# Probing the Upper Atmosphere and Ionosphere with Large Radars

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## **Target audience:**

Bright graduate students who don't know much about radars but have inquiring minds

## Goal of this talk:

To give you some idea of

- 1. What radars are good for
- 2. How they differ from lidars (the uses of phase coherence)
- 3. Some basic radar concepts and techniques

- More specifically, we will try to cover (pretty fast), or at least mention
- 1. The radar equation
- 2. The difference between scattering from hard and **SOFT** (main emphasis) targets
- 3. Some properties of soft targets; e.g.,
  - Range dependence of the scattered signal strength
  - The Bragg condition why the radar picks out a single spatial Fourier component of the refractive index fluctuations in a random medium
  - Over- vs under-spread and why it matters; range and frequency aliasing
  - Statistical ideas why one sample isn't enough even if the signal-to-noise ratio S/N is very large

- 4. Some radar techniques; e.g.,
  - FFT analysis of the Doppler spectrum from under-spread targets (Easy to do. Can measure very small Doppler shifts, for example 1 Hz, even if the pulse bandwidth is 1 MHz.)
  - ACF analysis of the spectrum from overspread targets (Not so easy. The price of beating the Fourier uncertainty principle is the addition of radar "clutter", or signals from unwanted ranges that act like noise.)
  - Pulse compression (How to turn a long low power pulse into a short high power one with the same number of joules.)
  - Radar interferometry (How to locate strong scatterers precisely within the scattering volume.)
- 5. Incoherent scatter

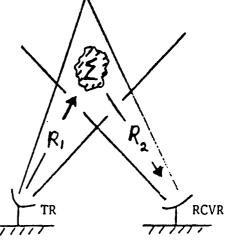
The very weak scatter from purely thermal fluctuations (the irreducible minimum level) in plasma density. For a plasma in thermal equilibrium, the scattered power and signal Doppler spectrum depend in a quantitatively known way on the plasma density, temperatures, ion composition, drift velocity, etc.

So by measuring the power spectrum, or more likely the signal autocorrelation function (ACF), we can determine most of the important plasma parameters via least squares fitting to the theory.

#### RADAR EQUATION

Arec 4TT R<sup>2</sup> Prec = ٤ incident fraction total power scattering received

X-section



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FOR A SINGLE TRANSMIT-RECEIVE ANTENNA (PULSED RADAR)

$$P_{rec} = P_t \frac{GA_{eff}}{(4\pi R^2)^2} \Sigma$$

density

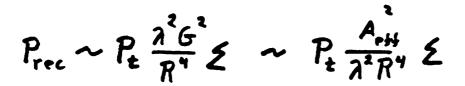
AND

$$G = 4\pi A_{eH}/\lambda^2$$

(ANTENNA THEORY)

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WHAT IS  $\Sigma$  ? [SOFT vs HARD TARGET]

WHAT IS G OR A eff ? [NEAR FIELD vs FAR FIELD]

.

DOES NOT FILL BEAM - e.g. PLANE, MISSILE, SATELLITE

**<b>S** INDEPENDENT OF RANGE

•

SOFT TARGET

FILLS BEAM - e.g. SCATTER FROM ATMOSPHERE, IONOSPHERE

. •

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$$\sum = \sigma_{\text{per unit}} V_{s}$$

AND

$$V_{s} \simeq \Omega R^{2} l \simeq \frac{4\pi}{G} R^{2} l$$

WHERE

$$\mathbf{Q}$$
 = MIN [PULSE LENGTH = CT/2, LAYER THICKNESS]

HENCE

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$$P_{rec} \sim \frac{\lambda^2 G \sigma L}{R^2} \sim \frac{\sigma L A_{eff}}{R^2}$$

What is a "soft" target? Scattering medium "Soft target fills the beam . (Hard target does not.) Radar equation (far field case);  $\frac{P_{r}}{P_{r}} = \left(\frac{G_{t}}{4\pi r^{2}}\right) \frac{\sigma_{t}}{\pi r_{f} + t} \left(\frac{A_{off}}{4\pi r^{2}}\right) \sim \frac{G_{t}}{F^{4}} \frac{A_{off}}{r^{4}} \sigma_{target}$ But Jurget ~ (beam area) (pulse longth) ~ r' 2 pulse (No Aeff for hard target)  $= \frac{P_{r}}{P_{t}} \sim \frac{A_{off} 2}{-2}$ Born approximation always valid for cases of interest

E.P. Single (weak) scattering only, Scatter doesn't alter (attennate) incident beam

Method: Measure the statistical properties (power spectrum or auto-correlation function) of the Scattered signal, which is a Gaussian random variabl

$$\frac{Signal statistics NR}{Straight-forward to show that (for a plasma)}$$

$$\frac{\langle F_{s}(t) F_{s}^{*}(t+t) \rangle \sim \langle \Delta N(A,t) \Delta N^{*}(A,t+t) \rangle}{H}$$

$$\frac{\langle F_{s}(t) F_{s}^{*}(t+t) \rangle \sim \langle \Delta N(A,t) \Delta N^{*}(A,t+t) \rangle}{H}$$

$$\frac{\langle F_{s}(t) F_{s}^{*}(t+t) \rangle}{H} \sim \langle \Delta N(E,t) \Delta N(E+E,t+t) \rangle e^{\frac{A}{2}t} e^{\frac{A}{2}t} e^{\frac{A}{2}t}$$

$$\frac{\langle F_{s}(t) F_{s}^{*}(t+t) \rangle}{H} \sim \langle \Delta N(E+E,t+t) \rangle e^{\frac{A}{2}t} e^{\frac{A}$$

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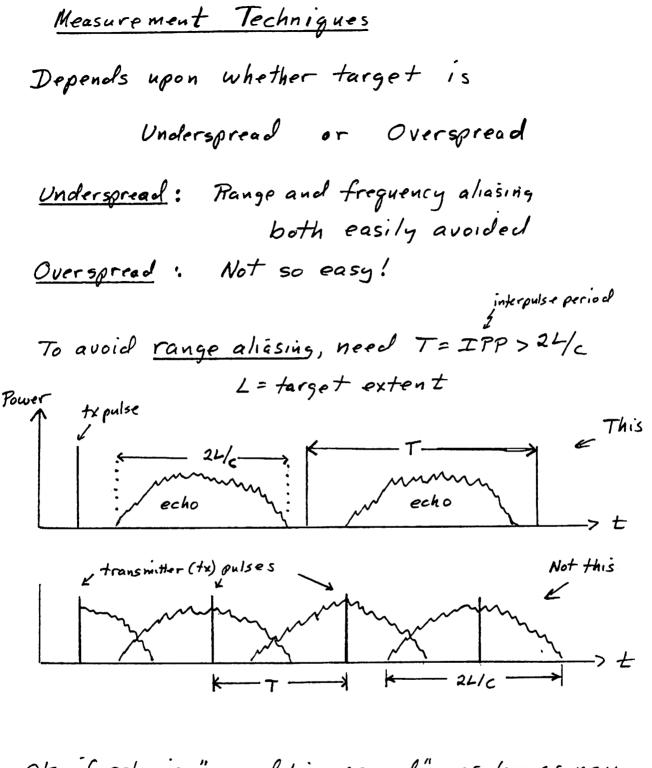
Statistics and Errors Signal and noise are both Gaussian random variables We have to estimate their statistical properties (e.g. mean power, power spectrum ACF) Signal power = Soc P Aant medium 2 (soft target) Frans. R2 pulse Noise power = N = K T B Boltz System receiver For "matched" fiftering (gives max 5/N) we often (but not always) have Brec = Zoulse  $\implies \frac{S}{N} \propto \frac{2}{Pulse} \propto \left( \Delta R \right)^2$ Erange resolution Using many samples of the signal, we form an estimator of the true signal power, or

ACF, etc

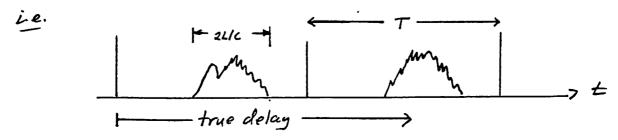
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For example,  $\widehat{S+N} = \frac{1}{K} \underbrace{\frac{5}{2}}_{i=1}^{K} \frac{1}{(\text{transmitter on})}^{2}$ ,  $\widehat{N} = \frac{1}{K} \underbrace{\frac{5}{2}}_{i=1}^{K} \frac{1}{(\text{trans.off})}^{2}$  $\widehat{R}(\widehat{z}) = \frac{1}{K} \frac{K}{2} V(\underline{z}_i) V^*(\underline{z}_i + \widehat{z}) = \frac{1}{K} \rho(\underline{z}) = \frac{R(\underline{z})}{R(0)}$ Easy to show that <N> = N (unbiased estimator) Mean square errors in the estimate:  $S_{x}^{2} = \left\langle \left(\frac{\hat{x} - x}{x}\right)^{2} \right\rangle \simeq \frac{1}{K} \left(\frac{S + N}{S}\right)^{2} A_{2const \sim O(1)}$ where X = S, P(2), or whatever K= number of independent samples used in the estimator => Use tradeofts between K and S/N wisely <>> => ensemble average (~ time average) in the above

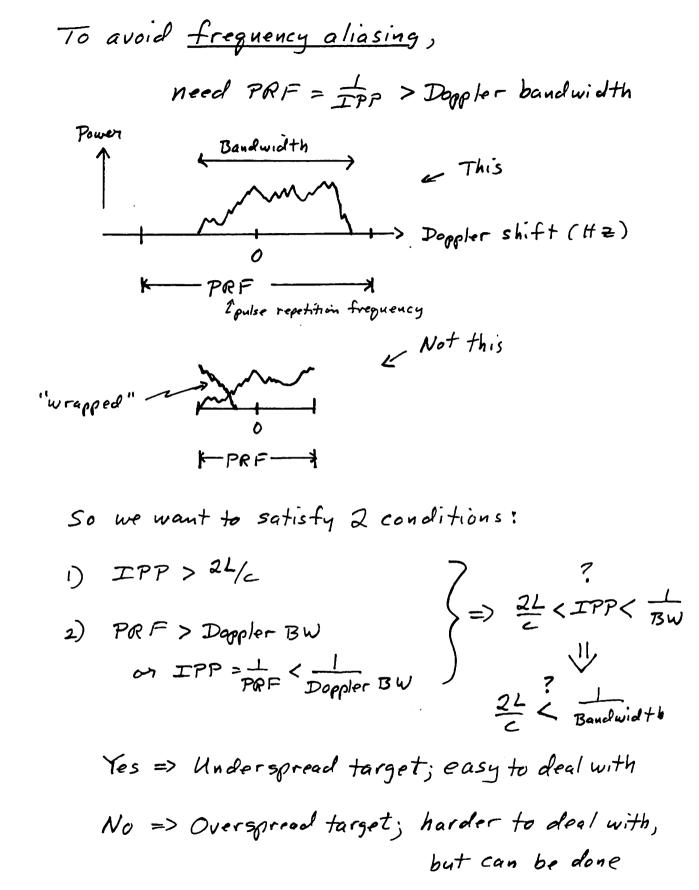
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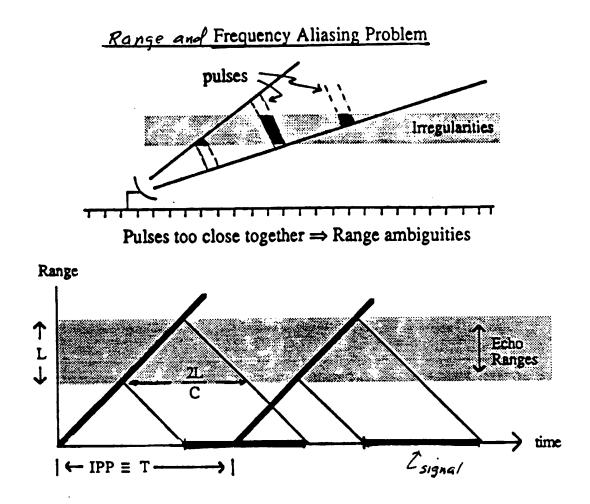


OK if echo is "second time around" - as long as you Know this is the case (which you asually do)

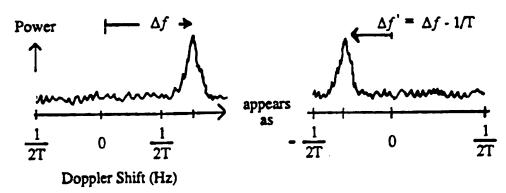


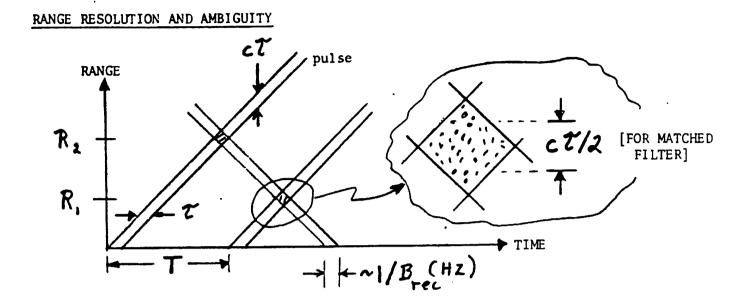
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- Need T > 2L/c (as shown) to avoid ambiguity.
- But we also need T < 1/2lΔfl to avoid frequency aliasing. (Δf = echo Doppler shift)</li>
   i.e., need |Δfl < 1/2T < c/4L</li>
- If not true => target echo is aliosed in frequency





MATCHED FILTER: RECEIVER GATE WIDTH ( $\sim B^{-1}$ ) = PULSE DURATION

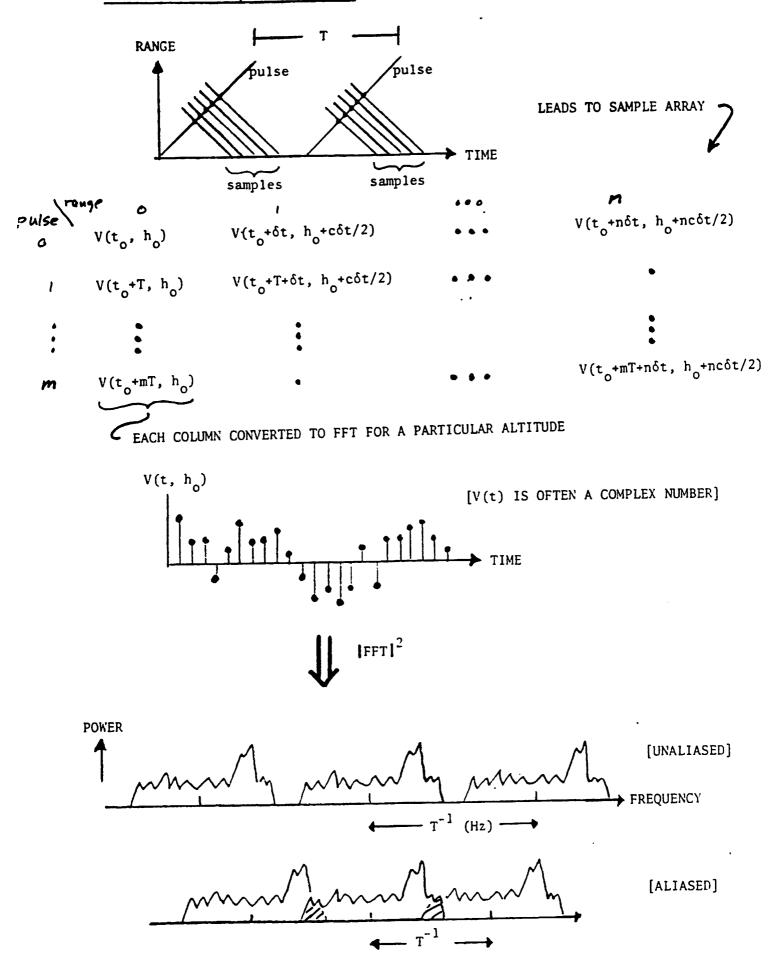
AMBIGUITY: SIGNALS RECEIVED SIMULTANEOUSLY FROM  $R_1$ ,  $R_2 = R_1 + CT/2$ , ETC

RESOLUTION:  $\delta R \simeq MAX [C\tau/2, CB_{rec}^{-1}/2] \simeq C\tau/2$  FOR MATCHED FILTER

TO AVOID OVERLAPPING ECHOES, NEED  $P_s(R_2) \ll P_s(R_1) \longrightarrow LARGE T$ 

BUT FOR STATISTICAL REASONS AND TO AVOID FREQUENCY ALIASING, WE WANT SMALL T

#### SAMPLING AND FREQUENCY ALIASING



Underspread

3

Examples Examples Scatter from stratospheric and mesospheric irregularities Scatter from Quiroral irregularities (sometimes)

> Simple techniques work fine, e.g. 1) Transmit Evenly spaced train of pulses 2) Sample and digitize at each range of interest 3) Compute FFT for each range and average the power spectra

Also available and useful: 1) Coherent integration (this has various definitions) 2) Pulse compression using complementary code pairs (Golay codes), which have no range sidelobes

These work only if the medium correlation time >> IPP

R.g., the stratosphere, for which 2 r few XIO's correl NI IPP ~ 1 ms perhaps

# Overspread

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Examples: Incoherent scatter from random thermal fluctuations in the ionosphere Radar echoes from Mars Radar echoes from the aurora (sometimes)

Techniques now are not so simply

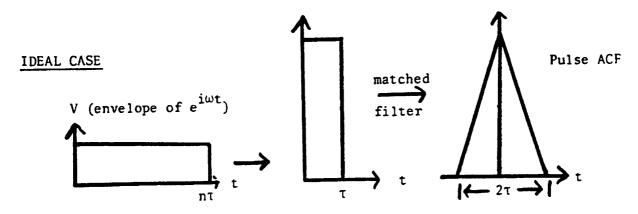
Measure ACF using multipulse schemes (adds clutter)

Pulse compress with Barker (or longer) codes, but be careful about code length (must be 2 or << Ecorrel) Combine both of the above For mildly overspread (e.g. auroral case),

can replace the usual power spectrum with double-pulse cross spectrum that unravels mild frequency aliasing

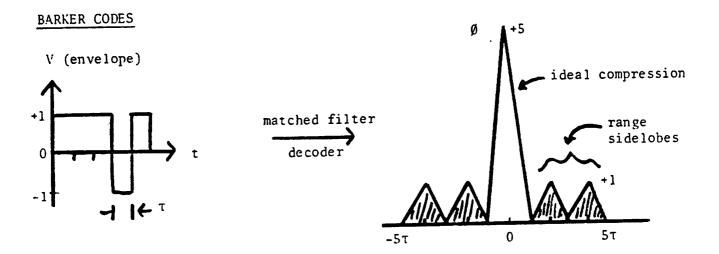
All of these could be used also for undergreed targets, but usually are not

Radar interferometry is also a powerful technique for improving spatial resolution for either class of target



CAN USE FREQUENCY "CHIRPING" OR PHASE CODING

IN PRACTICE USE <u>BINARY PHASE CODING</u> AND DECODE WITH COMPUTER OR SPECIAL PURPOSE DIGITAL OR ANALOG DEVICES



 $\emptyset$  = AMBIGUITY FUNCTION (FOR NO DOPPLER)

= VOLTAGE FROM SMALL STATIONARY TARGET

= ACF OF CODE

TARGET MUST REMAIN COHERENT FOR n⊤ (UNCOMPRESSED DURATION) GROUND CLUTTER DURATION ≥ UNCOMPRESSED PULSE MAX COMPRESSION WITH BARKER CODE (UNITY SIDELOBES) IS 13:1 (n=13) OTHER LONGER SIMILAR NON-CYCLIC CODES AVAILABLE

e.g., n= 28 ---- MAX SIDELOBE OF 2

Pulse Compression (con't)

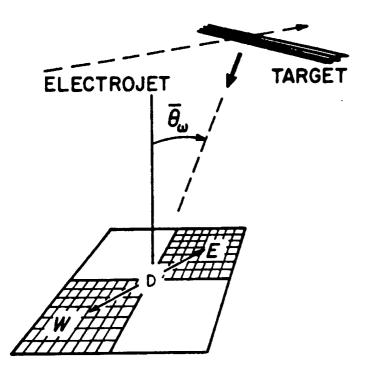
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All forms of pulse compression rely on careful use of phase information.

Hence, unknown significant Doppler shifts and/or phase decorrelation (soft targets) will seriously distort/destroy the compression. (These effects are described by the full radar "ambiguity function".)

For highly coherent, underspread targets, many other (than Bartrer) coding schemes are possible, some of which are very long and give very high compression ratios. e.g. complementary code pairs cyclic codes

### RADAR INTERFEROMETRY (Equatorial Geometry)



The geometry of the electrojet interferometer. The entire Jicamarca 50-MHz array was used for transmission, but the scattered signals were received separately on the east and west quarters, whose phase centers are separated by the distance D which is 208.2 m. The fieldaligned "target" is assumed to occupy a small range of angles centered about the small mean angle  $\theta_{\omega}$ , and the subscript  $\omega$ refers to the Doppler shift of the echo.

Simplest Situation (Single Target)

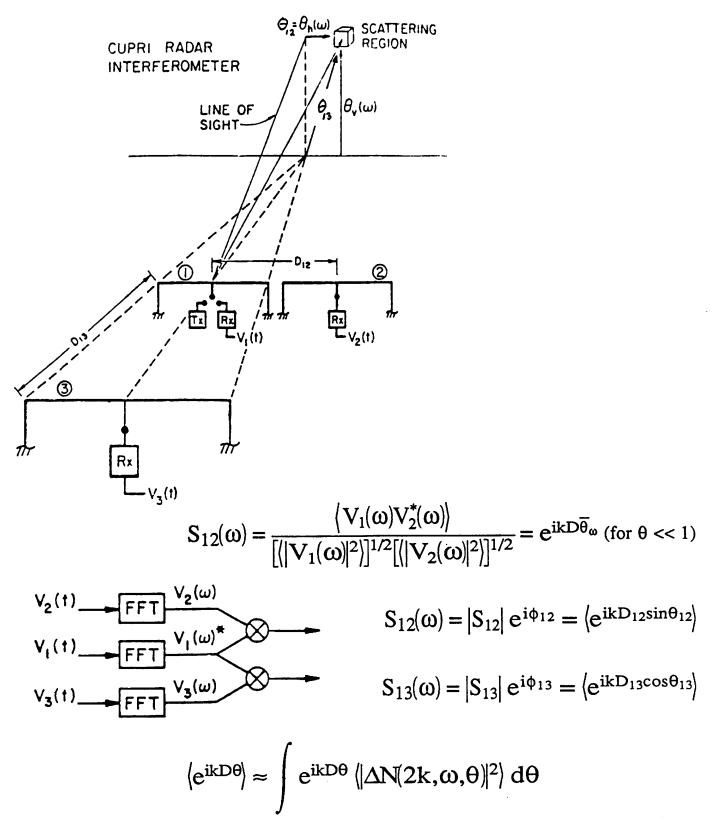
Suppose

$$V_{E} = V_{01} e^{i\omega t}$$
$$V_{W} = V_{02} e^{i\omega t - ikDsin\theta}$$
$$(k = 2\pi/\lambda radar)$$

Then

$$\frac{\langle |V_E V_W^*| \rangle}{\langle |V_E|^2 \rangle \langle |V_W|^2 \rangle^{1/2}} = e^{ikDsin\theta} \Rightarrow \theta \text{ and } d\theta/dt \Rightarrow \text{velocity}$$

In other words, the time delay between the arrival of the signal at the E and W antennas  $\Rightarrow$  a phase shift which  $\Rightarrow \theta$ . This idea can be extended to multiple targets with different Doppler shifts.



- For point targets, this is simply 2-D direction finding.
- For distributed targets, each baseline provides one point on the complex spatial ACF, which is the FT of the angular power spectrum.
- In both cases, the information is provided for each Doppler shift separately.

$$|S(\omega)| \cong e^{-(1/2)k^2 D^2 (\delta \theta_{\omega})^2} \equiv \text{coherence} \Rightarrow \text{size}$$

$$\phi(\omega) = kD \left\{ \begin{array}{c} \sin \overline{\theta}_{\omega} \\ \cos \overline{\theta}_{\omega} \end{array} \right\} \equiv \text{phase} \implies \text{position}$$

In the auroral case the 2-D, orthogonal baseline data can be combined to give contour plots which roughly indicate the shape of the scattering center.

Measuring the ACF of an overspread target (e.g. "incoherent" scatter)

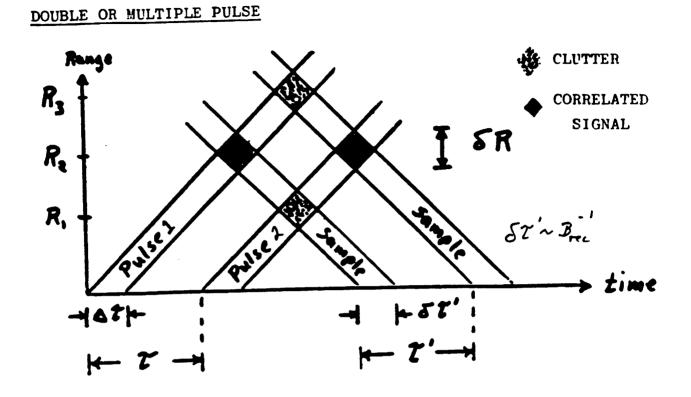
(apparently) How do we manage to violate, the Fourier Uncertainty Principle ?

We use the fact that signals from disjoint scattering volumes are completely <u>uncorrelated</u>.

The price for this:

We add "clutter" (c), or unwanted signal from other ranges, to the noise, This clutter is averaged out, but it increases the statistical errors

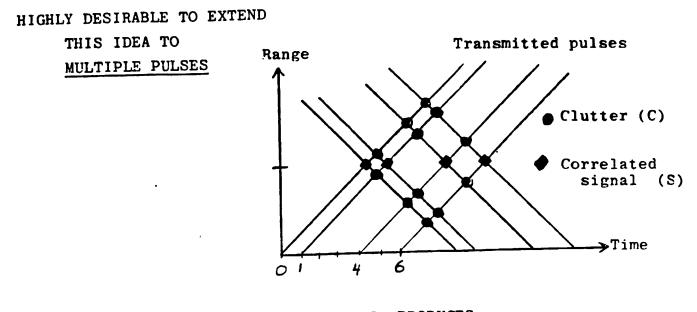
 $\delta_{\chi}^{2} \rightarrow \sim \frac{1}{H} \left( \frac{S + N + C}{c} \right)^{2}$ 



• SAMPLE PRODUCTS 
$$\rightarrow \langle \vee(R_2, t) \vee^{+}(R_2, t+2') \rangle \rightarrow \rho(R_2, 2')$$

- TRANSMIT (CYCLICLY) DIFFERENT SPACINGS AND SAMPLE AT ALL RANGES TO DETERMINE COMPLETE  $\rho(\mathbf{R}, \tau')$ OR USE MULTIPLE  $\mathcal{T}, \mathcal{T}'$ , AS WE SHALL SEE
- GOOD RANGE AND LAG RESOLUTION POSSIBLE
- CLUTTER (ECHOES FROM UNWANTED RANGES) ADDS TO NOISE
- CAN HAVE  $\mathcal{T} \neq \mathcal{T}'$  AND/OR  $\Delta \mathcal{T} \neq \mathcal{T}'$  (UNMATCHED FILTER) BUT NOT RECOMMENDED (LIKELY TO GIVE SYSTEMATIC ERRORS)
- MUST HAVE  $\mathcal{Z} \ge \Delta \mathcal{Z} + \mathcal{Z} \mathcal{Z}'$
- ➡ CLUTTER ECHOES CAN BE <u>ELIMINATED</u> IF PULSES 1 AND 2 HAVE ORTHOGONAL POLARIZATIONS (WITH MATCHING RECEIVER SYSTEM)

#### ACF (continued)



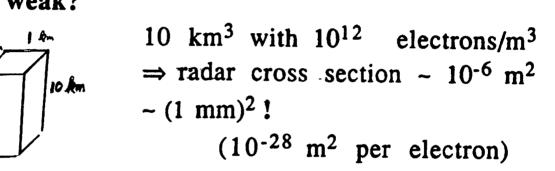
• EXAMPLE: 4 PULSES AT t = 0, 1, 4, 6 PRODUCES lags = 0, 1, 2, 3, 4, 5, 6 *L not useful - range a hased* 

- IN GENERAL: n PULSES  $\rightarrow$  n(n-1)/2 DIFFERENT LAGS
- SOME "MISSING" LAGS FOR n > 4
- CLUTTER POWER ~ (n-1) x SIGNAL POWER
- SAME ADVICE AS IN DOUBLE PULSE CASE FOR  $\mathcal{L}$  vs  $\mathcal{L}'$ ,  $\Delta \mathcal{L}$  vs  $\mathcal{J} \mathcal{L}'$ ,  $\mathcal{L}$  vs  $\Delta \mathcal{L} + \mathcal{J} \mathcal{L}'$
- BEST TO MAKE n AS LARGE AS POSSIBLE, CONSISTENT WITH THE VARIOUS CONSTRAINTS OF PULSE LENGTH, ETC., <u>IF</u> COMPUTER CAN HANDLE THE INCREASED PROCESSING
   STATISTICS IMPROVE EVEN THOUGH CLUTTER INCREASES — ESPECIALLY IF S/N << 1 AND HENCE C ≤ N</li>
- CANNOT USE ORTHOGONAL POLARIZATION TECHNIQUE TO ELIMINATE CLUTTER
- CANNOT USE MULTIPLE FREQUENCIES EITHER (ELIMINATES CLUTTER, BUT ALSO SIGNAL!)
- SAME IDEA USED IN "NON-REDUNDANT" ANTENNA ARRAYS FOR APERTURE SYNTHESIS. SOME REDUNDANCY OK IN ANTENNA ARRAY CASE, BUT NOT FOR RADAR ACF MEASUREMENT (GIVES RANGE ALIASING)

What is it?

*Extremely* weak scatter from electrons that are as unorganized as possible (usually not totally "incoherent" in some sense - but don't worry about this refinement now).

How weak?



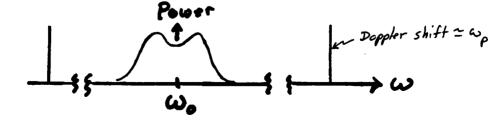
But can be "easily" detected, nevertheless, with a (W.E. Gordon, K.L. Bowles, 1958) <u>powerful</u> radar

Theory

•Linear plasma kinetic theory

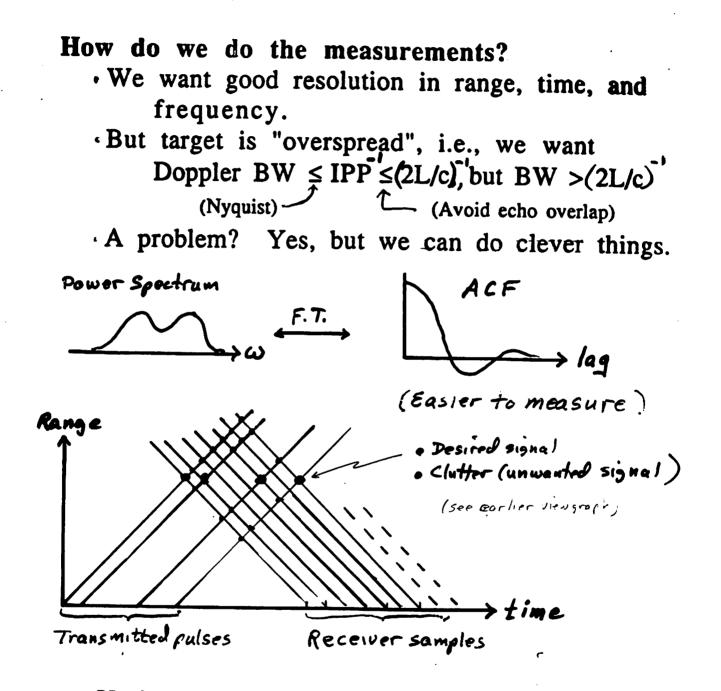
•Thoroughly worked out

•Very rich - spectrum of scattered signal depends on many plasma parameters



•Shape and total power ⇒ N<sub>e</sub>, T<sub>e</sub>, T<sub>i</sub>, V<sub>d</sub>, ... etc. ion composition (incl. negative ions) V<sub>en</sub>, differential ion drifts, currents (Ve-Ve,

IS (continued)



- Various coding schemes and lag sequences used • Individual pulses may be "compressed" (a.
- Individual pulses may be "compressed" (e.g. Barker coding)

# IS (continued)

Choice of lag spacing or further coding + statistical averaging ↓ Range "clutter" (echoes from the "wrong" altitude) eliminated since echoes from different regions of space are uncorrelated

## **ERRORS**

$$E^{2} \simeq \left(\frac{S+N+C}{S}\right)^{2} \frac{1}{K}$$

K = number of <u>independent</u> samples S = signal power N = noise power C = clutter power

# ANALYSIS

Least square fitting of theory to data ⇒ ionospheric parameters Fitentire profile at one time? (OASIS program) IS (continued)

Questions:

- •Non-Maxwellian plasmas (high latitudes)?
- •IS from unstable plasmas (high latitudes)? Yes, apparently, for k well inside stable regime.

# What can we study using IS?

- · Energy balance and Tn
- . Photoelectron energy distribution, including arrivals from conjugate hemisphere
- Low and mid latitude winds, tides, gravity waves, TIDs  $V_d = \frac{E \times B}{2}$
- -E fields, conductivities, dynamo theories  $\overline{I}$
- High latitude winds, ion drag, magnetospheric forcing
- •Magnetospheric convection, response to changes in the IMF and solar wind
- ·F region trough dynamics
- · Ion chemistry, composition transitions
- ·Ionosphere-magnetosphere coupling (fluxes
- of particles and energy) • Ion drift vs neutral winds (airglow) • High latitude heating events (natural)
- Artificial (HF) heating experiments

Altitudes covered and Resolution for IS.

h: ~ 80 Am (even less sometimes) to several × 10<sup>3</sup> Am

Dh: ~ 150m (1 us pulse) (Fresión, cooled pulses) to ~ 150 km (1 ms pulse) at high alts.

At: ~ few sees to ~ 1 hr

# IS (continued)

- IS is the most powerful ground based technique for monitoring most of the important parameters of the ionosphere.
- Rapid improvements in DSP technology mean that we should soon be able to exploit the full potential of the method (years ago 90-99+ % of the data was sometimes wasted).
- There are many global IS observing programs associated with CEDAR, e.g. GISMOS (substorms) GITCAD (ionosphere-thermosphere coupling) LTCS (lower thermosphere coupling) SUNDIAL (not an acronym!) WAGS (gravity waves) CHARM (hydrogen) MISETA (equatorial) ATLAS

# IS (continued)

# **RECENT TOPICS**

Non-Maxwellian ion distributions at high latitudes when drift velocity large.
Can you observe IS looking along B while unstable waves are being generated with k nearly ⊥ B? Evidence seems to ⇒ Yes.
Ionosphere is changing rapidly now with increasing solar activity.
Digital data processing power improving

rapidly. Cheap way to improve observatories.

## **NEW OBSERVATORIES?**

USSR EISCAT receiving station (VHF) Svalbard (Spitzbergen)? Japan? UK? Resolute Bay, Canada? Fairbanks, AK? Indonesia? (Japan) Other USSR observatories?

# TIMETABLE?

- Any new high latitude radars should be ready by the time of the "Cluster" multisatellite launch in ~ 1995 if at all possible.
- So time is pretty short.