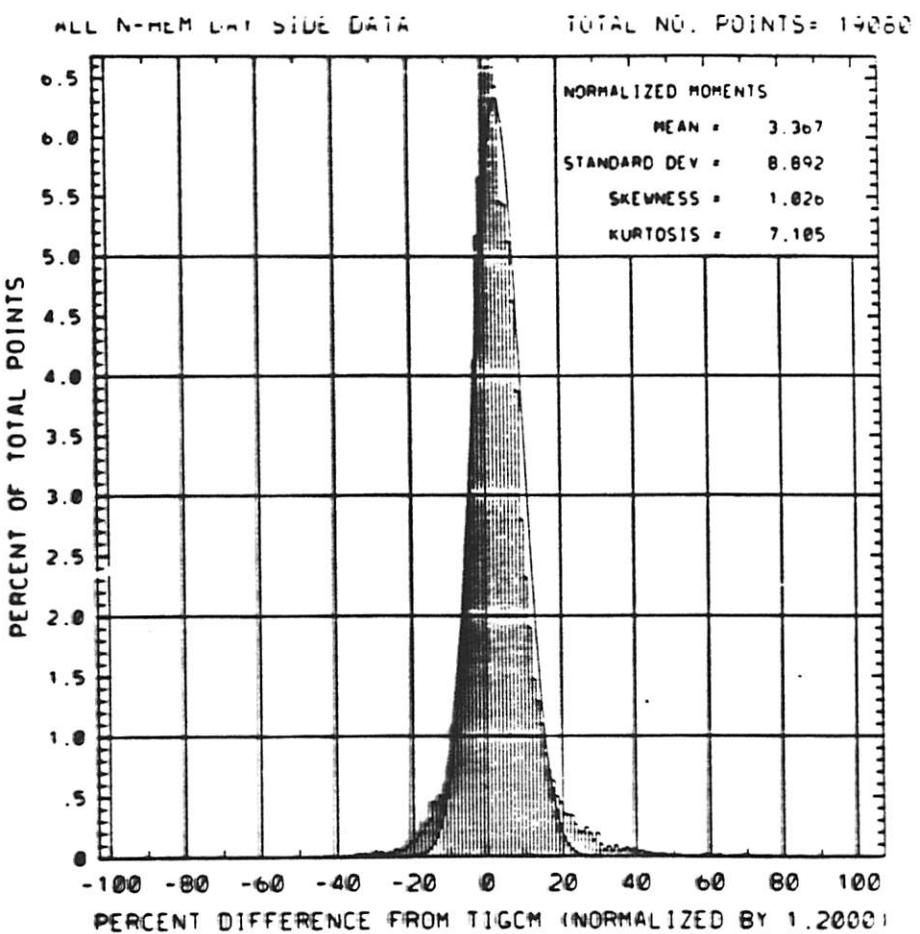


SETA-2 ORBIT 1026 DAYS 82194-82195 AVE ALT 224.40
 (261 POINTS FROM UT 22.75 to 24.23)



SETA-1 ORBIT 180 DAY 79086 AVE ALT 201.32
 (204 POINTS FROM UT 19.99 to 21.14)





SUMMARY

What have we learned

- Thermosphere is stable, no internal instabilities
dynamically reproducible
- Variability caused by variations in solar
and annual forcing.
- Lower thermosphere appears highly variable
because of disturbances from lower atmosphere
 - + Tides
 - + Gravity Waves and mixing
 - + 2 day - - - 16 day wave .
 - + TIME-GCOS suggest large variability in
lower thermosphere .
- Global composition - O/N₂ , O/O₂ ratio
- Ionospheric variability
 - + winds
 - + composition
 - + ion drag .
- Processors — station, satellite track etc
- Diagnostic Processors , Physical & chemical
processes .