

1991 CEDAR Workshop  
NIST Auditorium, Boulder, CO  
2-5PM Tuesday, June 18, 1991

Optics Short Course

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University of Alaska at Fairbanks

# Optics Tutorial

(Featuring Hernandez, Romick and Smith)

**Tuesday Afternoon**

**NIST Auditorium 2.00pm - 5.00pm**

**4 Sessions starting at:-**

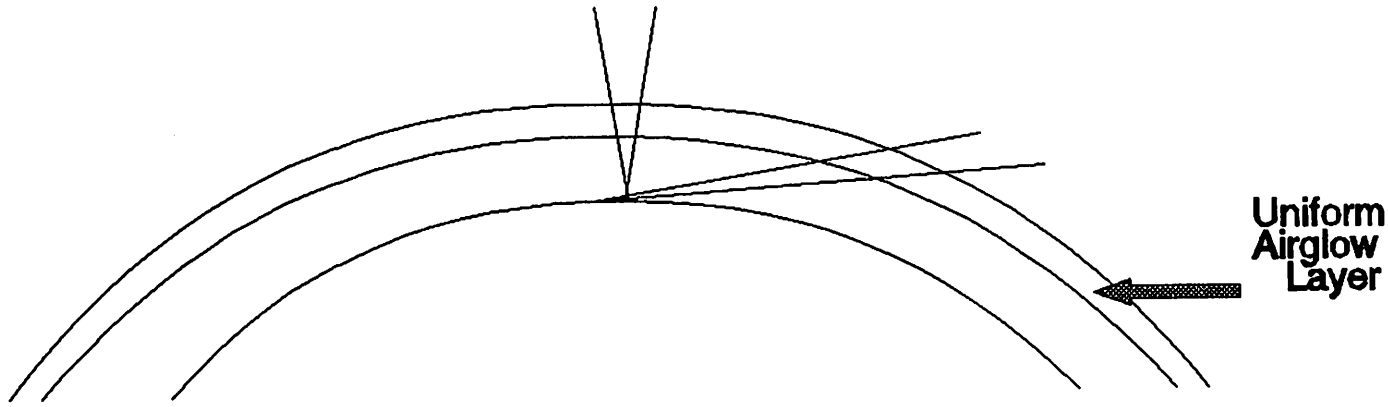
**2.00pm: Optics in Aeronomy**

**3.00pm: Imaging the atmosphere**

**3.45pm: Observing lines and bands**

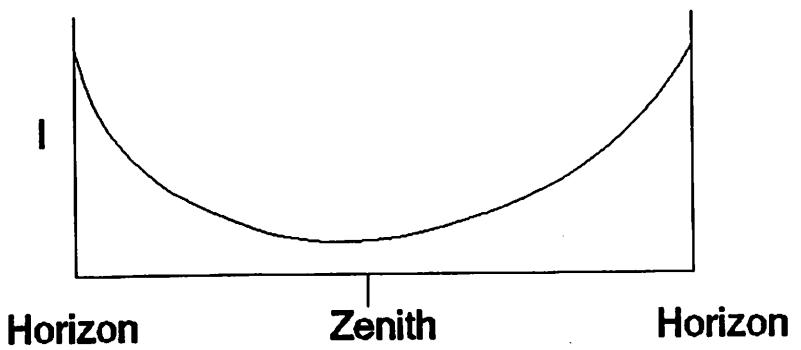
**4.30pm: Doing dynamics optically.**

# The View of a Ground Based Instrument

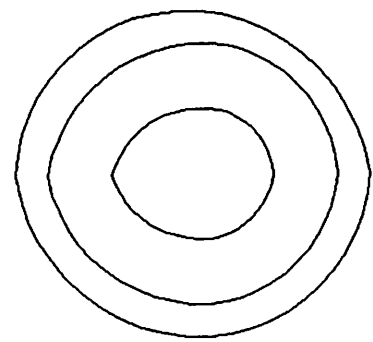


## The van-Rhijn Effect

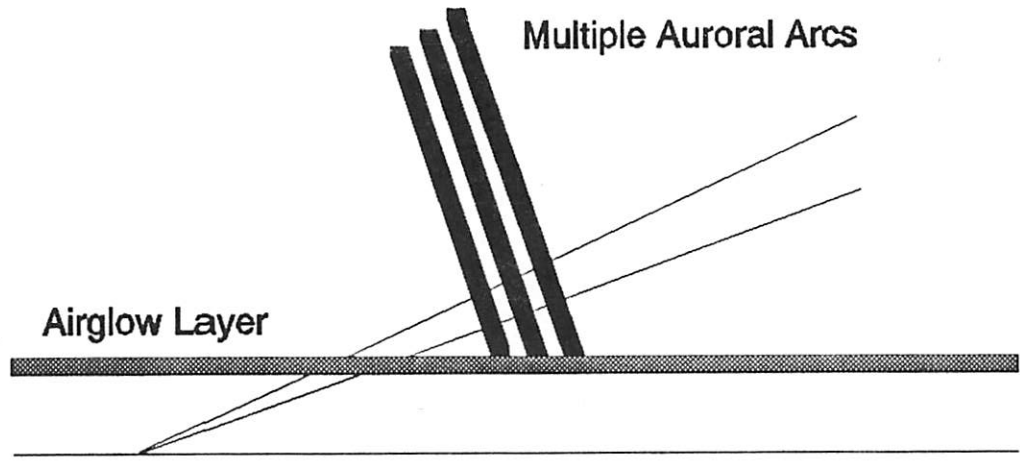
Meridian Scan Mode



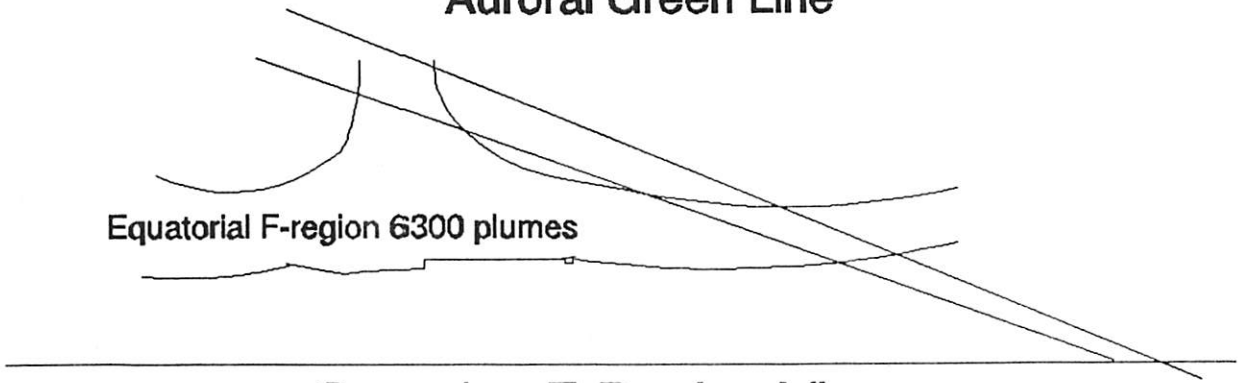
## Alt-Azimuth Scan



Isophote map

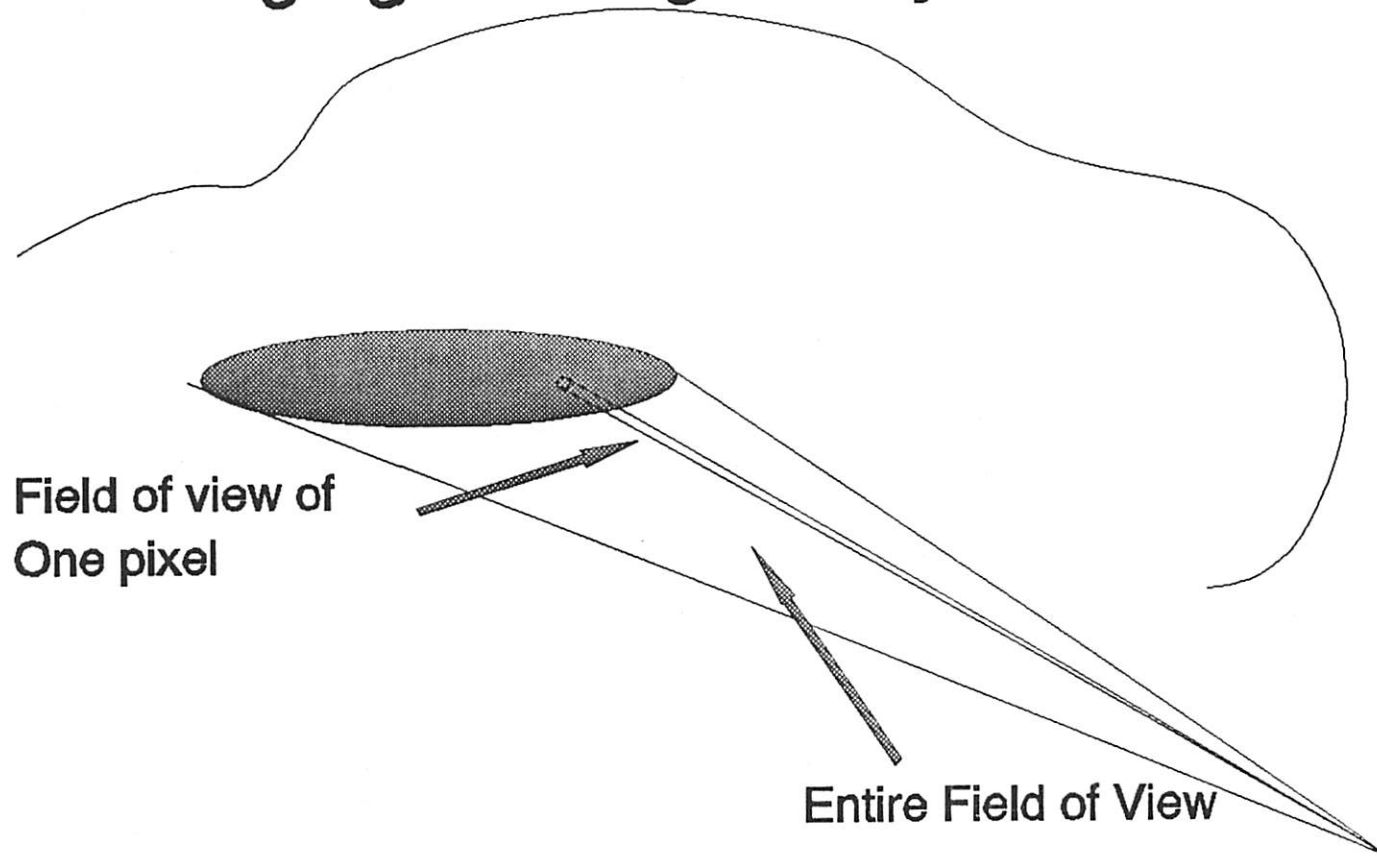


Ground-based view  
of  
Auroral Green Line



Complex F-Region View

# Imaging the airglow layer

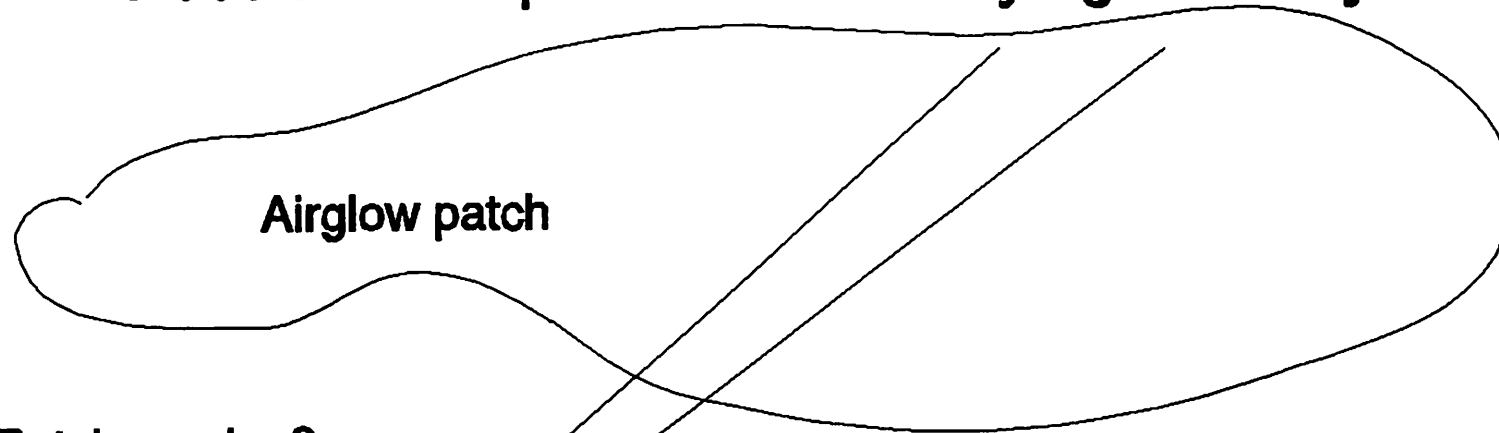


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$$\text{Signal seen} = \frac{A\Omega}{4\pi} R \times 10^6 \text{ Photons per second}$$

Small pixels receive a weak signal, require more time.

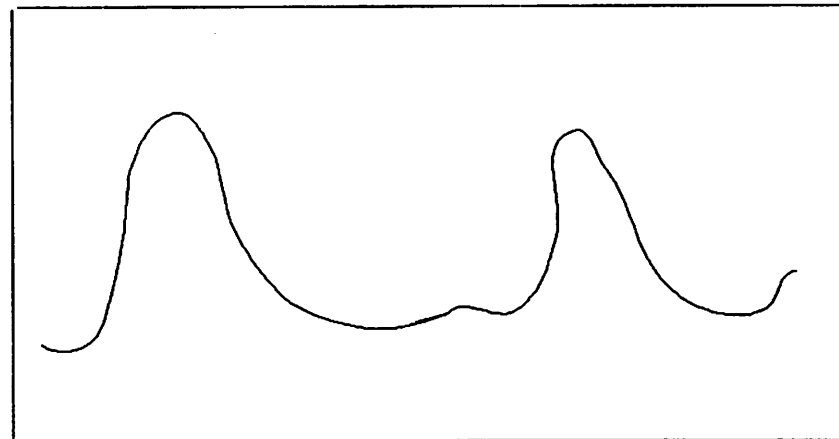
# Possible Interpretations of Varying Intensity



**Airglow patch**

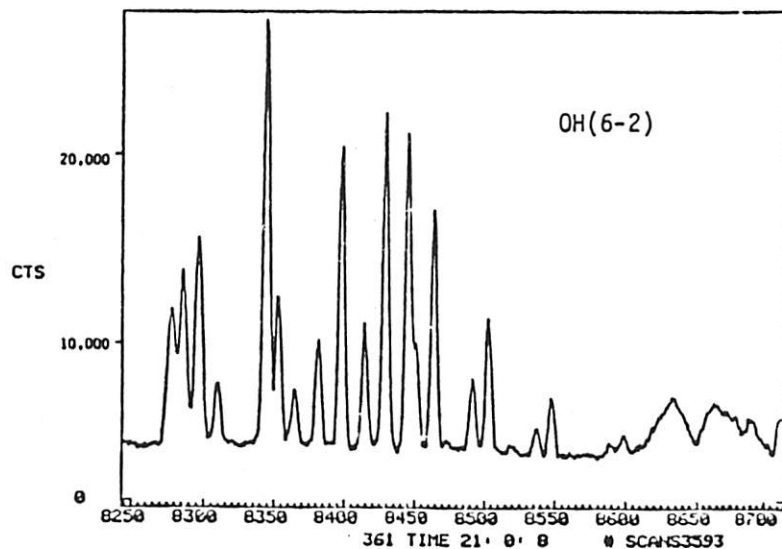
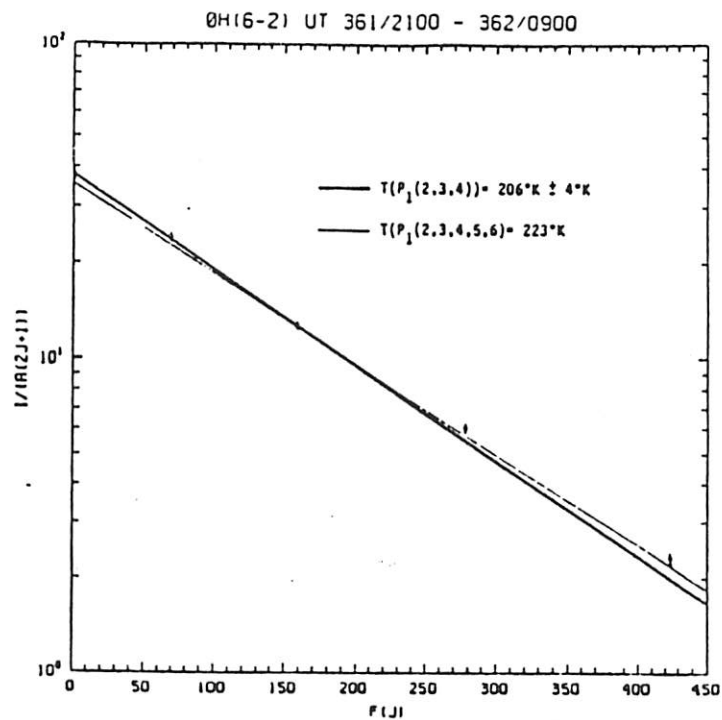
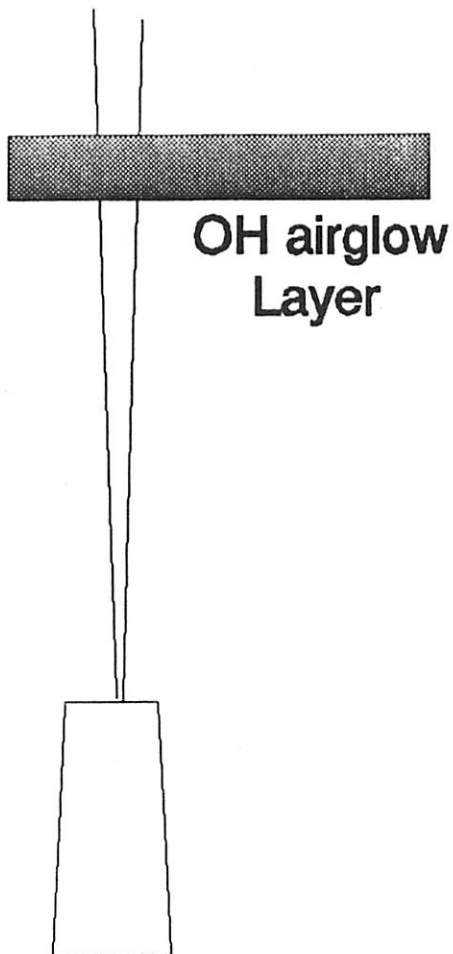
**Patch moving?  
Patch changing  
Intensity ?**

**Intensity**

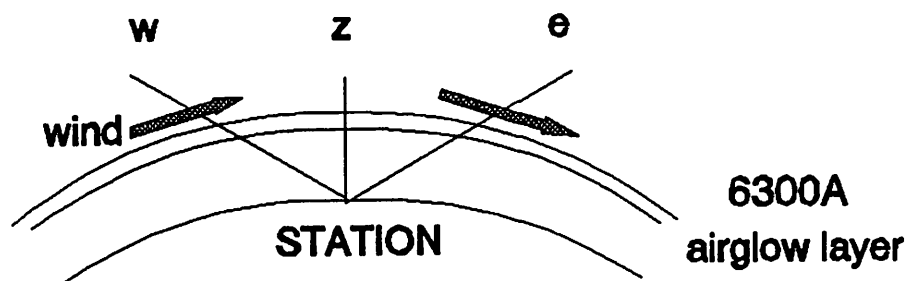


**Time**

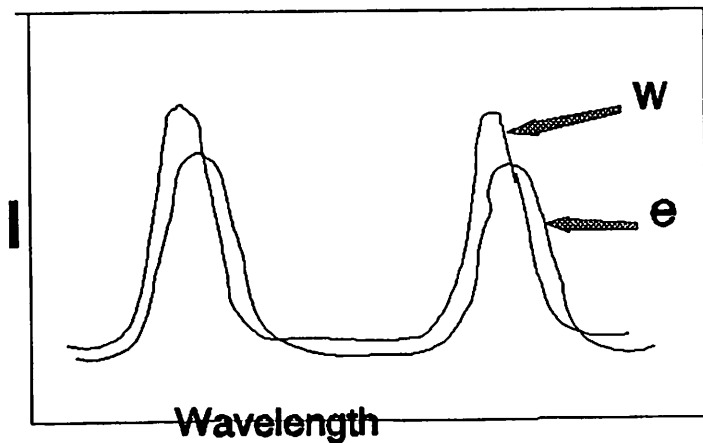
# Observations with a Medium Resolution Spectrometer



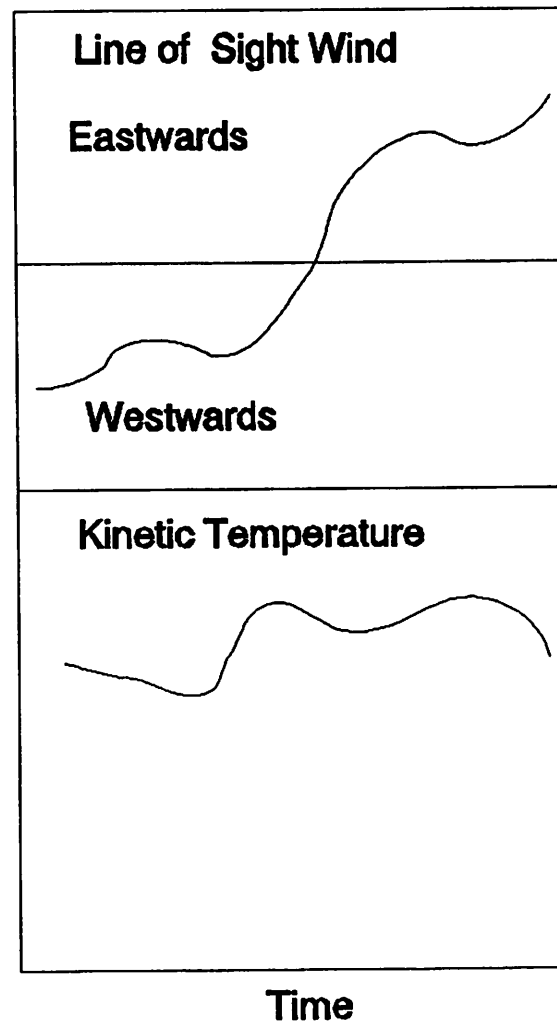
## Observing Geometry



## Observed Spectra from a Fabry-Perot Spectrometer

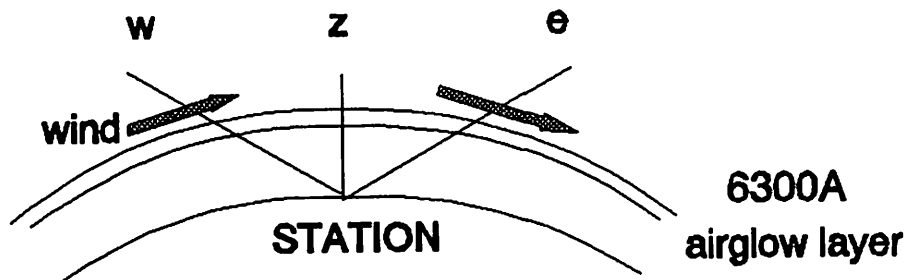


## Dynamics Data (for each direction of view)

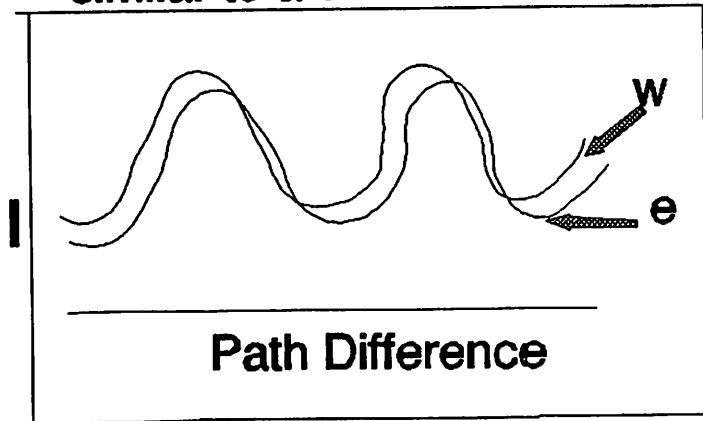




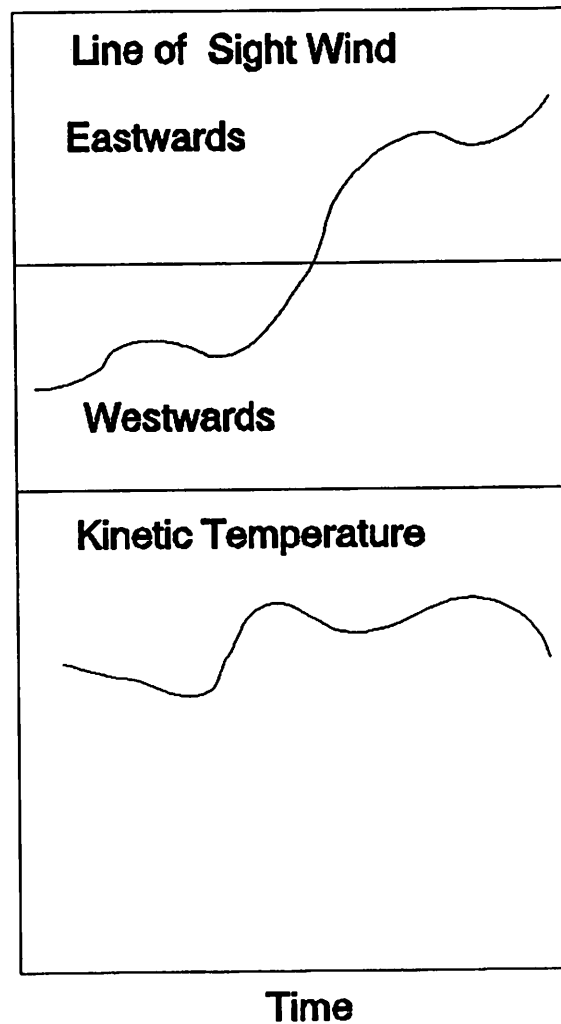
# Observing Geometry



# Observed Spectra for a Michelson Interferometer similar to a WAMDII



# Dynamics Data for each pixel in fringe image

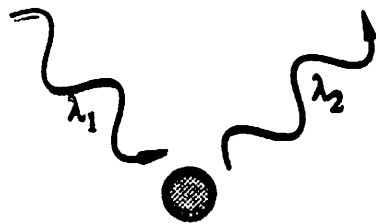


Wave length Resolved Emissions

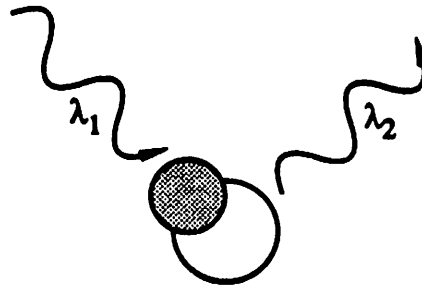
can be used to identify  
the particular radiating  
atom or molecule.

Other conditions lead to  
information about the  
excitation process.

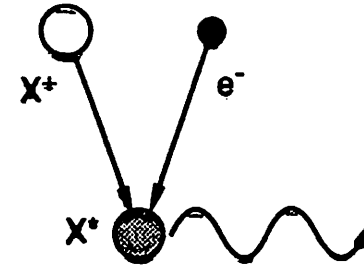
*Identification of the Emitter Through*  
**ATMOSPHERIC RADIATION PROCESSES**



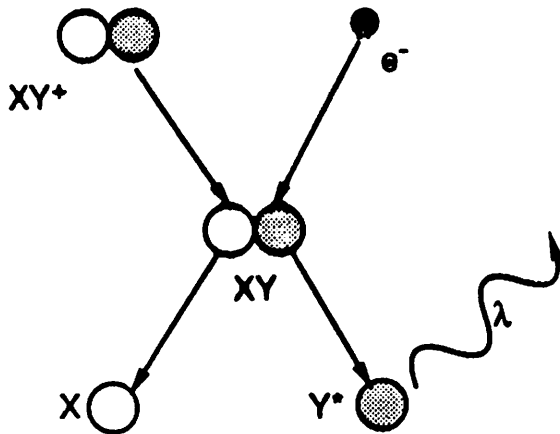
**Resonant Scattering**  
 $\lambda_1 = \lambda_2$



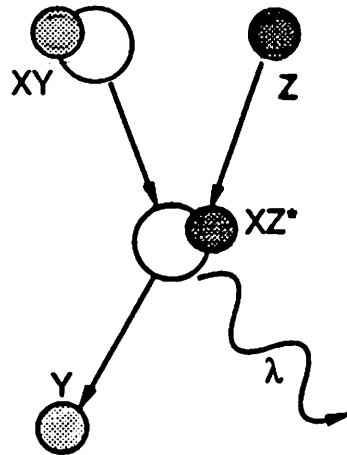
**Fluorescent Scattering**  
 $\lambda_1 < \lambda_2, E_1 > E_2$



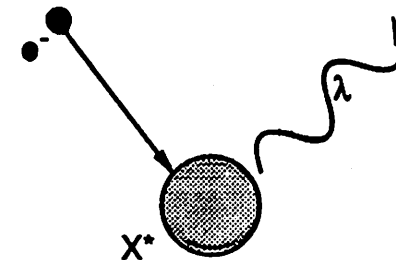
**Radiative Recombination**



**Dissociative Recombination**

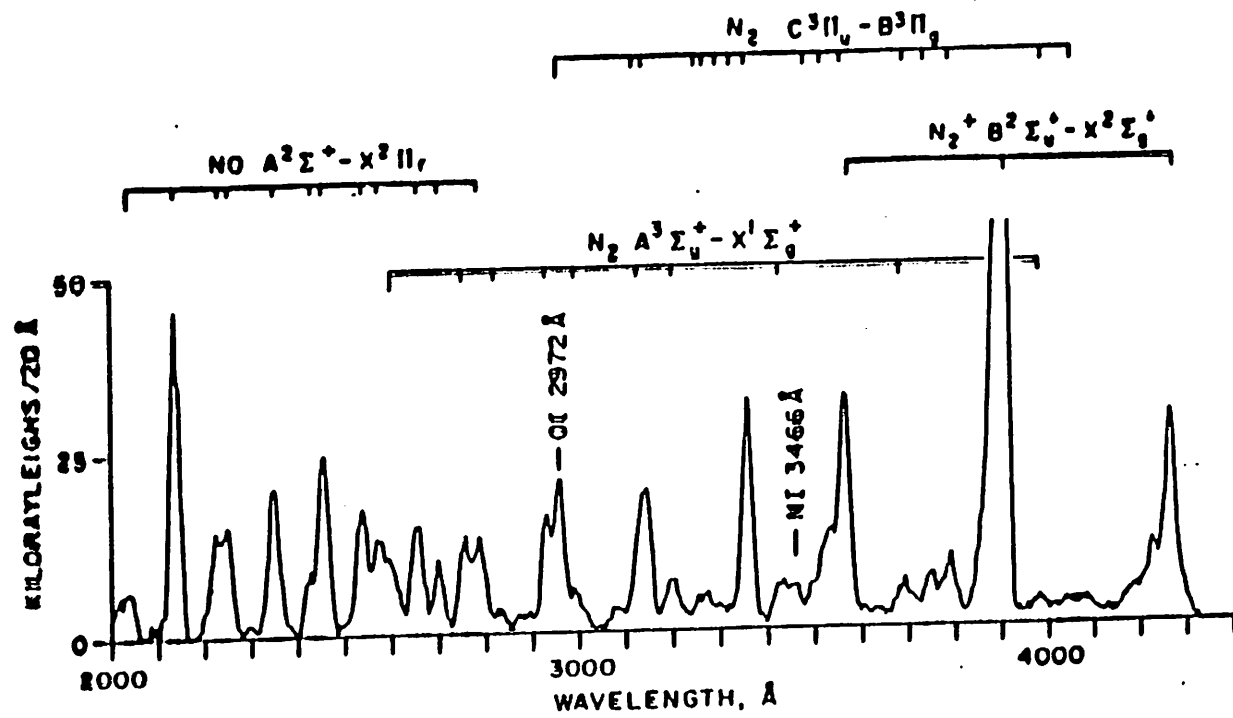


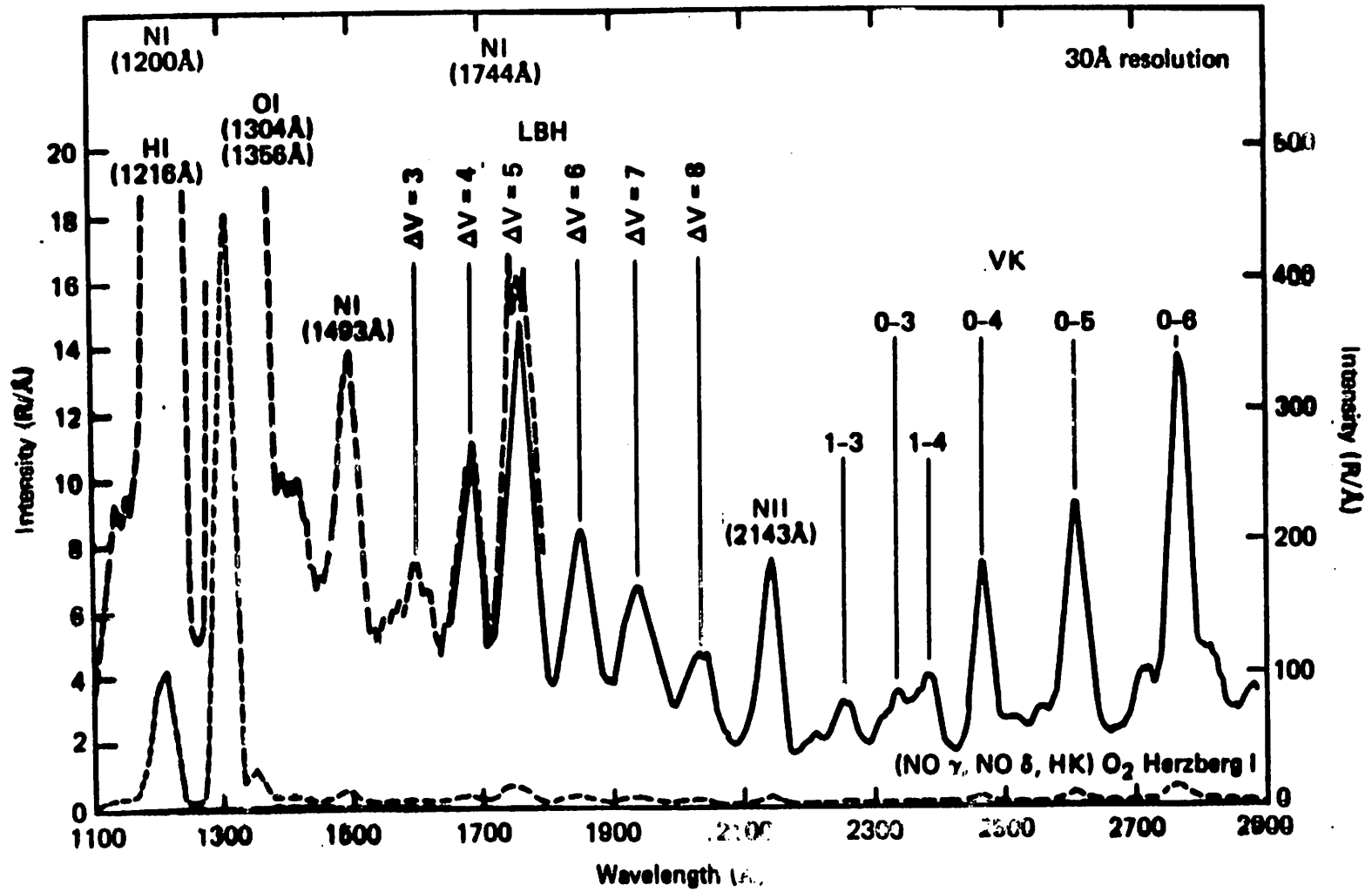
**Chemiluminescence**



**Electron  
Impact  
Excitation**

Excitation Conditions	Basic Process
Dayglow	Solar EUV and Photoelectrons
Twilight	Mixture - decay processes and Chemistry - Conjugate photoelec.
Nightglow	Chemistry and Conjugate photoelectrons
Aurora	All types of energetic particles





Objective	Observable	Approach	Mode
<b>Neutral Composition</b> -Day atomic O  -Day N <sub>2</sub> -Day O <sub>2</sub> -Night O -Global dynamics -Air density	OI 130.4, 164.1 nm OI 130.4, 135.6 nm N <sub>2</sub> VK bands N <sub>2</sub> LBH, 2PG bands N <sub>2</sub> LBH bands O <sub>2</sub> Herzberg I He 58.4 nm Rayleigh scattering	Line ratios Line ratios Quenching Emission peak Absorption O <sub>2</sub> SR O+O He density Limb scans	E,L E,L L E,L E,L E,L L L
<b>Ionization rates</b> -O+hp,e -N2+hp,e	OII 83.4, 61.7 nm NII 108.5, 91.6 nm	Rate from intensity Rate from intensity	L L
<b>Photoelectron fluxes</b>	N <sub>2</sub> LBH, 2PG	Combine with model	E,L
<b>Minor species</b> -Day NO -Day N -Day Mg -Day/night H -Day He -Night N -Night NO	NO γ 215 nm NI 149.3, 174.3 nm MgI,II 285.2, 279.8 nm HI 121.6, 102.6, 656.3 nm HeI 58.4 nm NO δ bands NO <sub>2</sub> continuum	Fluorescent scattering Electron impact Resonant scattering Resonant scattering Resonant scattering N+O N+O	N E,L L L E,L L E,L E,L

E= Earth-viewing spectrographic imager makes measurement  
 L= Limb-viewing imaging spectrograph makes measurement

Objective	Observable	Approach	Mode
<b>Electron density</b> -Day -Day -Day/Storm -Night -Night -F layer height	OII 83.4 nm OII 61.7, 54.0 nm OI 135.6 nm, N <sub>2</sub> LBH OI 91.1, 130.4, 135.6 nm OI 630 nm OI 130.4, 135.6, 630 nm	multiple scattering line ratios N <sub>e</sub> from O/N <sub>2</sub> ratio O <sup>+</sup> +e O <sub>2</sub> <sup>+</sup> +e Hgt from line ratios	L L E L E,L E,L
<b>Gravity waves and Wave number spectra</b>	OH (6,2) 825-860 nm OH Meinel O <sub>2</sub> ATM OI 557.7 nm	line ratio and spatial variations	E,L E,L E,L E



Objective	Observable	Approach	Mode
Polar mesosph clouds	ice	Mie scattering	E,L
Auroras	all bands	Particle precipitation	E,L
Energy deposition -Electrons  -Protons -Solar EUV	N <sub>2</sub> 2PG, LBH; N <sub>2</sub> <sup>+</sup> 1NG OI 297.2, 557.7, 630 nm OI 844.6 nm HI 121.6, 486.1 nm Dayglow	Electron impact Electron impact Electron impact Proton impact Photoelec. production	E,L E E E L
Neutral temperatures -Day  -Night	O <sub>2</sub> ATM OI 135.6 nm, N <sub>2</sub> LBH, 2PG OH Meinel, O <sub>2</sub> ATM	Band profile Scale height Band profile	E,L L E,L

There are very few cases where there is a simple direct relationship between a particular emission and the density of the emitter. Thus models enter as necessary linkages between observed emissions and derived parameters.

There are some studies  
that do not need quantitative  
intensity measurements or  
derived constituent densities.  
Morphological studies from  
images have contributed a  
great deal towards our understanding  
of the auroral oval.

POLAR BEAR AMBROAL IMAGE

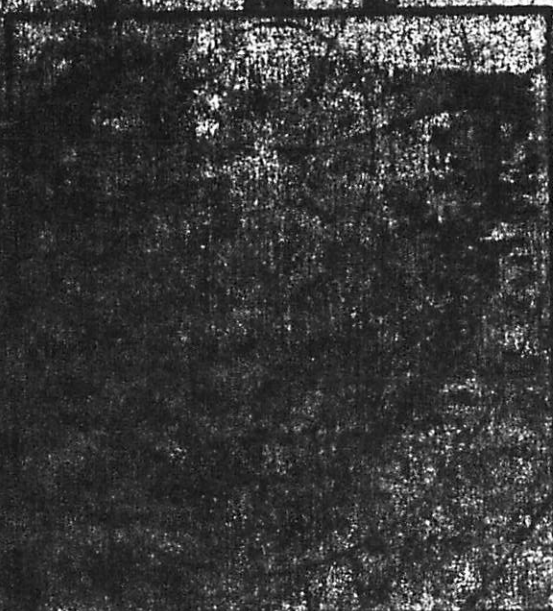
1500

SOURCE

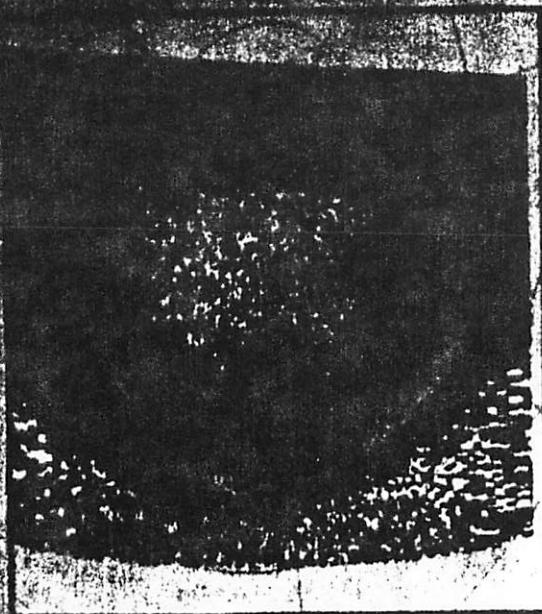
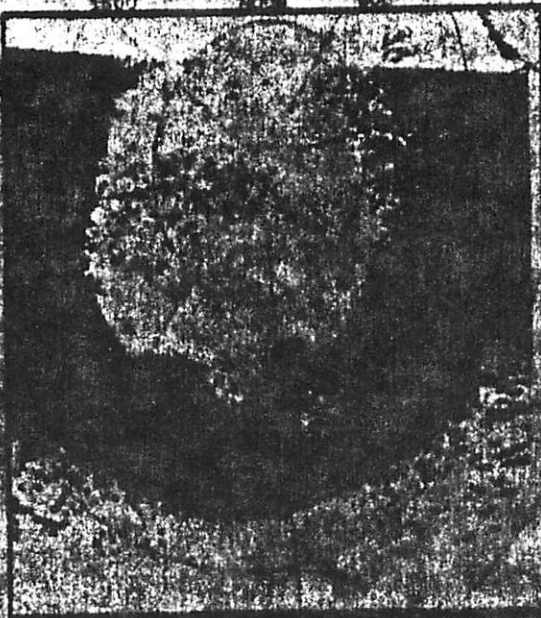
1500

201288

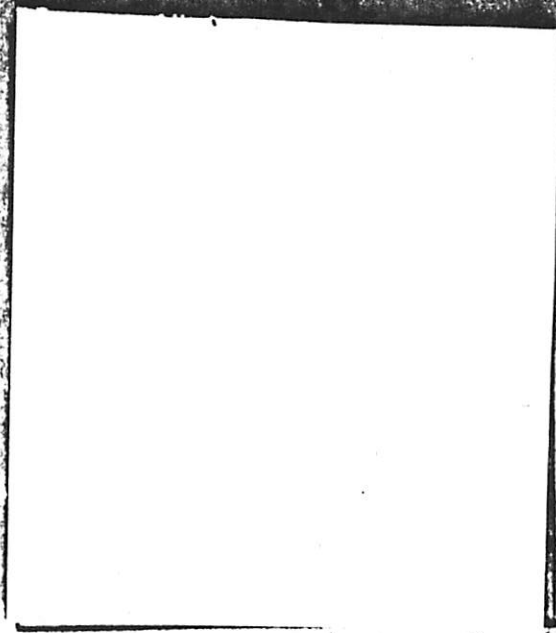
1000



RAYLENS



RAYLENS



28 JAN 1987 (DAY 28) 4: 5: 35 - 4: 16: 54

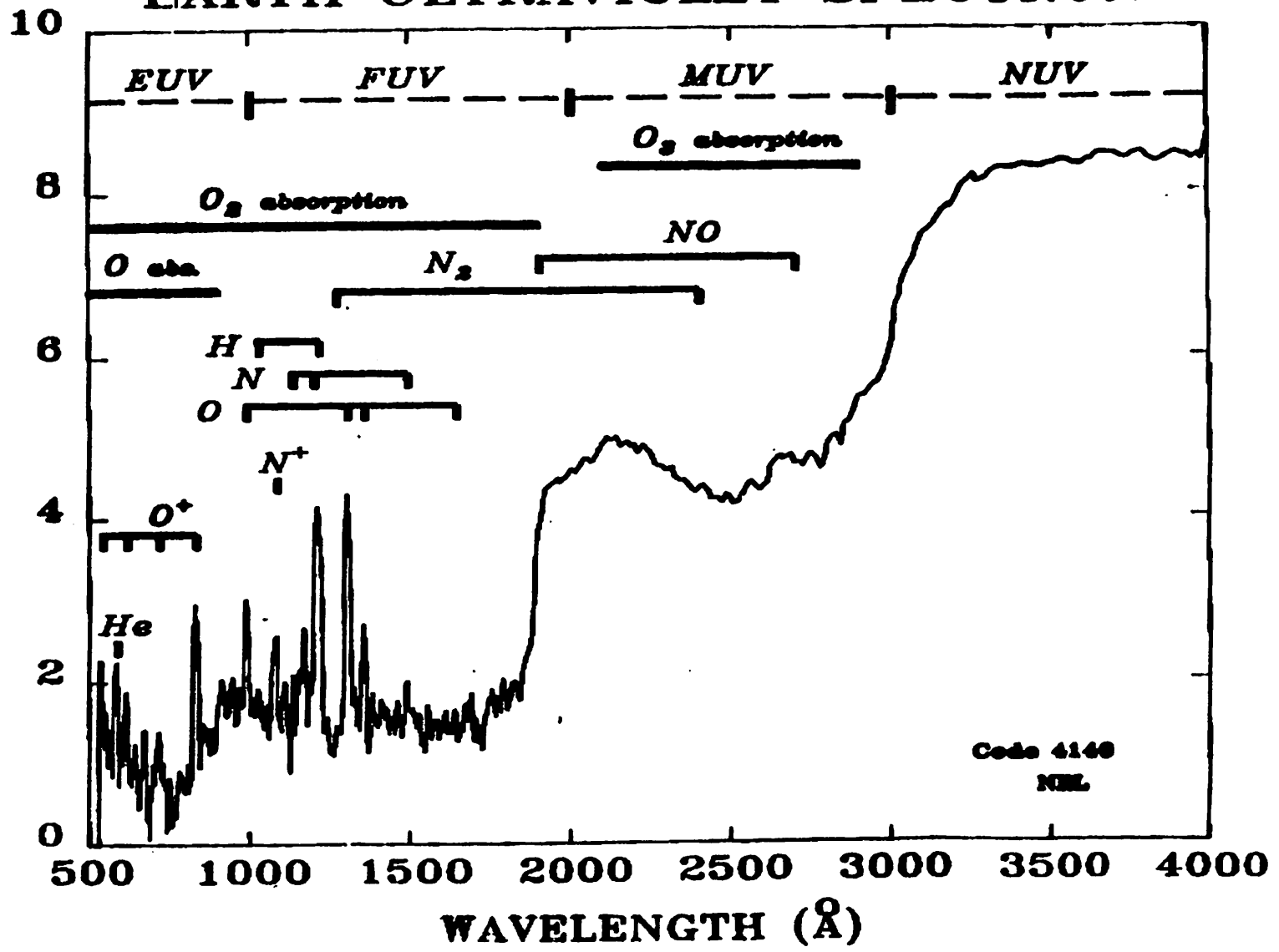
To cover all of the quantitative studies using optical observations is beyond the scope of this short course.

As examples I will concentrate on some DAYGlow observations and derived quantities.

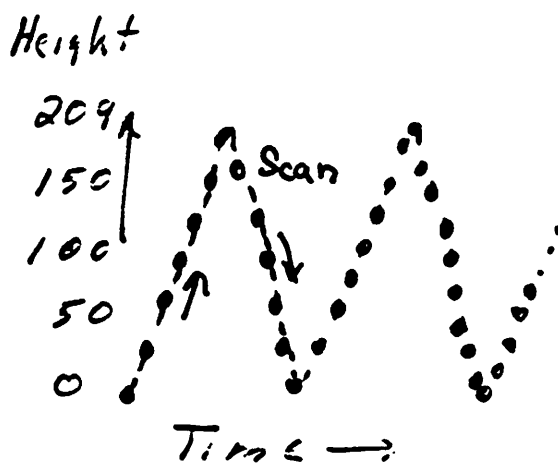
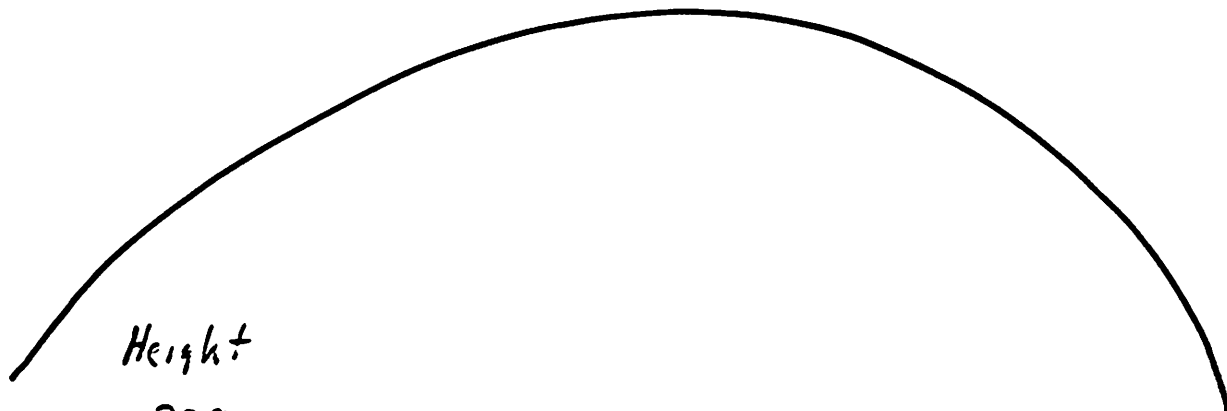
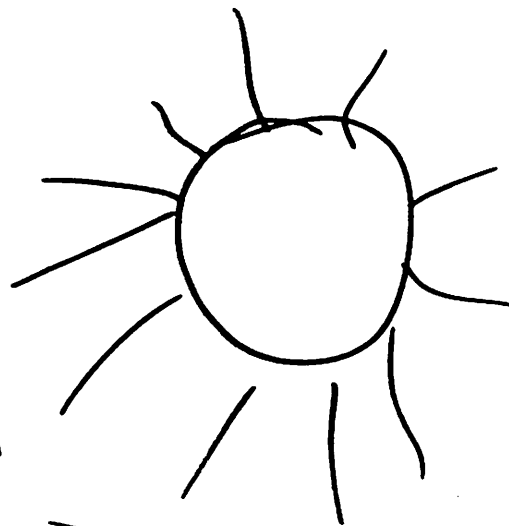
11:52 AM \*APL JHU LAUREL

# EARTH ULTRAVIOLET SPECTRUM

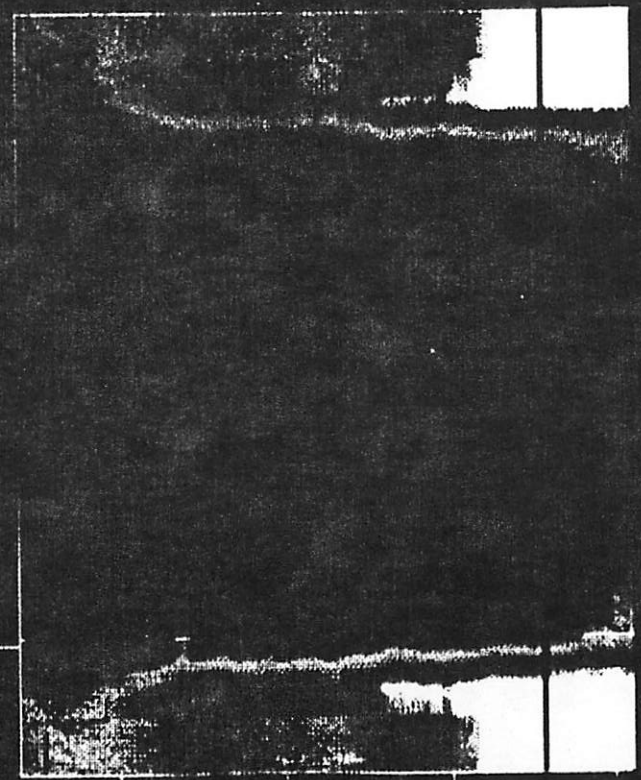
LOG INTENSITY (Rayleigh/10 Å)



# Satellite Limb Scan



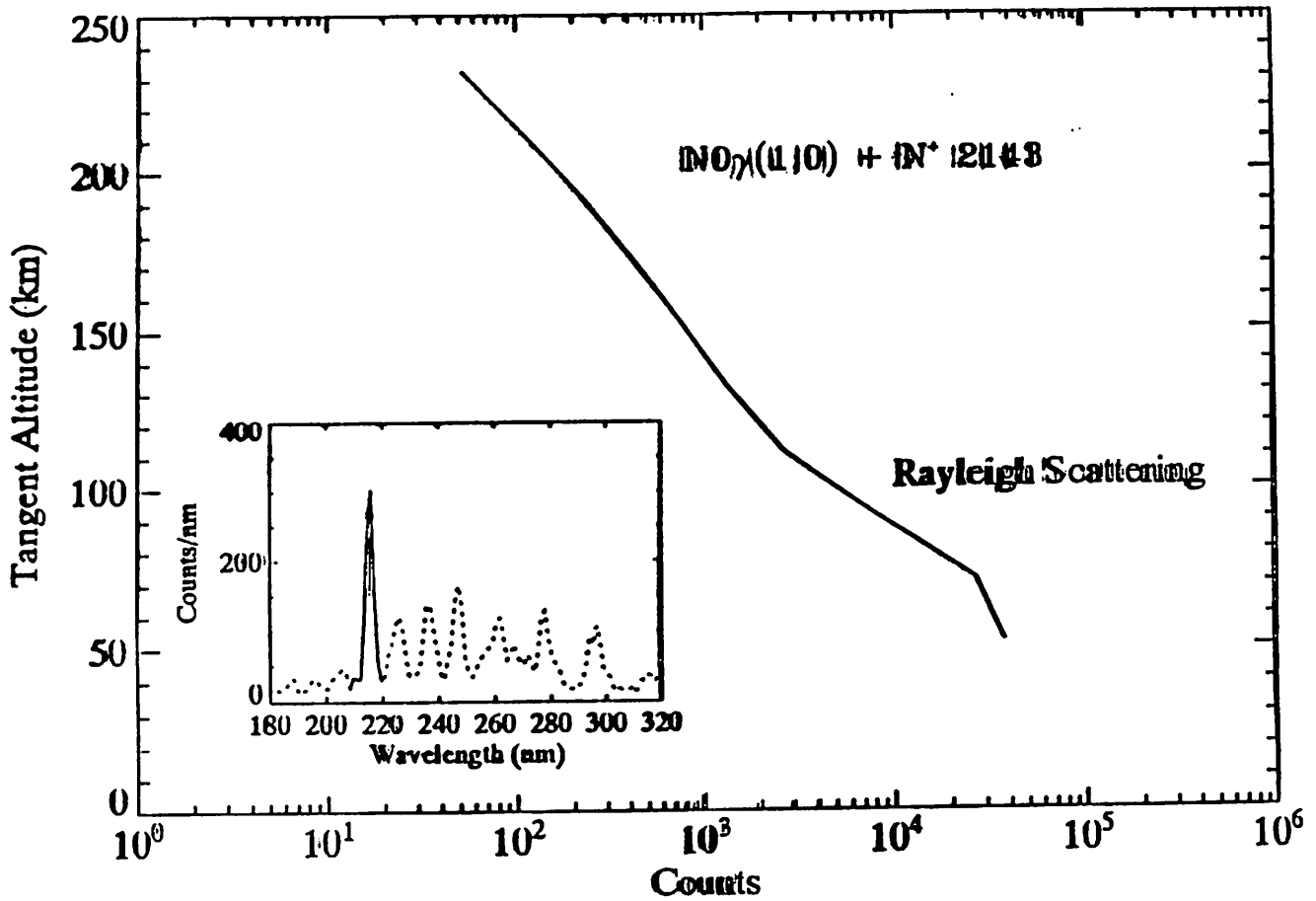
ALL INFORMATION CONTAINED



END



(noon)



(Analysis from CPI and JHU/APL)

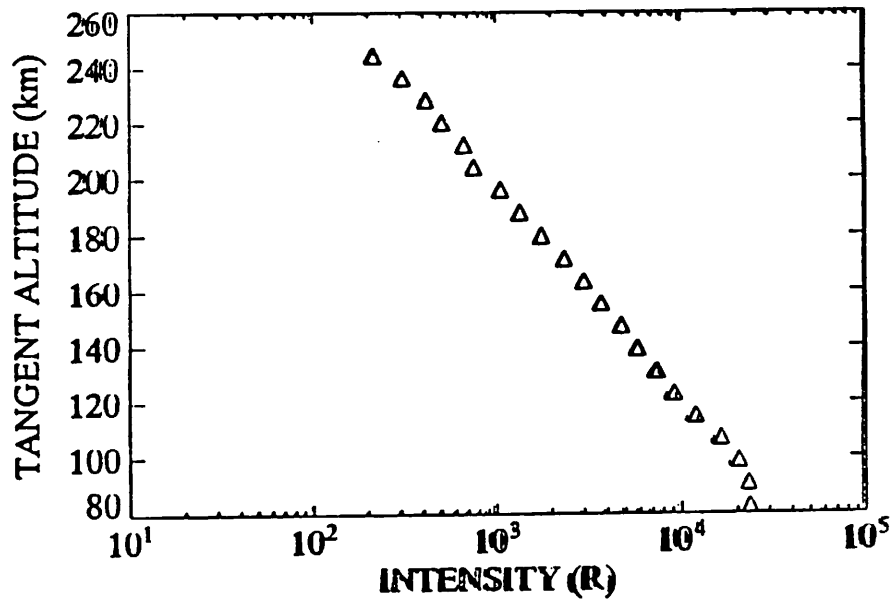
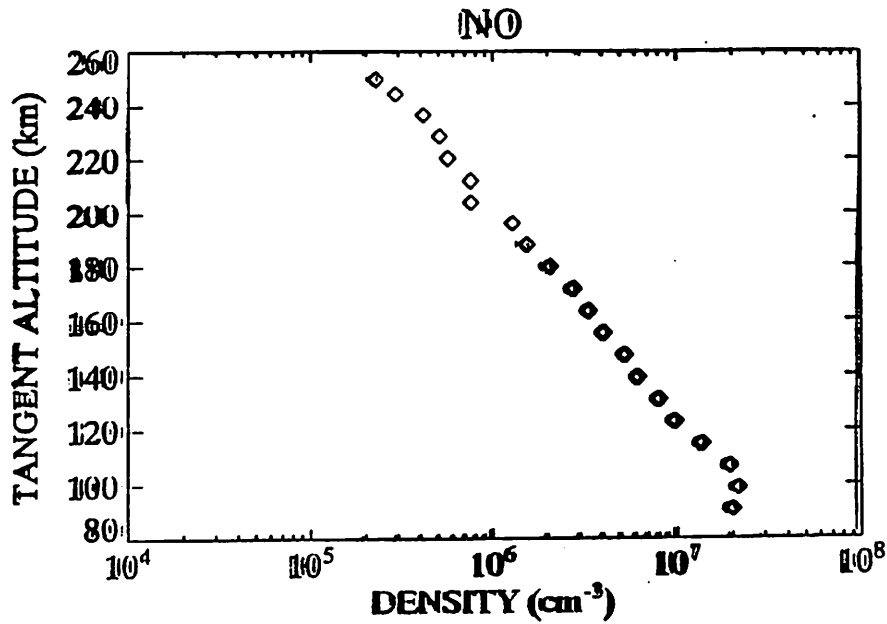
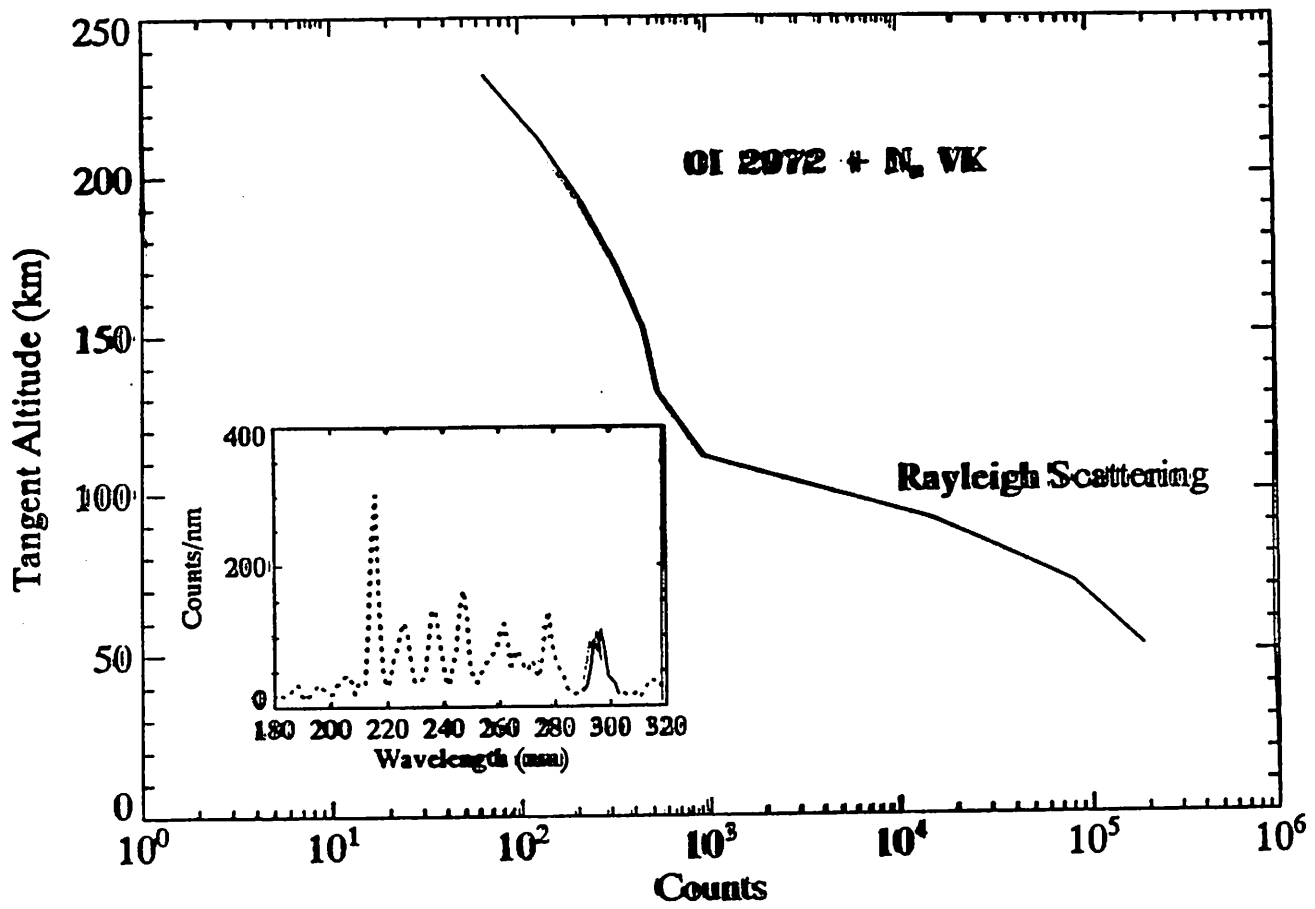
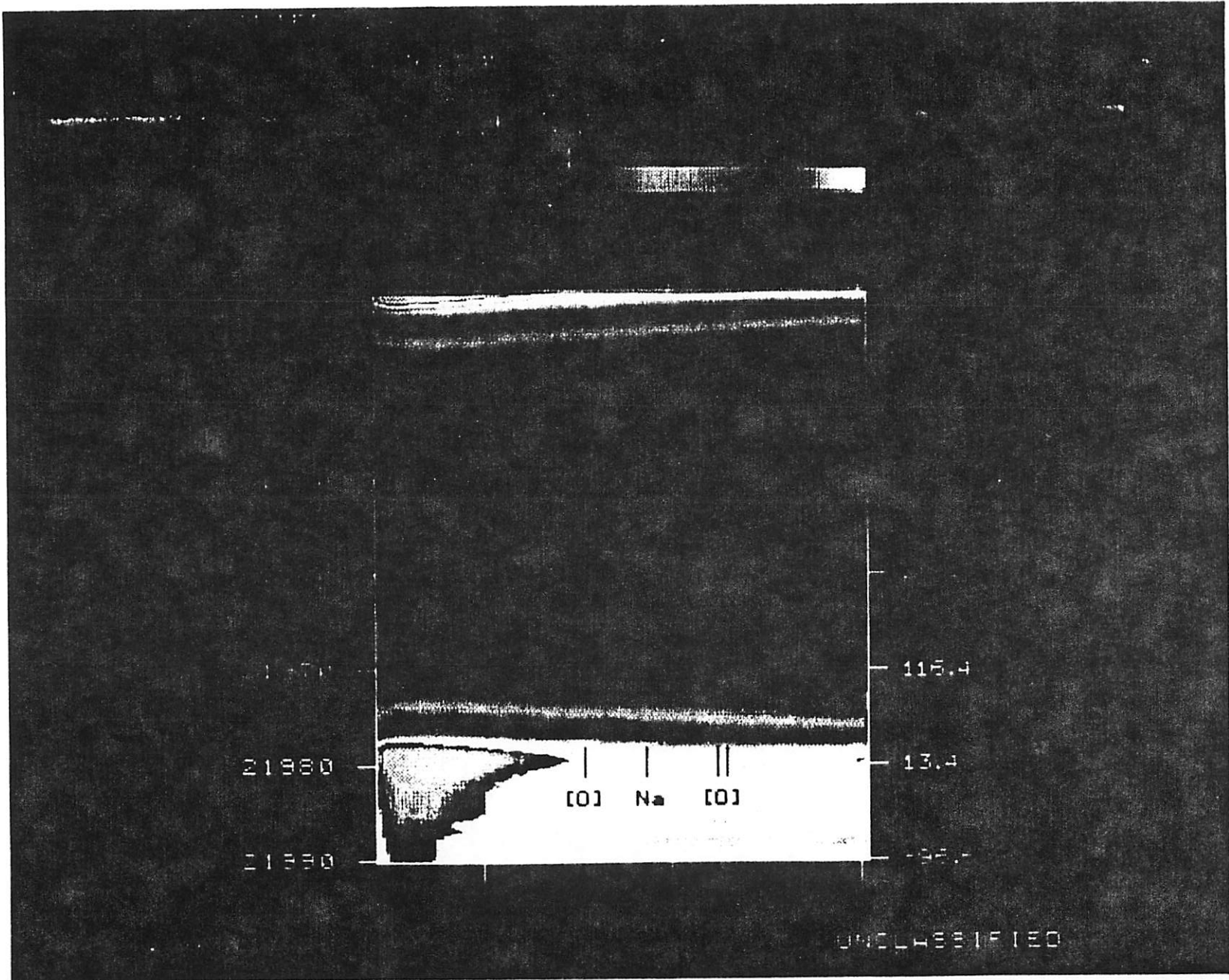


Figure 17 - Conversion of a reduced earth limb dayglow observation of the NO intensity into a NO density profile.

*(ANALYSIS FROM CPI and JHU/APL)*



( Analysis from CPI and JHU/APL )



### SUMMARY

The MUV dayglow observed from a low earth orbiting satellite at 2.8 nm resolution have been analyzed. Theoretical radiances were calculated utilizing a dayglow energy deposition and radiance model. Comparison of theory and data below a tangent altitude of 180 km shows that the emission is dominated by Rayleigh scattering. As the tangent altitude rises spectral signatures of NO, N<sub>2</sub>, O<sup>+</sup> and O appear. Analysis of these emissions shows that the observed emission is consistent with currently accepted ion-neutral chemistry in the mesosphere and lower thermosphere.

The NO density deduced compares well with SME results and shows an apparent scan-to-scan variation which implies very short time scale variations in the radiation field and/or NO density. The theory consistently overestimates the data near 205 nm where both NO and N<sub>2</sub> LBH emit radiation. The good fit to the remaining N<sub>2</sub> LBH data provides a measure of magnitude of the solar EUV energy deposited in the thermosphere. The deduced NO density above 110 km is used as input to the ion-neutral chemistry model which calculates the O(<sup>1</sup>S) and O(<sup>1</sup>D) excitation rates. The neutral density background atmosphere was calculated with MSIS86 for the solar and geomagnetic conditions appropriate to the measurements. No scaling of the MSIS86 densities were required.

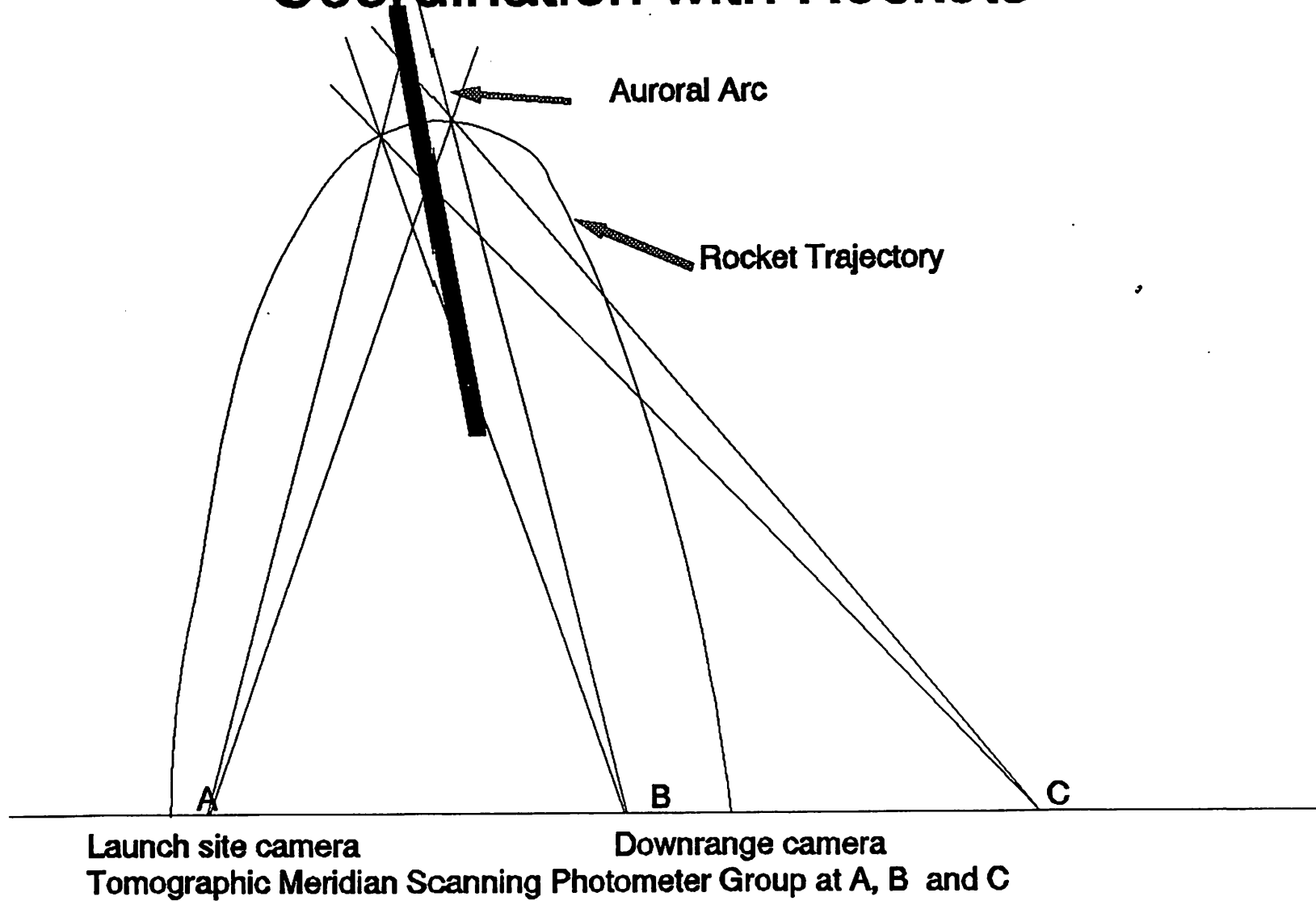
*( Analysis from CPI and JH4/APL )*



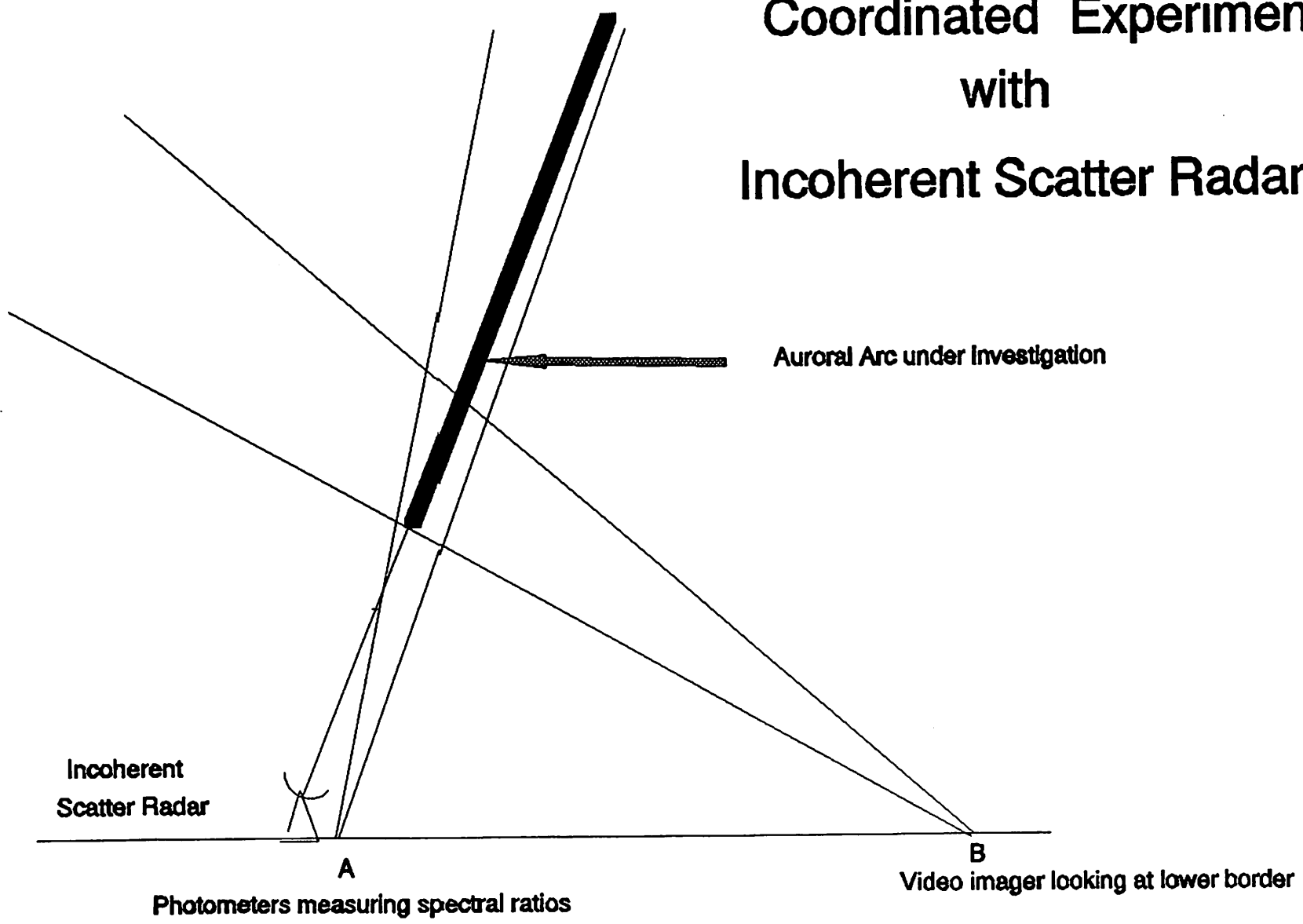
## General Guidelines

- 1) OPTICAL Observations provide a method for remotely determining atmospheric parameters
- 2) The Accuracy of these determinations depends on our knowledge of specific excitation and loss mechanisms cross sections and perhaps neutral and ion dynamics.
- 3) Characteristics of the geometry of the measurement impact the resolution of the derived parameters.
- 4) Simultaneous observations of different emissions are necessary to evaluate models which link emissions to atmospheric parameters.

# Coordination with Rockets



# Coordinated Experiments with Incoherent Scatter Radars





# THE PHOTOMETRIC MATRIX

$$I_{\lambda}(x,y,t)$$

- \* Imaging data fills in the values in this 3-D matrix. The instrument is truly multiplex, ie all dimensions in the matrix are filled at once.
- \* Data studies are usually shown in 2-D extracts. For any given position in the imaged field, "post-hoc" photometry can be performed giving

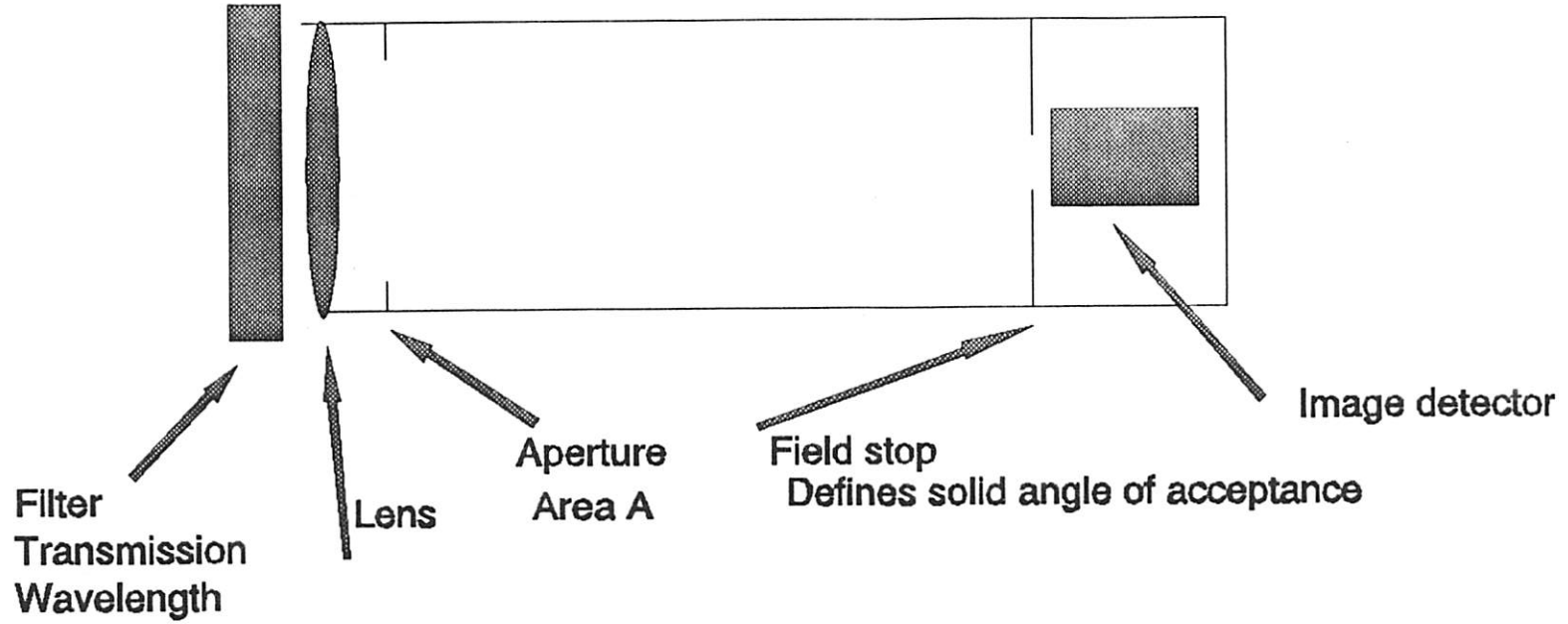
$$I_{x,y,\lambda}(t).$$

- \* Alternatively we can study spatial variations at an instant:

$$I_{\lambda,t}(x) \text{ or } I_{\lambda,t}(y)$$

- \* Studies in any of these spatial or temporal series must be done in the awareness that layer height and geometry can change without any direct knowledge from the measurement.
- \* Calibrations in intensity, flatfielding, optical distortion, and photometric linearity are required before that data have a scientific value. Also error bars must be determined.

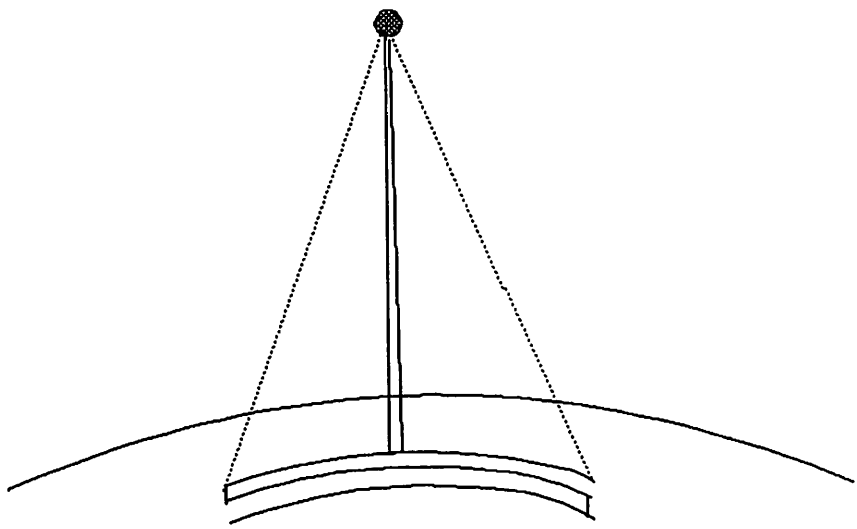
# Photometric Imager



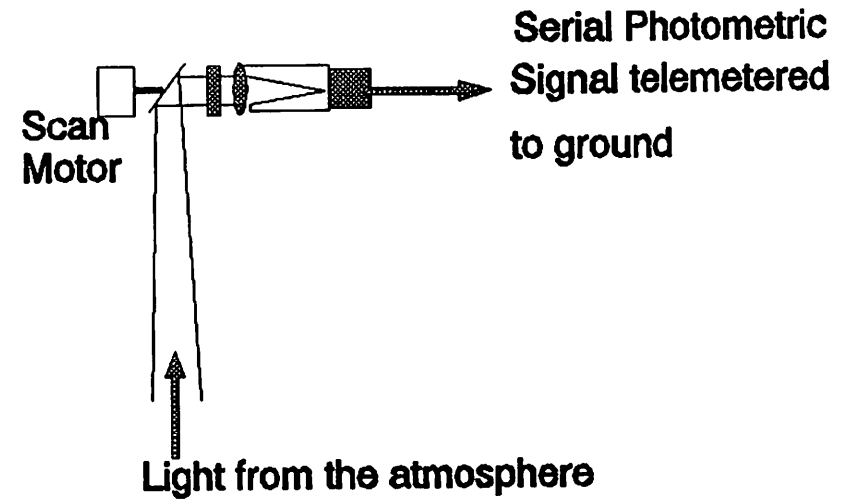
$$I = \frac{A\Omega}{4\pi} \times 10^6 \tau_L \tau_F Q$$

- A = the aperture of the optical component
- $\Omega$  = the solid angle of acceptance of the component
- $\tau_F$  = the transmission of a prefilter
- $\tau_L$  = the transmission of the lens or other component
- Q = the quantum efficiency of the detector

# Flying Spot Imager

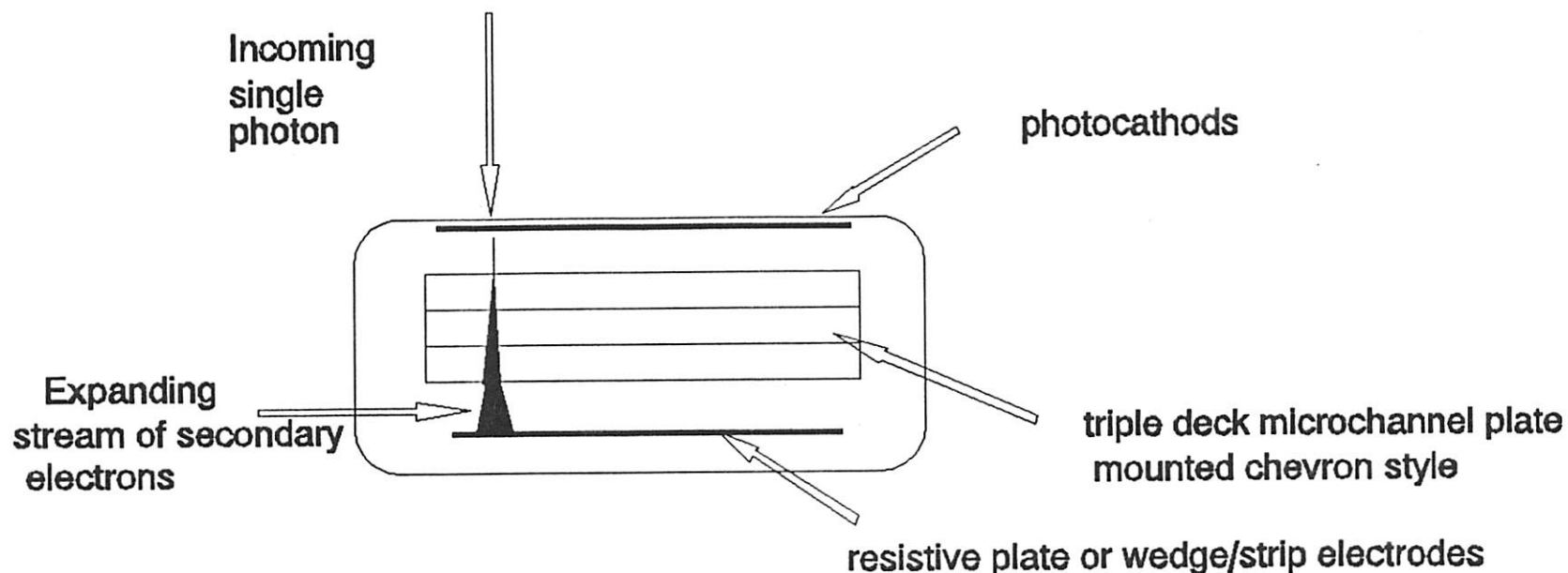


Light received from zig-zag track



Data quality depends upon the sensitivity and noise performance of the single channel photometer, and the brightness of the light source in the atmosphere.

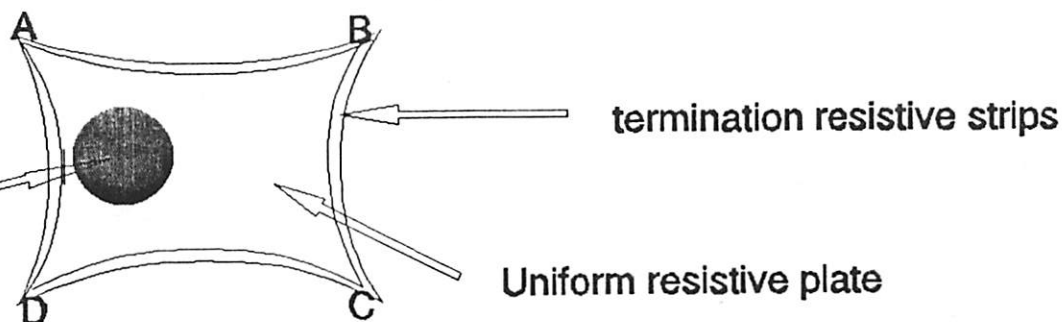
# The Imaging Photon Detector



$$x = \frac{(A+B) - (C+D)}{A+B+C+D}$$

$$y = \frac{(B+C) - (A+D)}{A+B+C+D}$$

Charge on anode spreads uniformly to electrodes



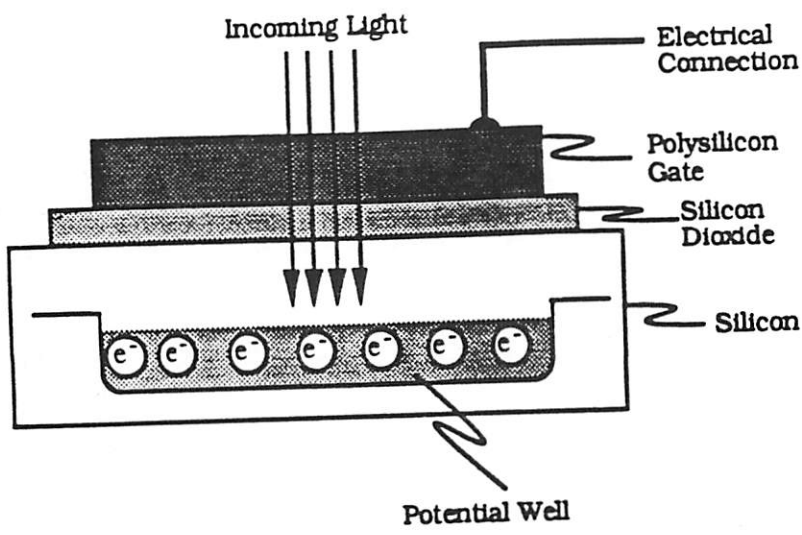


Figure 2-2. Cross-Section of a Simple Photodetector

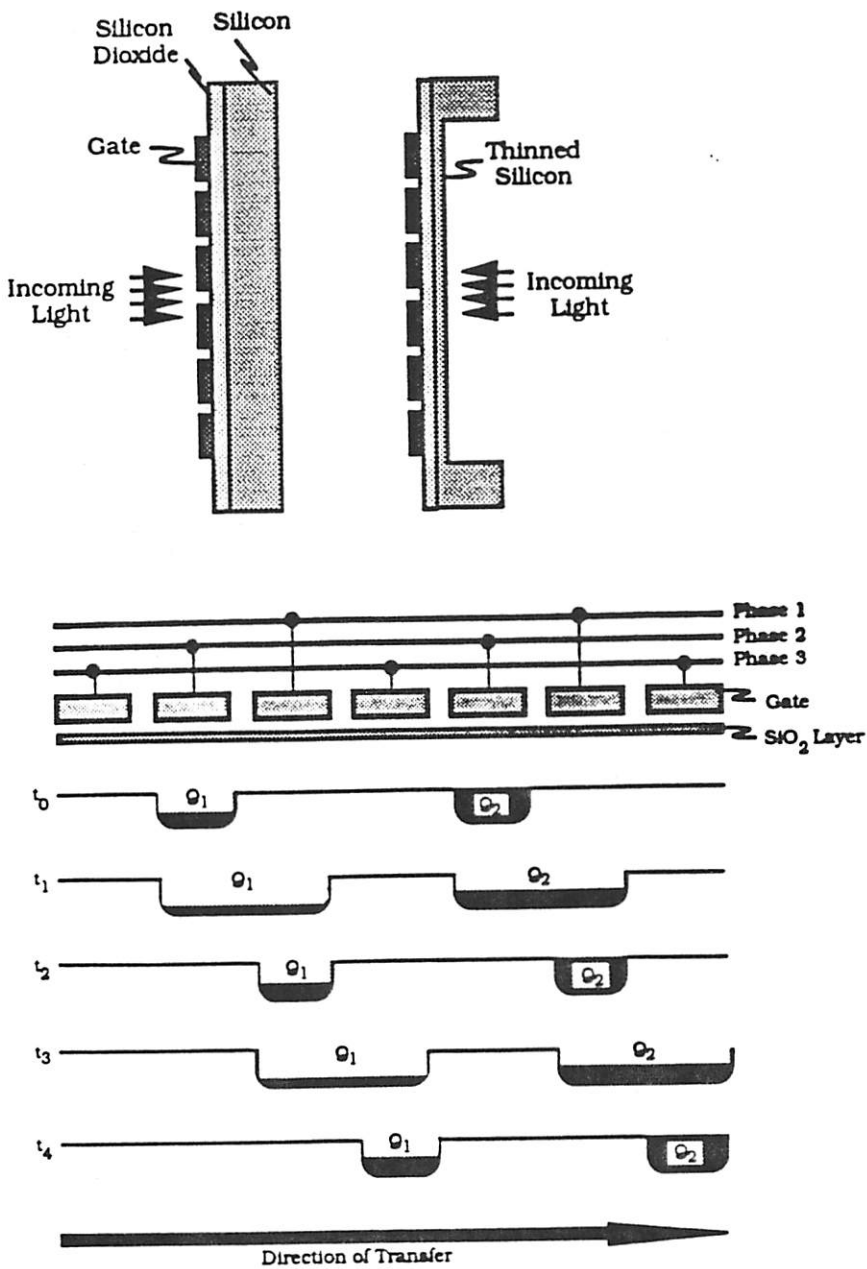


Figure 2-3. Charge Transfer in a 3-Phase CCD

# Image Intensifiers

Devices which convert an optical image to electronic form, amplify the signal and convert back to optical.

Conversion to electronic form is by a photocathode.  
 Amplification may involve secondary electrons  
 Conversion back to an optical image is by phosphor.

Focussing can be magnetic or electrostatic. (proximity).  
 Here is an electrostatic type.

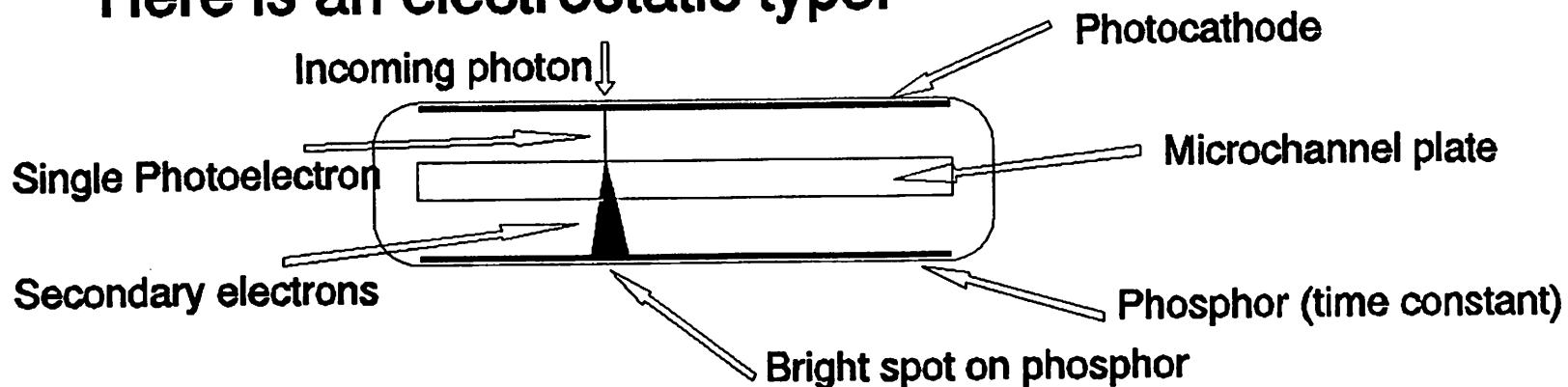
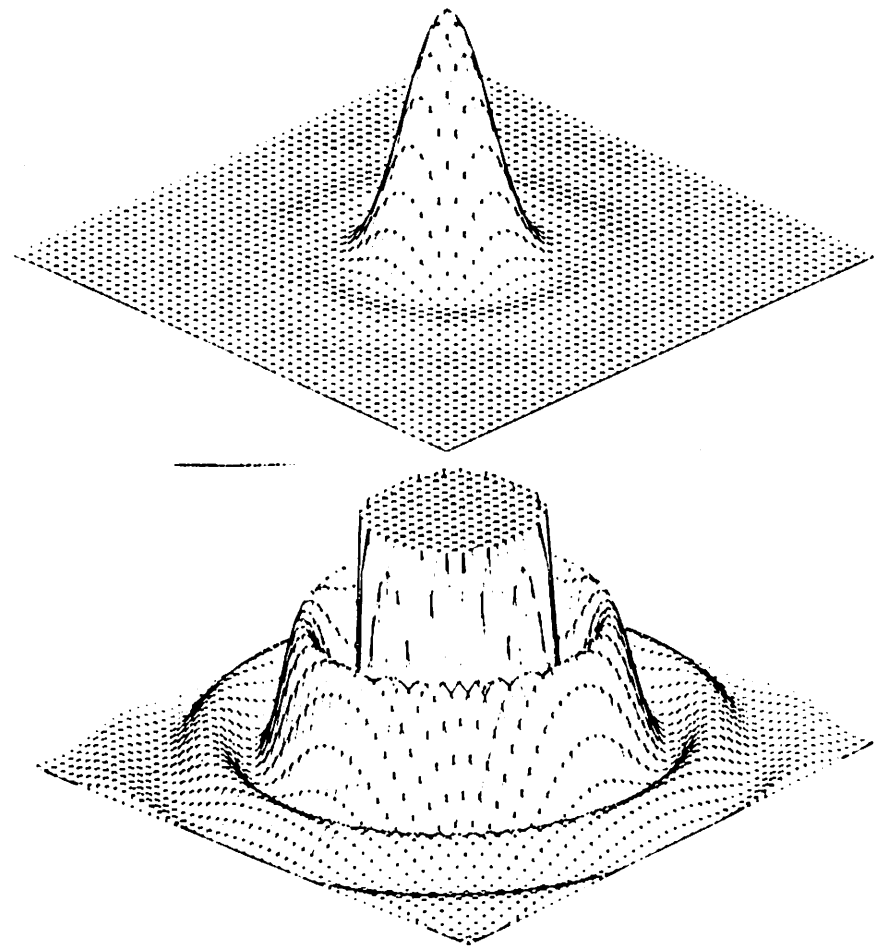
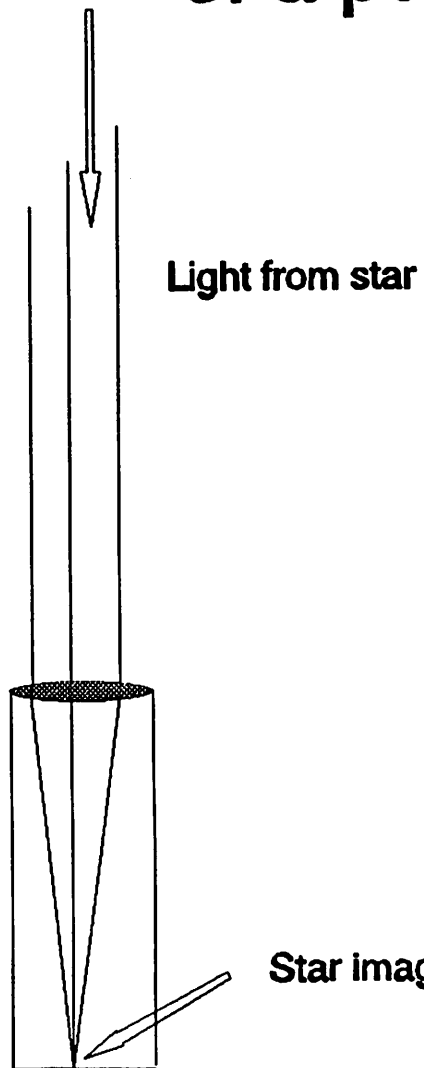


TABLE OF COMPARISON			
Criterion	CCD	IPD	Flying Spot
Wavelength sensitivity	$< 4000\text{\AA} - 11000\text{\AA}$	S25 <sup>*</sup> 3000-7500 $\text{\AA}$ GaAs <4000-9000 $\text{\AA}$	>25 GaAs Bi-Alk UM.
Read noise	2-10e/pix at 50MHz (increases with A/D speed)	N/A	N/A
Thermal noise	0.5e/s at -50°C using MPP <sup>†</sup> bias	$1.5 \times 10^{-3}$ e/s at 0°C for S25	$1-2\text{s}^{-1}$ dependent on cooling and photocathode
Spatial non-linearity	<0.2%	~1%	depends on satellite, stability and accuracy mirror ~0.1%.
Photometric non-linearity	1. Small up to full well.	dependent on dead time in processing and on any mcp <sup>††</sup> overload.	linear over 3-4 OM
Image brightness limitation	Full well ~250k electrons	mcp <sup>††</sup> overload dependent no limit on pixel storage except in computer.	dead time limited

\* Multi-pinned phase

†† microchannel plate.

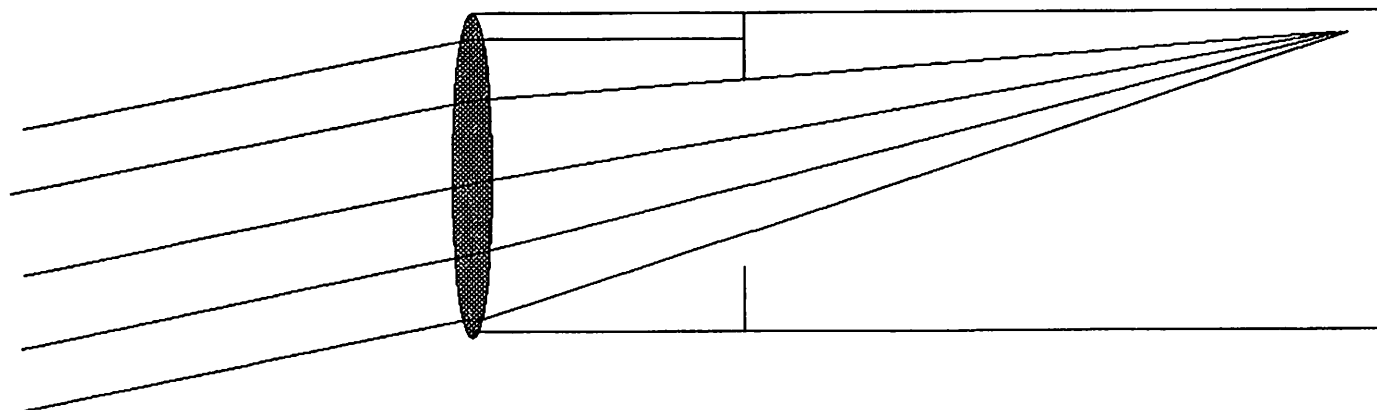
# Effect of diffraction on the image of a point source





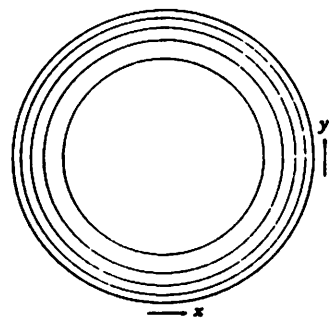
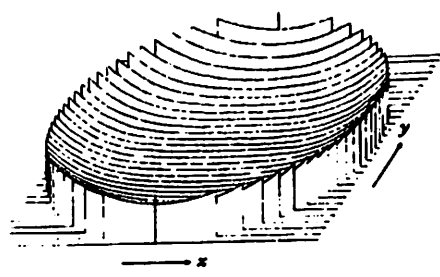
# Vignetting

Some off-axis rays are obstructed by camera structure

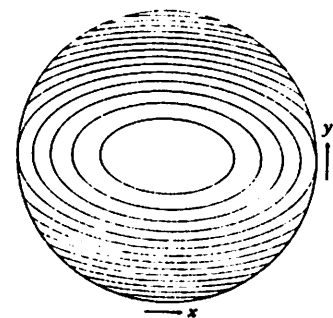
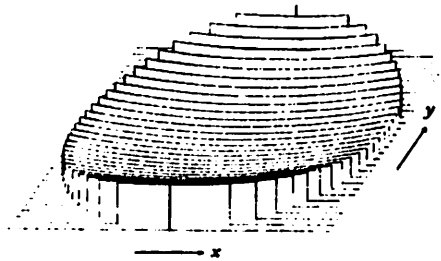


# Aberrations

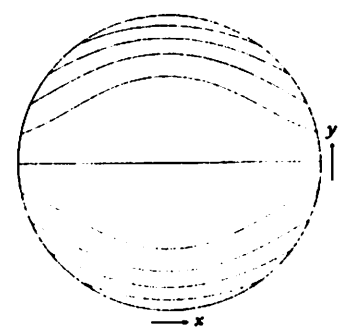
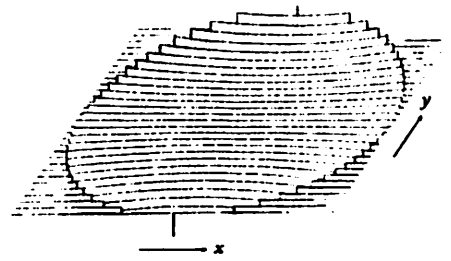
## Spherical



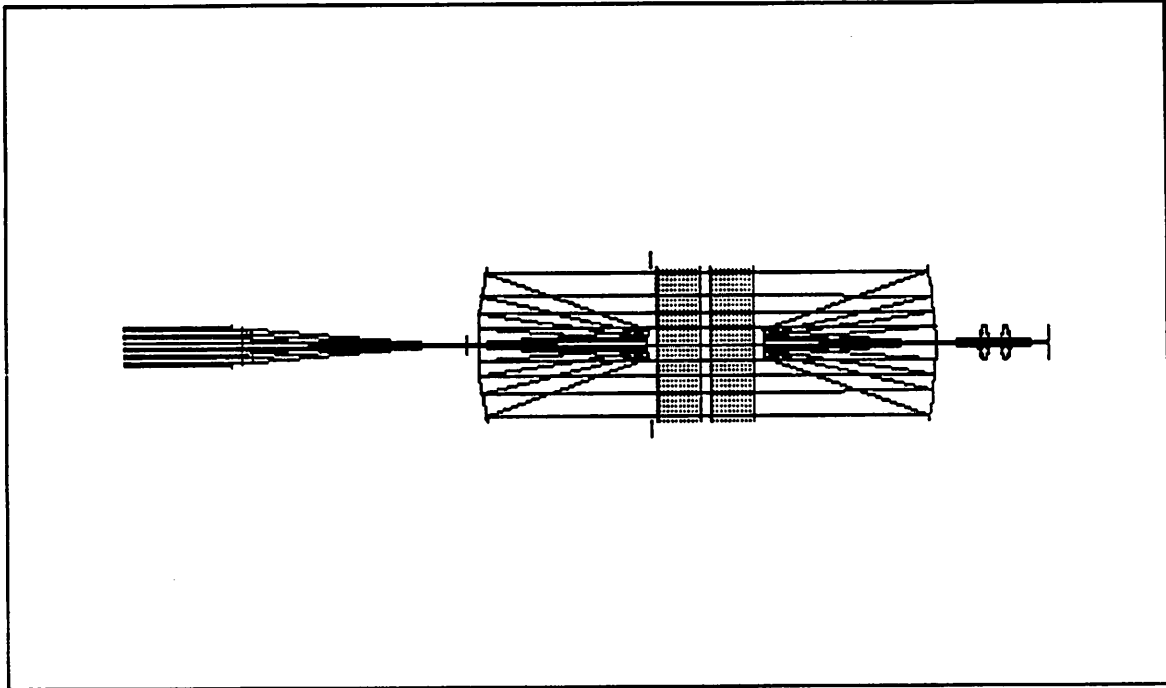
## Astigmatism



## Coma



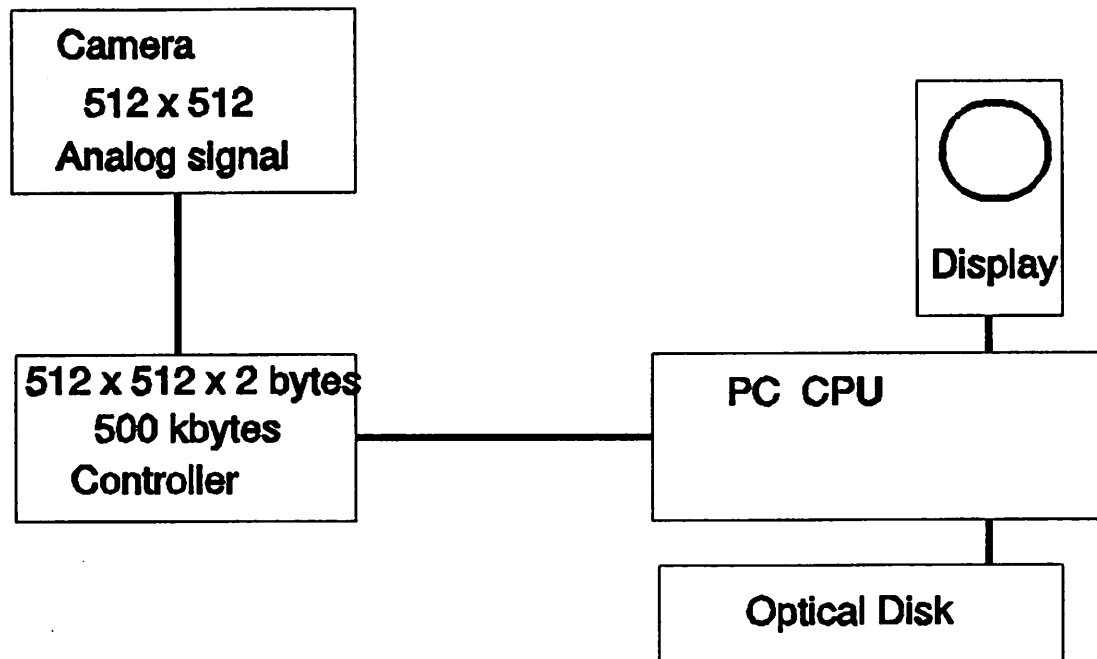
# CONSTANCY OF $A\Omega$



$$I = \frac{A\Omega}{4\pi} \times 10^6 \tau_L \tau_F Q$$

- A = the aperture of the optical component
- $\Omega$  = the solid angle of acceptance of the component
- $\tau_F$  = the transmission of a prefilter
- $\tau_L$  = the transmission of the lens or other component
- Q = the quantum efficiency of the detector

# Data Storage



# Imaging Speed

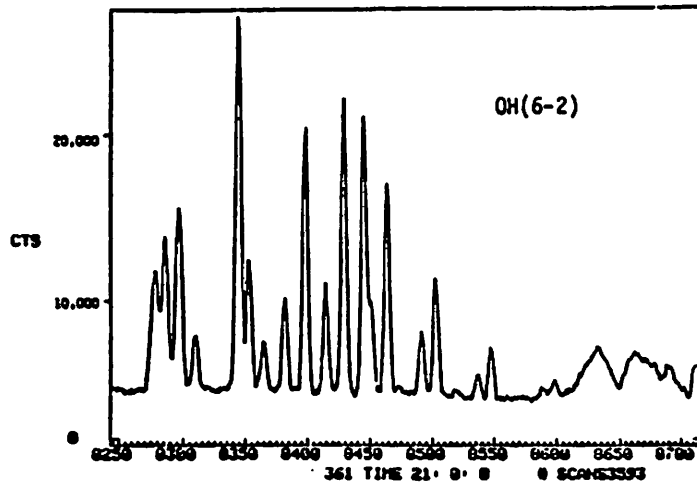
- Depends on shot, dark and read noise.
- Limited by speed of data handling and transfer to disk.
- For IPD also limited by the serial processing time.

# THE SPECTROPHOTOMETRIC MATRIX

$$I(\lambda, x, t)$$

- \* Data matrix in 3 dimensions:  
1 spectral, 1 spatial (along the slit), 1 time.
  
- \* Data studies (often 2-dimensional):
  - Spectral type:  
Spatial variations  $I_t(\lambda, x)$   
Temporal variations  $I_x(\lambda, t)$
  
  - Photometric study of one feature:  
Spatial variations  $I_\lambda(x, t)$   
Temporal variations  $I_\lambda(t, x)$
  
- \* Geometrical factors, such as the van Rhijn effect need to be considered in any spatial studies.

# Spectral Information in lines and bands



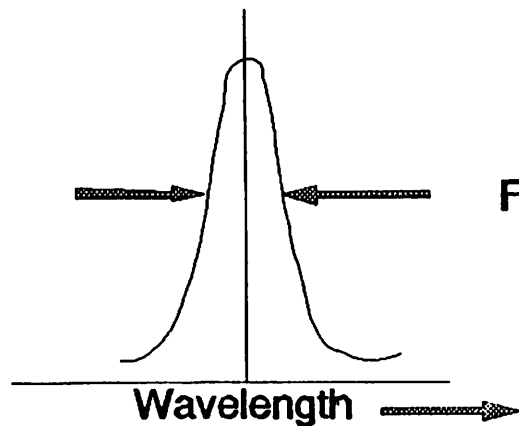
## Line and band intensities

Most information can be obtained with between 1 and 5Å resolution.

Peak shift  
47.6 m/s /mA at 6300A

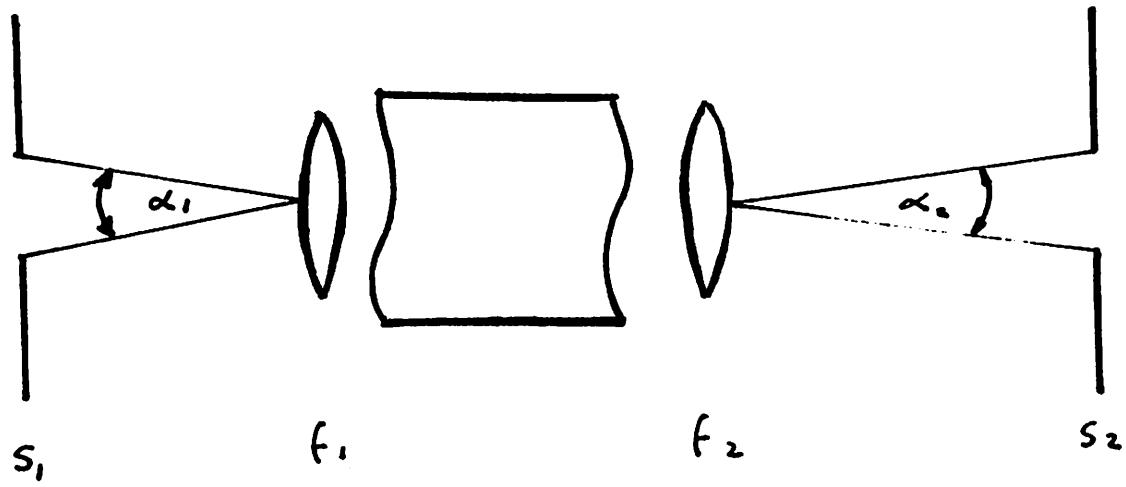


## Spectral line shapes



$$\begin{aligned} \text{FWHM} &= k \times \text{SQRT}(T/M) \\ &= 23.3 \text{ mA for } 5577\text{A OI at } 200\text{K} \\ &= 59.4 \text{ mA for } 6300\text{A OI at } 1000\text{K} \end{aligned}$$

GENERALIZED SPECTROMETER





**Spectral Properties:**

- a) Color ( Wavelength ).
- b) Shape.
- c) Area.
- d) Time behavior.

**Wavelength:**

$\lambda$ , expressed at 1 atmosphere, 15 C.  
 $\sigma = \lambda_o^{-1}$ , expressed in wavenumbers  
 (  $\text{cm}^{-1}$  .  $\lambda_o$ : vacuum wavelength.

**Resolving limit:**

$\delta\lambda$ : smallest resolvable spectral element,  
 in wavelength.  $\delta\sigma$ : smallest resolvable  
 spectral element, in wavenumbers.

**Resolving power:**

$$R = \delta\lambda / \lambda = \delta\sigma / \sigma .$$

**Flux delivered to the detector:**

$$F = I A \Omega \tau .$$

**Luminosity:**

$$L = F / I = A \Omega \tau .$$

**Angular dispersion:**

$$D = d\beta/d\lambda = d\beta/d\sigma .$$

**Spectral width:**

$$\omega = \Theta / D .$$

A spectrometer has a slit ( or aperture ) with angular width  $\Theta$  and angular height  $\Phi$ . The transmission properties for this aperture are given by  $\tau(\Theta, \Phi)$ . The associated solid angle is:

$$\Omega = \int_0^{2\pi} \int_0^{\Theta/2} \tau(\Theta, \Phi) \sin\Theta \, d\Theta \, d\Phi .$$

$$\Omega = 2 \pi [ 1 - \cos(\Theta/2) ] \approx \Theta^2 \quad ( \text{circular aperture} ) .$$

$$\Omega \approx \Theta\Phi \quad ( \text{otherwise} ) .$$

$$L \approx A \tau \Theta \Phi \quad \text{or} \quad A \tau \Theta^2 .$$

For one-dimensional dispersion devices, such as a grating or prism spectrometer:

$$\Theta = \omega D .$$

$$L_{sp} \approx A \tau \Phi \omega D = A \tau \Phi D \lambda R^{-1} .$$

For two-dimensional dispersion devices, such as Michelson and Fabry-Perot spectrometers:

$$\omega = \sigma \Theta^2 \delta^{-1} ,$$

$$L_{FP} \approx A \tau \delta \omega \sigma^{-1} = A \tau \delta R^{-1} .$$

For the specific case of a grating spectrometer at near-normal incidence with a grating with a blaze angle  $\gamma$ :

$$D = N n ( \cos\beta )^{-1} \quad ; \quad \sin\alpha + \sin\beta = N n \lambda ,$$

$$D = A ( \sin\alpha + \sin\beta ) ( A \cos\beta \lambda )^{-1} .$$

$A \cos\beta = A_o$ , where  $A_o$  is the area normal to the beam. In addition,  $\sin\alpha + \sin\beta = \sin(2\gamma)$ .

$$A_o D = A \sin 2\gamma \lambda^{-1} ,$$

$$L_g = \tau \Phi A \sin 2\gamma R^{-1} .$$

The comparison of the luminosity between these two types of dispersing spectrometers, **at equal resolving power**, assuming equal area grating and interference spectrometer pupils, is:

$$[ L_{FP} ( L_g )^{-1} ]_{A_{FP} = A_g} = 8 ( \Phi \sin 2\gamma )^{-1} .$$

For a typical grating with a blaze angle near  $15^\circ$  and a spectrometer with an angular height of 0.2 radians:

$$[ L_{FP} ( L_g )^{-1} ]_{A_{FP} = A_g} = 8 ( 0.2 \times 0.5 )^{-1} \approx 80 .$$

This comparison shows that, for the same resolving power, a 0.5 inch by 0.5 inch interference filter ( a special case of a Fabry-Perot device ) is as luminous as a grating spectrometer with a 4 inch by 5 inch grating.

Because of the larger luminosity of the two-dimensional dispersing devices, their use is preferentially directed to high-resolution studies where spectral line shapes and width measurements are desired.

The, simple, instruments described above have a **Luminosity  $\times$  Resolving-Power** product that is constant. However, there exist another class of instruments that are inherently **compensated** or can be compensated. A compensated device has the

property of a **Luminosity  $\times$  Resolving-Power** product that *increases* with increasing Resolving Power. They will not be discussed here.

Purposely, the above discussion has been limited to the flux delivered to the detector, and this detector is considered to be large enough to accept the flux for one resolvable element. A single detector requires that the spectrum be scanned across this detector, while a multiple detector device can observe many spectral elements simultaneously (multiplexing). For intrinsically-noisy detectors, it is possible to detect multiple wavelengths simultaneously and still have a net gain ( Fellgett advantage ). This technique is employed with Michelson devices in the infrared region.

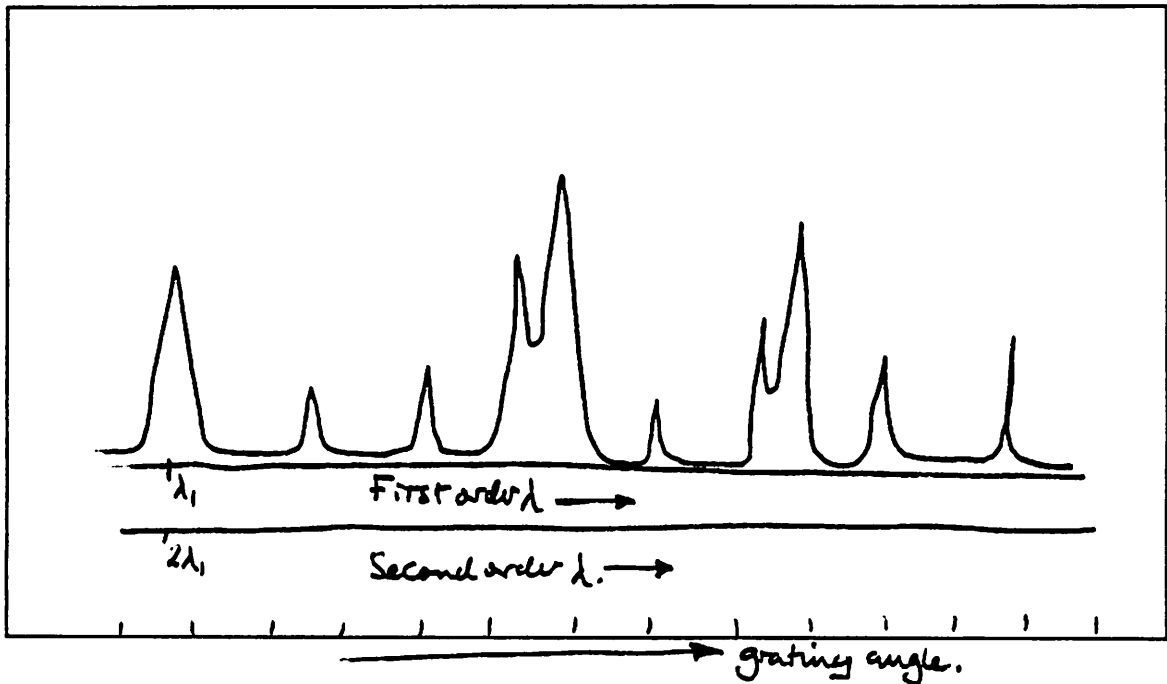
Finally, there is the topic of selectivity, that is the ability of a given spectrometer to observe an arbitrary region of the spectrum without instrumentally-caused contamination from other regions. In general, grating instruments have greater selectivity, although interference devices can be made to approach this selectivity.

#### Selected References

- F. A. Jenkins and H. E. White, *Fundamentals of Optics*, McGraw-Hill, Inc., New York, 1976
- R. W. Wood, *Physical Optics*, Optical Society of America, Washington, 1988
- G. Hernandez, *Fabry-Perot Interferometers*, Cambridge University Press, Cambridge, 1988
- Born, M. and E. Wolf. *Principles of Optics*, The MacMillan Co, New York, 1954

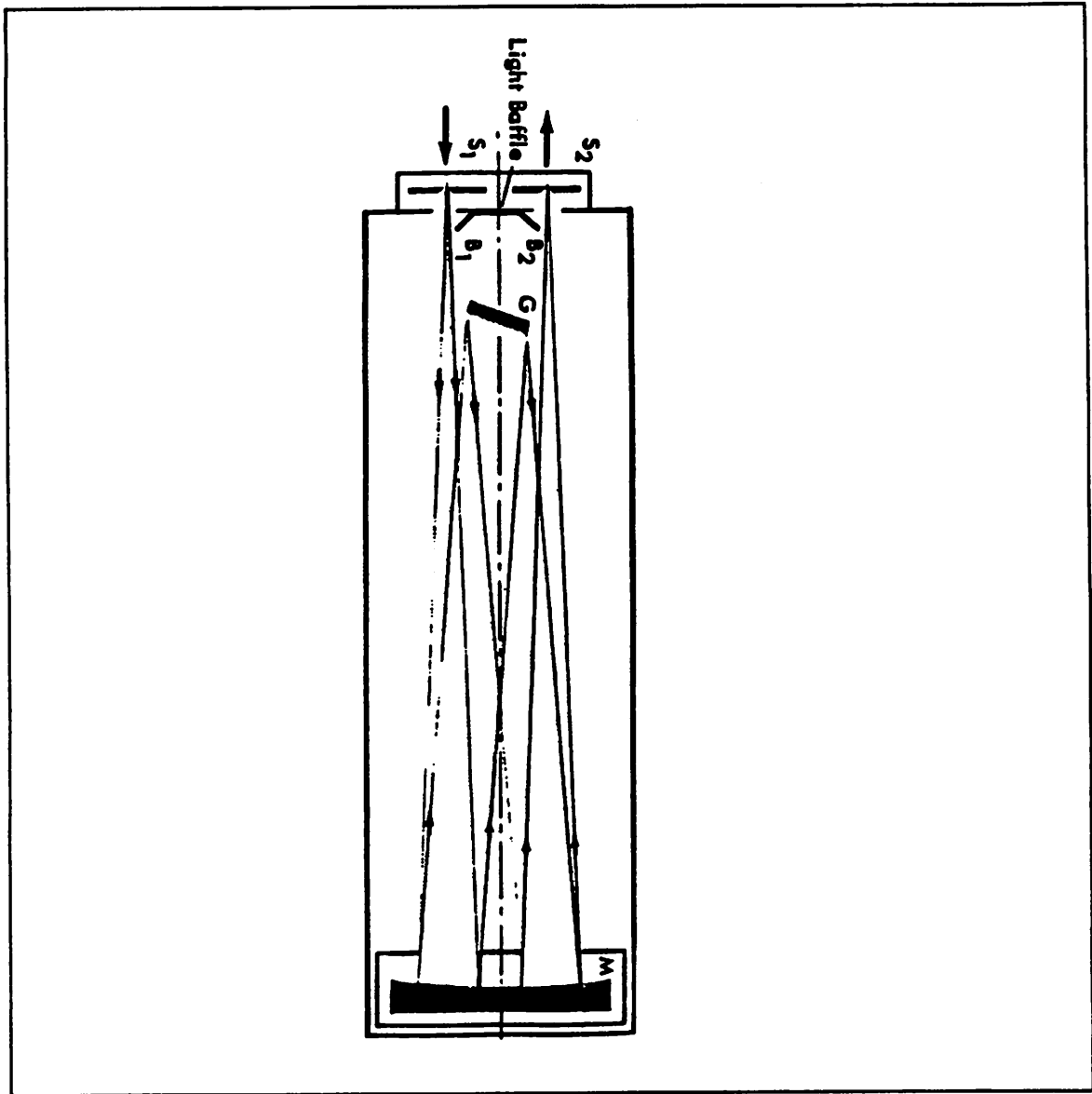
# OVERLAPPING ORDERS

$$2d\sin\theta = p_1\lambda_1 = p_2\lambda_2 = \dots$$



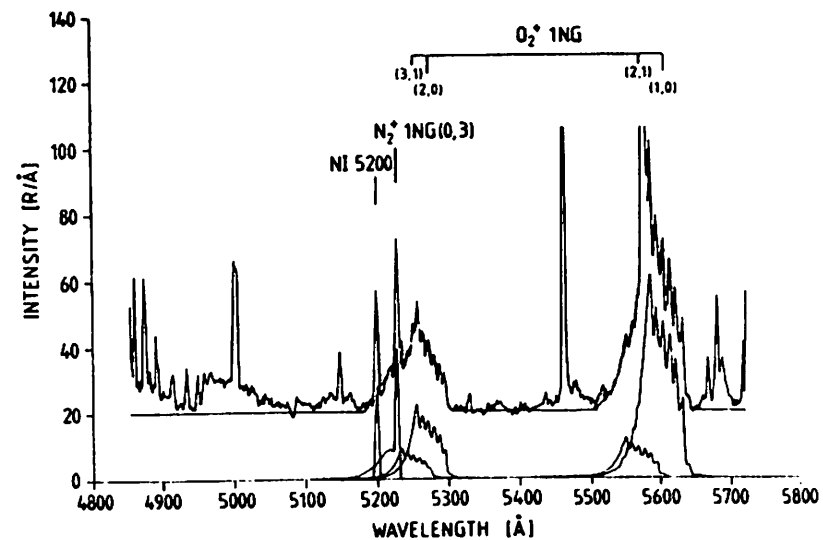
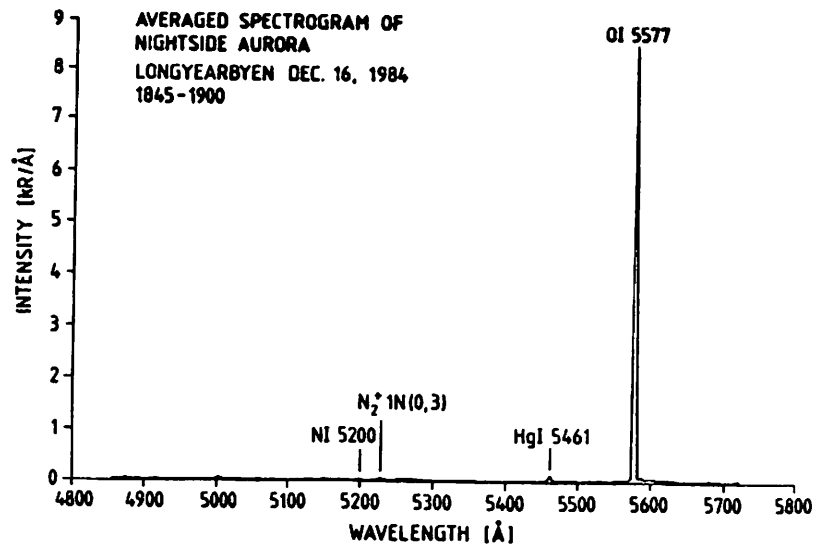
Use an order-sorter filter which absorbs the higher orders at shorter wavelengths.

# STRAY LIGHT

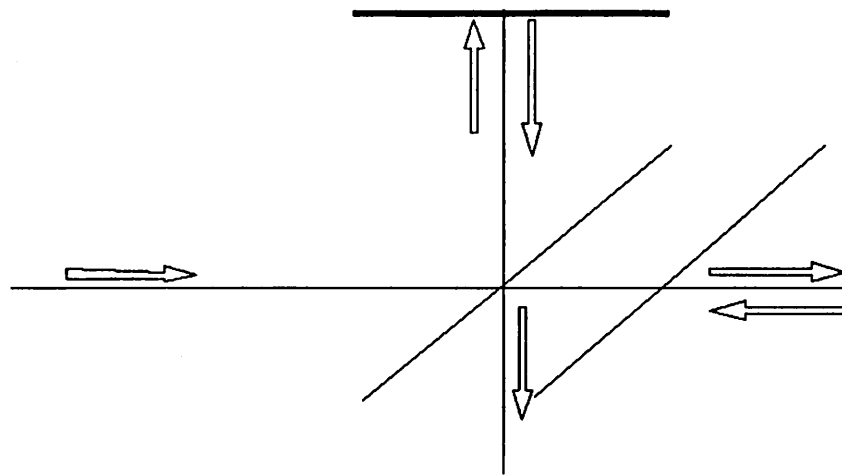


# Dynamic Range of the Detector

Example: structure at the base of the 5577 line  
molecular oxygen first negative bands.

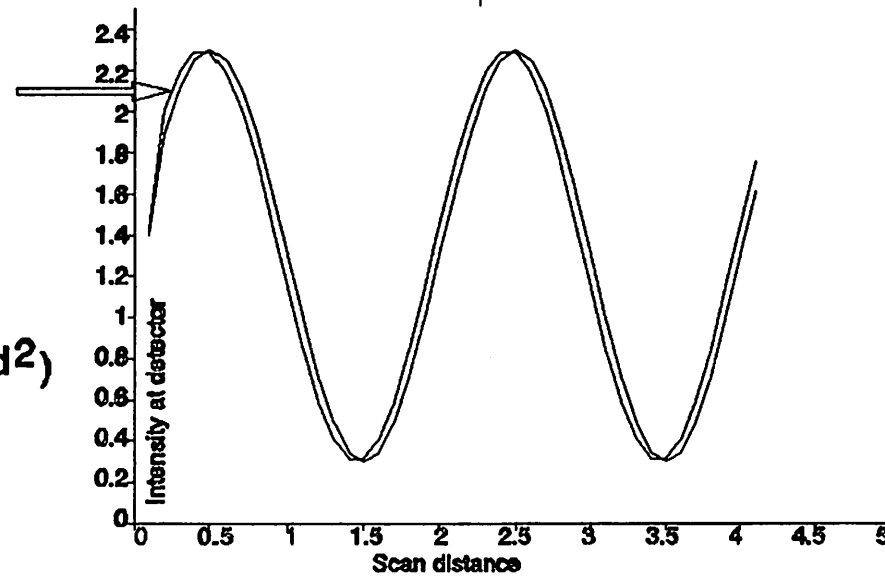


# Michelson Interferometer



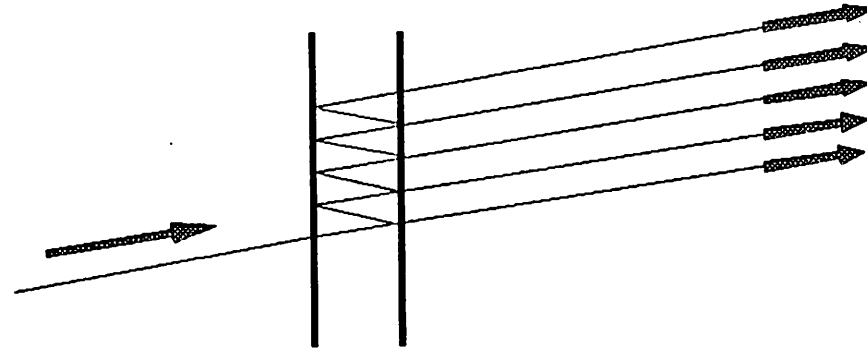
$B(1 + \cos(6.28sd))$   
 $s = \text{wavenumber}$   
 $d = \text{path difference}$

Visibility =  $\exp(-Qd^2)$



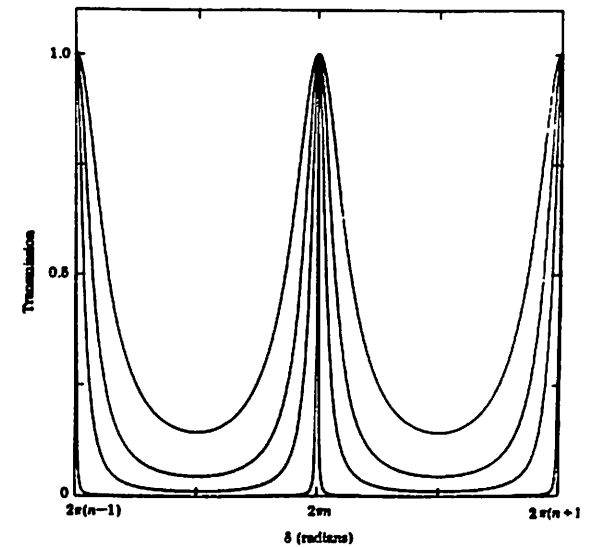


# Fabry Perot Etalon



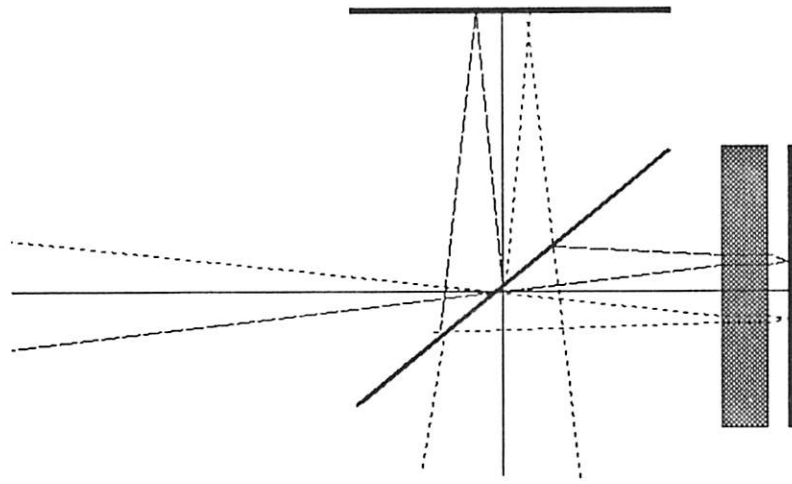
Instrument Function

$AT^2$



Sensitive to pressure (gas refractive index)  
temperature  
vibration

# Field Widening for Michelson Interferometer



→ Maintains the quasi-zero path condition when the path difference is non-zero and the rays are off-axis

→ utilizing a glass block whose thickness is specific to the geometrical paths.

# Field-Widening a Fabry-Perot Spectrometer

## The Dual Etalon Modulator Approach

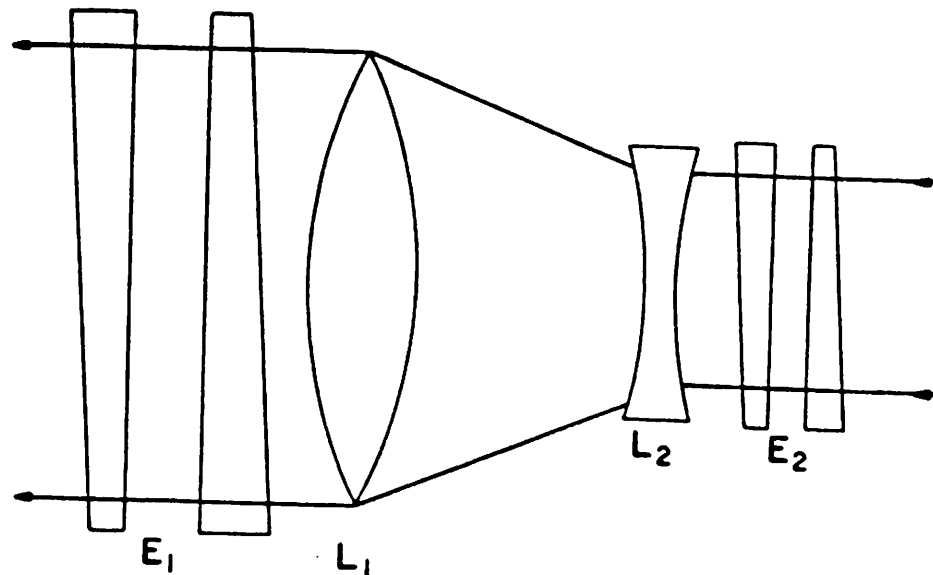


Fig. 1. Schematic representation of the beam expander used to couple the two etalons ( $E_1$  and  $E_2$ ) in this experiment.

# FPI SCANNING

$$2nd\cos\theta = p\lambda$$

For pinhole scanning,  $\theta$  may be considered close to zero  
and  $\cos\theta = 1$

$$\text{Hence } 2nd = p\lambda$$

Pressure scanning:  $p, d$  constant, vary  $n$  to scan  $\lambda$   
this is refractive index scanning

Piezo scanning:  $n, p$  constant, vary  $d$  to scan  $\lambda$   
this is scanning in plate separation

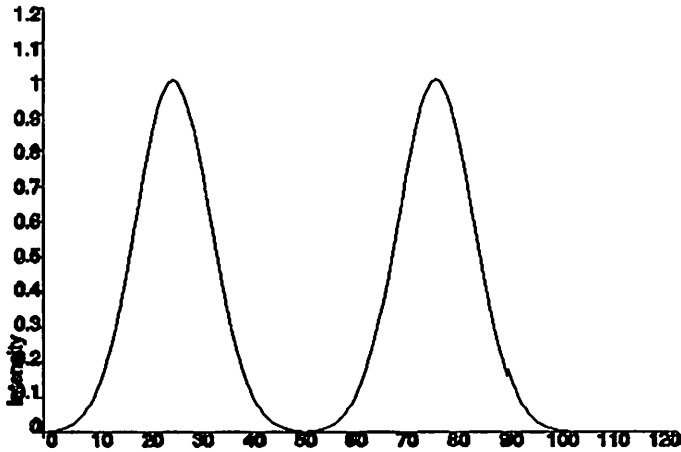
For spatial scanning, we may assume that  $\theta$  is small so that  
 $\cos\theta = 1 - \theta^2/2$

$$\text{Hence } \theta^2 = (p - p_0)/p_0$$

where  $p_0$  is the order at the center of the pattern.

Since  $\theta$  is proportional to fringe radius,  $p \propto \text{radius}^2$

## Finding the peak wavelength of a profile



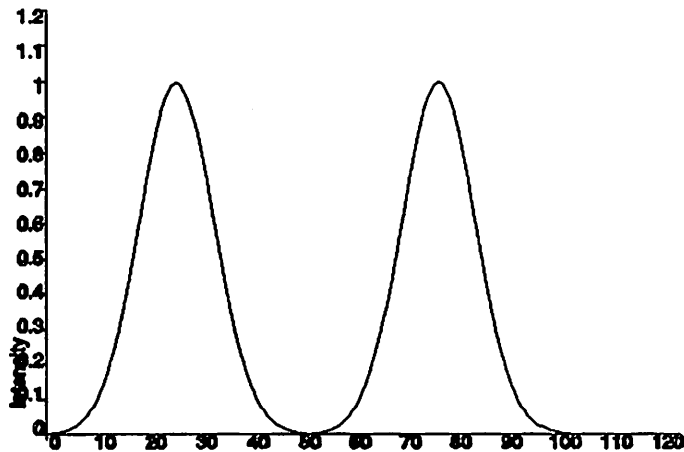
- \* Use a fit function
- or
- \* Use the phase of FT
- or
- \* Other suitable technique

For emissions not available in laboratory discharges

- \* get zero wavelength by averaging zenith

Scale velocities using standard Doppler theory.

# Getting the Temperature from the spectrum



- \* Analyze using one FSR
- \* Remove instrument function
- \* Find best fit to Gaussian curve for T at given M.
- \* Check for Gaussian shape.

