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**Tutorial Lecture** 

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**Time-Varying Convection** 



# Magnetohydrodynamics (MHD)

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From 3 of Maxwell's equations:  

$$\overline{\nabla \cdot B} = O$$

$$\overline{J} = (\nabla \times \overline{B})/\mu_{o}$$

$$\frac{\partial \overline{B}/\partial t = -(\nabla \times \overline{E})}{(\overline{Faraday's Law} with \partial D/\partial t = O)}$$
(Faraday's Law)  
Plus a generalised Ohm's Law  

$$\overline{[\overline{J} = \sigma(\overline{E}') = \sigma(\overline{E} + \overline{\nabla} \times \overline{B})]}$$
We get the "INDUCTION EQUATION"  

$$\frac{\partial B}/\partial t = \nabla \times (\overline{\nabla} \times \overline{B}) + \nabla^2 B/\mu_o \sigma$$
convective term diffusive term  
Magnetic Reynolds Number,  

$$R_m = \frac{\text{convective term}}{\text{diffusive term}} \sim \frac{VB/L}{B/\mu_o \sigma L^2} = \mu_o \sigma VL$$
If conductivity  $\sigma$ , and spatial scale, L, very large,  $R_m v$ . large  
 $\partial B/\partial t = \nabla \times (\overline{\nabla} \times \overline{B}) :$  in fact means  $\overline{B}$  moves with  $\overline{V}$  - we say  
 $\overline{B}$  is FROZEN-IN to plasma flow,  $\overline{V}$  (applies in most of  
interplanetary space, magnetosphere + F-region ionosphere)  
If L snall solfm <<1,  $\partial \overline{B}/\partial t = \nabla^2 \overline{B}/\mu_o \sigma$  and field  
DIFFUSES through plasma. Actually, high  $\sigma$  ensures that  
this only occurs in highly localised (small L) regions



For ideal MHD, Bs and Bm cannot mix (both frozen-in) If  $\overline{B}_{s} \neq \overline{B}_{m}$  current must flow in magnetopause Solar wind compresses current layer so [1 small] and  $\overline{R_{m}} \Rightarrow 1$ ]. Hence diffusion of B through plasma becomes important. Motion of  $\overline{B}_{s}$  and  $\overline{B}_{m}$  into X-line and of open field lines away from X-line, corresponds to an electric field,  $\overline{E}$ , along X-line, called the reconnection rate

## Field Line Convection due to Magnetic Reconnection

cycle time ≥ 6 hours



- Solar wind particle o Plasma sheet
- Figure 8.27 The history of a field line. (After S.-I. Akasofu, Chapman Memorial Lecture, 1973.)

Interplanetary Field Line  $(B_2 < 0)$ Closed Geomagnetic Field Line Open Field Line





#### A-2. MODEL.

(IMF By ( 0 For Northern hemisphere)



#### B-2 MODEL

(inf By ( 0 for southern howisphere)



FIG. 7. POLAR CONVECTION ELECTRIC POTENTIAL DISTRIBUTIONS FROM HEPPPER (1983), wITH DEPENDENCE ON THE "J" COMPONENT OF THE IMF. (a) The A-2 field – applied to the Northern Hemisphere with BY – vc. Applied to the Southern Hemisphere with BY – vc. Applied to the Northern Hemisphere with BY – vc. Applied to the Northern Hemisphere with BY – vc.

#### HEPPNER MODEL OF CONVECTION ELECTRIC POTENTIAL

# Origins of magnetospheric and ionospheric convection

## •1. Reconnection

Transfer of open flux from dayside to nightside by solar wind Return flow of closed field lines · 2. Viscous-like interactions any process which acts on closed field lines "anything but reconnection" includes: "impulsive penetration"; wave-driven diffusion; gradient drift entry; Kelvin - Helmholtz waves; solar wind dynamic pressure changes; etc. BUT how much of the apparently viscous effect is due to continuing tail reconnection of residual lobe open flux





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PLASMA FLOWS IN THE EQUATORIAL

Fig. 1. Electric equipotentials (or E × B flow lines) in the equatorial plane of idealized completely open and completely closed magnetospheres.



Fig. 2. Electric and magnetic fields measured before and after a dusk magnetopause crossing.

For Jully-open magnetosphere  $\Phi_v = 0$ 

Consider electric field observations by a satellite moving into magnetosphere at low magnetic latitudes, as shown Plasma drift, V = ExB/B2 : drift normal to path = electric field component along path, Eo voltage,  $\Phi = \int_{v}^{E} E_{o} dl$ where A and B are the edges of the anti-sunward moving LLBL

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Mozer, Geophys. Res. Lett., 11,135,1984

(NB. In comment, Heikkila (Geophys. Aes. Lett., 9,877, 1986) claims LLBL was not crossed , far enough Jown tail to see full IV].



MAGNETOSHEATH  $B_z$ , GAMMAS Fig. 4. Scatter plot of the viscous interaction potential versus *B*, for 28 magnetopause crossings within 2 hours of local dusk.

Dy is less than 15 KV in all cases and typically<5kY. If  $\Phi_v$  is the same on both flanks total contribution to  $\Phi_{pc}$  of viscous-like interactions is typically IOKV and less than 30 KV in all cases is typically IOKV and (consistent with \$pc observed during northward IMF) We Conclude: Reconnection contributes up to ~100 KV to Opc Viscous-like interaction contribute \$ 20KV



A. By>0



Fig. 6





Fig. 7

e.V

Goose Bay HF radar 22 Apr 1988 80 Invariant latitude (deg) 75 1446:57 to 1448:18 UT  $B_y > 0$  12.4 MHz (a) 70 80 Invariant latitude (deg) 75 500 m/ś → 1448:18 to 1450:58 UT 12.4 MHz  $B_{\gamma} \simeq 0$ (b) 70 80 Invariant latitude (deg) 75 1450:58 to 1452:18 UT 12.4 MHz  $B_{\gamma} < 0$ (c) 70 1300 1100 1200 Magnetic local time

Fig. 9



lobe possible reconnection sites subsolar reconnection for northward IMF site for on sonward edges of tail labe southward lobe IWE Introduces "lobe cells" into polar cap convection. (NB. Lassume open lobes never disappear completely) It reconnection occurs at one or other lobe, possibly depending on IMF Bx (?) (Northern hemisphere viscously favoured for Bx < 0?) driven cells 1By1>>0 open/closed boundary This "stirring" effect re-configures open field lines and causes circulation on open field lines.









FIG. 3. COMPARISON OF CIRCLE RADIUS *R* FROM THIS STUDY AND PREVIOUS STUDY.

Polar Cap Flux, 
$$F = B_{i} \pi R^{2}$$
  
 $R = 16.9 - 0.62B_{z}$  (deg.)  
gives  $F = (571.2 - 4.6B_{z} + 0.76B_{z}^{2}) \times 10^{6}$  (bb  
 $B_{z} = 100 \text{ m}$ )  
 $B_{z} = 100 \text{ m}$   
 $B_{z} = -5nT$ ,  $F \approx 3.6 \times 10^{8}$  (bb  
 $B_{z} = -5nT$ ,  $F \approx 8.2 \times 10^{8}$  (bb  
 $\Delta F / \Delta t \sim 130 \text{ kV} = 100 \text{ m}$ )  
(for  $\Delta t = 16.7$ )



Stability of Polarity of IMF Bz (a) Rostoker et al. (1988) Probability P<sub>1</sub> Hapgood et al. (1990) 0.5 10 time, t (hours) P is the probability that the IMF  $B_z$  component remains constant for a time t  $P_1 \approx 0.5$  for t=30 min. Cowley and Lochwood point out that information about Øj cannot reach DE for t<sup>\*</sup>≥ 30min. Probability that  $\phi_j$  has changed polarity by then,  $P_i^* \ge 0.5$ Hence even if  $\phi'(t) = \phi'(0)$  as soon as information reaches DE,  $\phi'(t^*) \neq \phi'(t^*)$  i.e. NOT STEADY STATE

## Electric field mapping

FLUX TUBE from magnetopause (m) to ionosphere (i)



 $\frac{E_m}{JB_m} = \frac{E_i}{JB_i}$ Often used but only applies to steady-state limit.



If  $V_{sh} = 450 \text{ kms}^{-1}$ ,  $B_n = 5nT$   $E_m = v_{sh}B_n = 2.25 \text{ mVm}^{-1}$ (For a Stern Gap width of  $7R_E$ ,  $V_{sg} = 2.25 \times 10^{-3} \times 7 \times 6370 \times 10^{3} \approx 100 \text{ kV}$ )

 $\begin{bmatrix} In steady - state \\ V_{Sg} = V_{pc} \\ E_m / \sqrt{B_m} = E_i / \sqrt{B_i} \\ for B_m \approx 50nT; B_i \approx 5 \times 10^{-5}T \\ E_i = 70 \text{ mV m}^{-1} \quad V_i = E_i / B_i \approx 1.4 \text{ km s}^{-1} \end{bmatrix}$ 

$$\begin{split} & \frac{E_{m}}{VB_{m}} - \frac{E_{i}}{JB_{i}} = \int_{i}^{m} \left(\frac{\partial B_{x}}{\partial t}\right) \frac{1}{JB} ds \\ & \text{let us consider} \quad \left(\frac{\partial B_{x}}{\partial t}\right) \text{ needed to make } E_{i} = 0 \\ & \text{for this } E_{n} = 2.25 \text{ nVm}^{-1} \text{ and } B_{m} = 50nT, by \\ & \text{assuming} \quad \left(\frac{\partial B_{x}}{\partial t}\right) \text{ is independent of s} \\ & \text{Can then use a model field (Tsyganentho T87 model)} \\ & \text{to compute } \int_{i}^{m} \frac{1}{JB} ds \\ & \text{For Stem Gap at } X = -15R_{E}, \int_{i}^{m} B^{-1/2} ds \approx 10^{12} \text{ mT}^{-1/2} \\ & \text{E}_{i} = 0 \quad \text{if } \frac{\partial B_{x}}{\partial t} = \frac{2.25 \times 10^{-3} / (50 \times 10^{-9})^{1/2}}{10^{12}} = 10^{-11} \text{ Ts}^{-1} \\ & \text{Substarm growth phase typically lasts ~ 45min \\ & = 2700s. \\ & \text{during which } \Delta B_{x} \sim \left(\frac{\partial B_{x}}{\partial t}\right) \Delta t \\ & \sim 27nT \\ & \text{Field changes of this magnitude are observed during substarm growth phases (eq. Fairfield and Ness, 1970; Fritz, 1984) implying Stern Gap voltage of \\ & 1000 \text{ hV need } not cause any incordentic \\ & \text{functional phase lasting 45min.} \\ & (instead, magnetic energy is stored in the tail) \\ \end{array}$$





Figure 1. Location of seven spacecraft during the CDAW-6 substorm of 11 UT on March 22, 1979. Note the radial alignment of four satellites along the 0200 LT meridian-with ISEE-1 at a GSE position of  $(-13.6 R_g, -7.2 R_g, 0.6 R_g)$  and ISEE-2 at  $(-12.1 R_g, -7.1 R_g, 0.3 R_g)$ . The relative positions of these satellites changed very little during the event discussed here.

Figure 3. Magnetic field measurements made by the magnetometer on satelli GOES-3 during the CDAW-6 substorm of 11 UT on March 22, i979. See te definition of V, D, and H components.

FRITZ ET AL. 205



Figure 5. Magnetic field measurements in GSE coordinates made by the magnetometer on satellite ISEE-1 during the CDAW-6 substorm of 11 UT on March 22, 1979.

Fritz et al. (1984)



Lockwood et al., 1986



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FIGURE 2. Example of an observed ionospheric response to a southward turning of the IMF (27 October 1984). (a) The sunward, dawnward and northward components of the IMF in GSM coordinates  $(B_x, B_y \text{ and } B_z, \text{ respectively})$ , observed by AMPTE-UKS when located immediately sunward of the Earth's bow shock. (b) The simultaneous observations by the EISCAT radar. The flow vectors have been rotated through 90° to avoid congestion of the plot; hence northward flow is shown by vectors directed to the right of the figure and westward flow by vectors directed upward (i.e. the vectors are in the direction of the electric field). The vectors are superimposed on a colour plot of two-minute averages of the ion temperature,  $T_i$ . (From Willis et al. 1986.)





FIG. 4c. AS FOR FIG. 4a EXCEPT FOR THE LOCAL TIME INTERVAL FROM 13:00 TO 15:00 M.L.T.

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Lockwood and Cowley (1992)











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Zero-flow equilibria

(Introduced by Cowley and Lochwood, 1992)



(b)



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Continuous Nightside -06 Reconnection Ød = 0  $\phi_n > 0$ 

NB. Average over a long (several days) time scale and  $\frac{d}{dt}A_{pc} = 0$ , i.e.  $\emptyset d = \emptyset_n$ :. Long term averages are steady-state models.



Steady State  $\phi_d = \phi_n$ 

1 24 }ends of { dayside
 iqhtside merging gaps

(c)

## Northward IMF Substorms



(a)

(Ь)



lobe circulation cell (1) due to reconfiguration of already open field lines. v are viscously driven cells.

 $\phi_{d}' = 0$  $\phi_n' > 0$ Ø, >0



Boundary moves so lobe and viscous cells are no longer distinct

(c)

 $\phi_{d}' = 0$  $\phi_{n}' > 0$  $\phi_{v} = 0$ 



Similar pattern if no viscous interaction

adiaroic open / closed boundary
 merging gap
 flow streamline
 boundary motion

Lochwood and Cowley (1992)





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X,



contour interval is 10 kV. The IMF values are shown at the upper right. In regions where the uncertainty in the large-scale electric field is 50% or greater the contours are dashed.

Dy and dayside flow decay in ~10min Øn and nightside flow decay in several hours



McPherron and Manka (1985)













## Summary

• Comparison of ionospheric transpolar voltage with voltage across LLBL shows convection is predominantly driven by reconnection • Explains By and Bz effects on convection Consideration of length of magnetotail and variability of IMF Bz shows steady-state is exceptional, in anything other than an average sense • ALL empirical models of convection and MOST conceptual ones assume steady state • Electric fields DO NOT map from the magnetopous to the ionosphere in non-steady conditions • In non-steady cases flow streamlines cross non -reconnecting (but moving) open /closed boundary • Average convection is the sum of 2 flow patterns driven by dayside and nightside reconnection · Much viscous like interaction is in fact residual nightside reconnection Transpolar voltage and polar cap size vary in a regular way during the substorm cycle